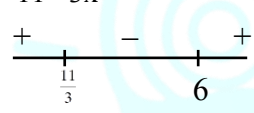
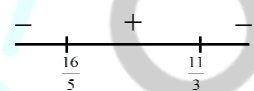
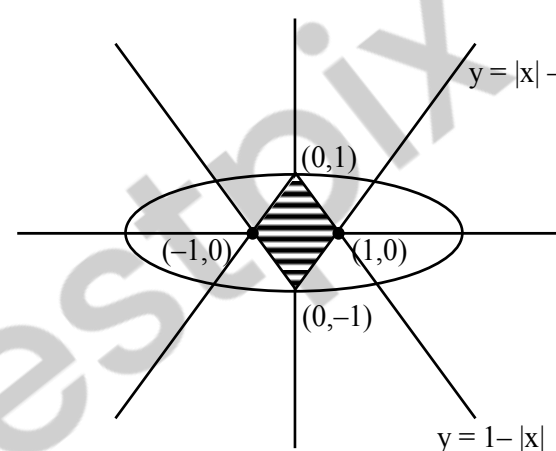


(HELD ON WEDNESDAY 21st JANUARY 2026)
TIME : 9:00 AM TO 12:00 NOON

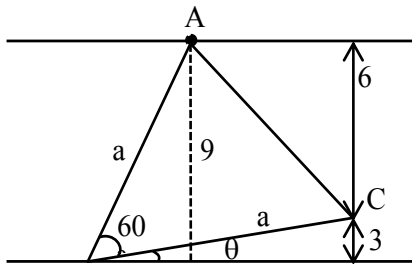
MATHEMATICS	TEST PAPER WITH SOLUTION																
SECTION-A 1. If the domain of the function $f(x) = \cos^{-1}\left(\frac{2x-5}{11-3x}\right) + \sin^{-1}(2x^2 - 3x + 1)$ is the interval $[\alpha, \beta]$, then $\alpha + 2\beta$ is equal to : (1) 1 (2) 3 (3) 5 (4) 2 Ans. (2) Sol. $f(x) = \cos^{-1}\left(\frac{2x-5}{11-3x}\right) + \sin^{-1}(2x^2 - 3x + 1)$ $-1 \leq \frac{2x-5}{11-3x} \leq 1$ $-1 \leq 2x^2 - 3x + 1 \leq 1$ $2x^2 - 3x + 2 \geq 0, 2x^2 - 3x \leq 0$ $x \in \left[0, \frac{3}{2}\right] \dots (i)$ $\frac{2x-5}{11-3x} + 1 \geq 0$ $\frac{2x-5+11-3x}{11-3x} \geq 0$ $\frac{6-x}{11-3x} \geq 0$  $\frac{2x-5}{11-3x} - 1 \leq 0$ $\frac{5x-16}{11-3x} \leq 0$  $x \in \left(-\infty, \frac{16}{5}\right] \cup \left(\frac{11}{3}, \infty\right)$ $x \in \left(-\infty, \frac{11}{3}\right) \cup [6, \infty)$ intersection $x \in \left(-\infty, \frac{16}{5}\right] \cup [6, \infty) \dots (ii)$ Intersection of (i) & (ii) $x \in \left[0, \frac{3}{2}\right]$ $\alpha = 0, \beta = \frac{3}{2} \Rightarrow \alpha + 2\beta = 3$	2. The area of the region, inside the ellipse $x^2 + 4y^2 = 4$ and outside the region bounded by the curves $y = x - 1$ and $y = 1 - x$, is : (1) $2(\pi - 1)$ (2) $2\pi - \frac{1}{2}$ (3) $3(\pi - 1)$ (4) $2\pi - 1$ Ans. (1) Sol.  Required area = area of ellipse – shaded area $= \pi \times 2 \times 1 - 4 \left(\frac{1}{2} \times 1 \times 1\right) = 2\pi - 2$ 3. The number of relations, defined on the set $\{a, b, c, d\}$, which are both reflexive and symmetric, is equal to: (1) 256 (2) 16 (3) 1024 (4) 64 Ans. (4) Sol. Number of relation which are reflexive and sym. both $= 1^4 \times 2^6 = 64$ <table style="width: 100%; text-align: center; margin-top: 10px;"> <tr> <td>(a, a)</td><td>(a, b)</td><td>(a, c)</td><td>(a, d)</td></tr> <tr> <td>(b, a)</td><td>(b, b)</td><td>(b, c)</td><td>(b, d)</td></tr> <tr> <td>(c, a)</td><td>(c, b)</td><td>(c, c)</td><td>(c, d)</td></tr> <tr> <td>(d, a)</td><td>(d, b)</td><td>(d, c)</td><td>(d, d)</td></tr> </table>	(a, a)	(a, b)	(a, c)	(a, d)	(b, a)	(b, b)	(b, c)	(b, d)	(c, a)	(c, b)	(c, c)	(c, d)	(d, a)	(d, b)	(d, c)	(d, d)
(a, a)	(a, b)	(a, c)	(a, d)														
(b, a)	(b, b)	(b, c)	(b, d)														
(c, a)	(c, b)	(c, c)	(c, d)														
(d, a)	(d, b)	(d, c)	(d, d)														



4. Let a point A lie between the parallel lines L_1 and L_2 such that its distances from L_1 and L_2 are 6 and 3 units, respectively. Then the area (in sq. units) of the equilateral triangle ABC, where the points B and C lie on the lines L_1 and L_2 respectively, is :

- (1) $15\sqrt{6}$ (2) 27
(3) $21\sqrt{3}$ (4) $12\sqrt{2}$

Ans. (3)



Sol.

$$\sin \theta = \frac{3}{a}$$

$$\sin (60^\circ + \theta) = \frac{9}{a}$$

$$\frac{\sqrt{3}}{2} \cos \theta + \frac{1}{2} \sin \theta = \frac{9}{a}$$

$$\sqrt{3} \sqrt{1 - \frac{9}{a^2}} + \frac{3}{a} = \frac{18}{a}$$

$$a = \sqrt{84}$$

$$\text{Area of } \triangle ABC = \frac{\sqrt{3}}{4} a^2 = \frac{\sqrt{3}}{4} \times 84 = 21\sqrt{3}$$

5. Let $\vec{a} = -\hat{i} + 2\hat{j} + 2\hat{k}$, $\vec{b} = 8\hat{i} + 7\hat{j} - 3\hat{k}$ and $\vec{c}$ be a vector such that $\vec{a} \times \vec{c} = \vec{b}$. If $\vec{c} \cdot (\hat{i} + \hat{j} + \hat{k}) = 4$, then $|\vec{a} + \vec{c}|^2$ is equal to :

- (1) 33 (2) 30
(3) 35 (4) 27

Ans. (4)

Sol. $\vec{a} = -\hat{i} + 2\hat{j} + 2\hat{k}$

$$\vec{b} = 8\hat{i} + 7\hat{j} - 3\hat{k}$$

$$\vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$$

$$\vec{a} \times \vec{c} = \vec{b} \Rightarrow (2c_3 - 2c_2)\hat{i} + (c_3 + 2c_1)\hat{j} - (c_2 + 2c_1)\hat{k} = 8\hat{i} + 7\hat{j} - 3\hat{k}$$

$$2c_3 - 2c_2 = 8, c_3 + 2c_1 = 7, c_2 + 2c_1 = 3$$

$$(c_1\hat{i} + c_2\hat{j} + c_3\hat{k}) \cdot (\hat{i} + \hat{j} + \hat{k}) = 4$$

$$\Rightarrow c_1 + c_2 + c_3 = 4, c_1 = 2, c_2 = -1, c_3 = 3$$

$$|\vec{a} + \vec{c}|^2 = |\hat{i} + \hat{j} + 5\hat{k}|^2 = 27$$

6. Let $a_1, a_2, a_3, \dots$ be a G.P. of increasing positive terms such that $a_2 a_3 a_4 = 64$ and $a_1 + a_3 + a_5 = \frac{813}{7}$.

Then $a_3 + a_5 + a_7$ is equal to :

- (1) 3256 (2) 3252
(3) 3244 (4) 3248

Ans. (2)

Sol. $ar \cdot ar^2 \cdot ar^3 = 64$

$$a^3 r^6 = 64 \Rightarrow ar^2 = 4$$

$$a + ar^2 + ar^4 = \frac{813}{7}$$

$$r^2 = 28$$

$$ar^2 + ar^4 + ar^6 = ?$$

$$ar^2 (1 + r^2 + r^4) = 4 (1 + 28 + 784) = 3252$$

7. Let $\vec{c}$ and $\vec{d}$ be vectors such that $|\vec{c} + \vec{d}| = \sqrt{29}$ and $\vec{c} \times (2\hat{i} + 3\hat{j} + 4\hat{k}) = (2\hat{i} + 3\hat{j} + 4\hat{k}) \times \vec{d}$. If $\lambda_1, \lambda_2 (\lambda_1 > \lambda_2)$ are the possible values of $(\vec{c} + \vec{d}) \cdot (-7\hat{i} + 2\hat{j} + 3\hat{k})$, then the equation

$$K^2 x^2 + (K^2 - 5K + \lambda_1)xy + \left(3K + \frac{\lambda_2}{2}\right)y^2 - 8x + 12y + \lambda_2 = 0$$

represents a circle, for k equal to :

- (1) 4 (2) 1
(3) -1 (4) 2

Ans. (2)

Sol. $|\vec{c} + \vec{d}| = \sqrt{29}$

$$\vec{c} + \vec{d} = \lambda ((2\hat{i} + 3\hat{j} + 4\hat{k}))$$

$$\lambda = \pm 1$$

$$\lambda(-14 + 6 + 12) = 4\lambda, \lambda_1 = 4, \lambda_2 = -4$$

$$k^2x^2 + (k^2 - 5k + 4)xy + (3k - 2)y^2 - 8x + 12y - 4 = 0$$

is circle

$$k^2 - 5k + 4 = 0 \Rightarrow k = 1, 4$$

$$k^2 = 3k - 2 \Rightarrow k = 1, 2$$

$$k = 1$$

8. Let $y = y(x)$ be the solution curve of the differential equation $(1 + x^2)dy + (y - \tan^{-1}x)dx = 0$, $y(0) = 1$. Then the value of $y(1)$ is :

$$(1) \frac{2}{e^4} + \frac{\pi}{4} - 1$$

$$(2) \frac{2}{e^4} - \frac{\pi}{4} - 1$$

$$(3) \frac{4}{e^4} + \frac{\pi}{2} - 1$$

$$(4) \frac{4}{e^4} - \frac{\pi}{2} - 1$$

Ans. (1)

Sol. $\frac{dy}{dx} + \frac{y}{x^2 + 1} = \frac{\tan^{-1}x}{x^2 + 1}$

$$\text{I.f.} = e^{\tan^{-1}x}$$

$$y \times e^{\tan^{-1}x} = \int e^{\tan^{-1}x} \cdot \frac{\tan^{-1}x}{1 + x^2} dx$$

$$y \times e^{\tan^{-1}x} = \tan^{-1}x (e^{\tan^{-1}x}) - e^{\tan^{-1}x} + c$$

$$y(0) = 1 \Rightarrow c = 2$$

$$y(1) = \frac{2}{e^{\pi/4}} + \frac{\pi}{4} - 1$$

9. The number of strictly increasing functions f from the set $\{1, 2, 3, 4, 5, 6\}$ to the set $\{1, 2, 3, \dots, 9\}$ such that $f(i) \neq i$ for $1 \leq i \leq 6$, is equal to :

$$(1) 21$$

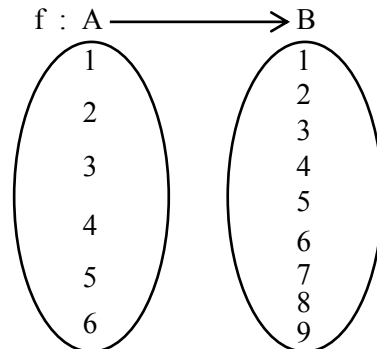
$$(2) 27$$

$$(3) 22$$

$$(4) 28$$

Ans. (4)

- Sol.** $f(i) \neq i$, $f(x)$ is strictly increasing function $f: A \rightarrow B$, where $A = \{1, 2, 3, \dots, 6\}$
 $B = \{1, 2, 3, \dots, 9\}$, then number of function $f: A \rightarrow B$ is equal to



$$f(i) \neq i \text{ Case - i } f(1) = 2 \Rightarrow {}^7C_5 = 21$$

$$\text{Case- ii } f(1) = 3 \Rightarrow {}^6C_5 = 6$$

$$\text{Case- iii } f(1) = 4 \Rightarrow {}^5C_5 = 1$$

$$\text{No of function } A \text{ to } B = 21 + 6 + 1 = 28$$

10. Let $f: \mathbb{R} \rightarrow (0, \infty)$ be a twice differentiable function such that $f(3) = 18$, $f'(3) = 0$ and $f''(3) = 4$.

Then $\lim_{x \rightarrow 1} \left(\log_e \left(\frac{f(2+x)}{f(3)} \right)^{\frac{18}{(x-1)^2}} \right)$ is equal to :

$$(1) 1$$

$$(2) 9$$

$$(3) 2$$

$$(4) 18$$

Ans. (3)

Sol. Let $T = \lim_{x \rightarrow 1} \left(\frac{f(x+2)}{f(3)} \right)^{\frac{18}{(x-1)^2}}$; 1^∞ form

$$\Rightarrow T = e^{\lim_{x \rightarrow 1} \frac{18}{(x-1)^2} \left(\frac{f(x+2) - f(3)}{f(3)} \right)}$$

$$\Rightarrow T = e^{\lim_{x \rightarrow 1} \frac{18}{(x-1)^2} \left(\frac{f(x+2) - f(3)}{18} \right)}$$

$$\Rightarrow T = e^{\lim_{x \rightarrow 1} \left(\frac{f(x+2) - f(3)}{(x-1)^2} \right) \frac{0}{0} \text{ form}} \text{ apply L' pital}$$

$$\Rightarrow T = e^{\lim_{x \rightarrow 1} \frac{f'(x+2)}{2(x-1)} \frac{0}{0} \text{ form}} \text{ apply L' pital}$$

$$\Rightarrow T = e^{\lim_{x \rightarrow 1} \frac{f''(x+2)}{2} \frac{4}{2}} = e^{\frac{4}{2}} = e^2$$

$$\Rightarrow \log_e (T) = 2$$

11. Let the foci of hyperbola coincide with the foci of the ellipse $\frac{x^2}{36} + \frac{y^2}{16} = 1$. If the eccentricity of the hyperbola is 5, then the length of its latus rectum is:

- (1) 12 (2) 16
(3) $\frac{96}{\sqrt{5}}$ (4) $24\sqrt{5}$

Ans. (3)

Sol. Let e_1 be eccentricity of ellipse

$$\Rightarrow e_1 = \sqrt{1 - \frac{16}{36}} = \sqrt{1 - \frac{4}{9}} = \frac{\sqrt{5}}{3}$$

$$\text{So } ae_1 = 6 \cdot \frac{\sqrt{5}}{3} = 2\sqrt{5}$$

$$\text{Now H: } \frac{x^2}{p^2} - \frac{y^2}{q^2} = 1$$

$$p \cdot e = ae_1$$

$$p \cdot 5 = 2\sqrt{5}$$

$$p = \frac{2}{\sqrt{5}} \Rightarrow e^2 = 1 + \frac{q^2}{p^2} \Rightarrow 25 = 1 + \frac{5q^2}{4} \Rightarrow q^2 = \frac{96}{5}$$

$$\text{So length of LR } \frac{2q^2}{p} = \frac{96}{\sqrt{5}}$$

12. The value of $\int_{-\pi/6}^{\pi/6} \left(\frac{\pi + 4x^{11}}{1 - \sin(|x| + \pi/6)} \right) dx$ is equal to

- (1) 2π (2) 4π
(3) 8π (4) 6π

Ans. (2)

Sol. $= 2\pi \int_0^{\pi/6} \frac{1}{1 - \sin\left(x + \frac{\pi}{6}\right)} dx$ let $x + \frac{\pi}{6} = t$ $dx = dt$

$$= 2\pi \int_{\pi/6}^{\pi/3} \frac{dt}{1 - \sin t} = 2\pi \int_{\pi/6}^{\pi/3} \frac{1 + \sin t}{\cos^2 t} dt$$

$$= 2\pi \left[\int_{\pi/6}^{\pi/3} \sec^2 t dt + \int_{\pi/6}^{\pi/3} \sec t \tan t dt \right]$$

$$= 2\pi \left[(\tan t)_{\pi/6}^{\pi/3} + (\sec t)_{\pi/6}^{\pi/3} \right]$$

$$= 2\pi \left[\left(\sqrt{3} - \frac{1}{\sqrt{3}} \right) + \left(2 - \frac{2}{\sqrt{3}} \right) \right]$$

$$= 2\pi \left[\sqrt{3} + 2 - \sqrt{3} \right] = 4\pi$$

13. Let the mean and variance of 7 observations 2, 4, 10, x, 12, 14, y, $x > y$, be 8 and 16 respectively. Two numbers are chosen from $\{1, 2, 3, x-4, y, 5\}$ one after another without replacement, then the probability, that the smaller number among the two chosen numbers is less than 4, is:

- (1) $\frac{3}{5}$ (2) $\frac{4}{5}$
(3) $\frac{2}{5}$ (4) $\frac{1}{3}$

Ans. (2)

Sol. Mean $(\bar{x}) = 8$ (Given)

$$\Rightarrow \frac{2 + 4 + 10 + x + 12 + 14 + y}{7} = 8$$

$$\Rightarrow x + y = 14 \dots (1) \dots$$

Variance $(\sigma^2) = 16$ (Given)

$$\Rightarrow 16 = \frac{2^2 + 4^2 + 10^2 + x^2 + 12^2 + 14^2 + y^2}{7} - 8^2$$

$$\Rightarrow x^2 + y^2 = 100 \dots (2) \dots$$

$$\therefore (x + y)^2 = x^2 + y^2 + 2xy$$

$$\Rightarrow xy = 48 \text{ (sum is 14 product is 48)}$$

Since problem states $x > y$

$$\therefore x = 8 \text{ and } y = 6$$

Now set $X = \{1, 2, 3, 4, 6, 5\}$

Now we choose two numbers one after another without replacement total outcomes = $6 \times 5 = 30$

We want the prob. That the smaller number among the two is less than 4

$$P(\text{smaller} < 4) = 1 - P(\text{smaller} \geq 4)$$

$$= 1 - \frac{6}{30} = \frac{4}{5}$$

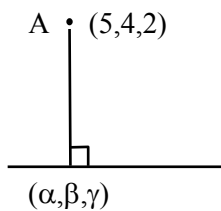
14. Let (α, β, γ) be the co-ordinates of the foot of the perpendicular drawn from the point $(5, 4, 2)$ on the line $\vec{r} = (-\hat{i} + 3\hat{j} + \hat{k}) + \lambda(2\hat{i} + 3\hat{j} - \hat{k})$.

Then the length of the projection of the vector $\alpha\hat{i} + \beta\hat{j} + \gamma\hat{k}$ on the vector $6\hat{i} + 2\hat{j} + 3\hat{k}$ is :

- (1) $\frac{15}{7}$ (2) 4
(3) $\frac{18}{7}$ (4) 3

Ans. (3)

Sol.



$$\vec{r} = (-\hat{i} + 3\hat{j} + \hat{k}) + \lambda(2\hat{i} + 3\hat{j} - \hat{k})$$

$$\frac{x+1}{2} = \frac{y-3}{3} = \frac{z-1}{-1} = \lambda$$

Any general point P on the line is

$$(2\lambda - 1, 3\lambda + 3, -\lambda + 1)$$

Let the given point is A $(5, 4, 2)$

$$\overrightarrow{AP} = (2\lambda - 6)\hat{i} + (3\lambda - 1)\hat{j} + (-\lambda - 1)\hat{k}$$

$$\because \overrightarrow{AP} \perp \text{Line (L)}$$

$$\therefore \overrightarrow{AP} \cdot (2\hat{i} + 3\hat{j} - \hat{k}) = 0$$

$$2(2\lambda - 6) + 3(3\lambda - 1) - 1(-\lambda - 1) = 0$$

$$\Rightarrow \lambda = 1$$

$$\therefore \alpha = 1$$

$$\beta = 6$$

$$\gamma = 0$$

Let the vector $\vec{u} = \alpha\hat{i} + \beta\hat{j} + \gamma\hat{k}$

$$\vec{u} = \hat{i} + 6\hat{j} + 0\hat{k}$$

$$\& \vec{w} = 6\hat{i} + 2\hat{j} + 3\hat{k}$$

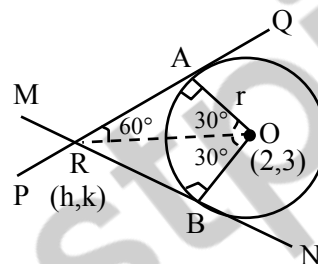
$$\text{So projection} = \frac{|\vec{u} \cdot \vec{w}|}{|\vec{w}|} = \frac{18}{7}$$

15. Let PQ and MN be two straight lines touching the circle $x^2 + y^2 - 4x - 6y - 3 = 0$ at the points A and B respectively. Let O be the centre of the circle and $\angle AOB = \pi/3$. Then the locus of the point of intersection of the lines PQ and MN is:

- (1) $3(x^2 + y^2) - 18x - 12y + 25 = 0$
(2) $x^2 + y^2 - 12x - 18y - 25 = 0$
(3) $x^2 + y^2 - 18x - 12y - 25 = 0$
(4) $3(x^2 + y^2) - 12x - 18y - 25 = 0$

Ans. (4)

Sol. Given circle



$$x^2 + y^2 - 4x - 6y - 3 = 0$$

$$C(2, 3) \& r = 4$$

$$\cos 30^\circ = \frac{r}{OR} = \frac{4}{OR}$$

$$\Rightarrow OR = \frac{8}{\sqrt{3}}$$

Now

$$OR^2 = (h - 2)^2 + (k - 3)^2$$

$$\Rightarrow 3(x^2 + y^2) - 12x - 18y - 25 = 0$$

16. If the coefficient of x in the expansion of $(ax^2 + bx + c)(1 - 2x)^{26}$ is -56 and the coefficients of x^2 and x^3 are both zero, then $a + b + c$ is equal to

- (1) 1300 (2) 1500
(3) 1403 (4) 1483

Ans. (3)

Sol. $(ax^2 + bc + c) \sum_{r=0}^{26} {}^{26}C_r (-2x)^r$

Coeff. of x^2 : $a \cdot {}^{26}C_0 (-2)^0 + b \cdot {}^{26}C_1 (-2) + c \cdot {}^{26}C_2 (-2)^2 = 0$

$\Rightarrow a - 52b + 1300c = 0 \dots (1)$

Coeff. of x^3 : $a \cdot {}^{26}C_1 (-2) + b \cdot {}^{26}C_2 (-2)^2 + c \cdot {}^{26}C_3 (-2)^3 = 0$

$\Rightarrow -52a + 1300b - 20800c = 0 \dots (2)$

Coeff. of $x = -56$

$\Rightarrow b \cdot {}^{26}C_0 (-2)^0 + c \cdot {}^{26}C_1 (-2)^1 = -56$

$b - 52c = -56 \dots (3)$

After solving (1), (2) & (3)

$a = 1300, b = 100, c = 3$

$\Rightarrow a + b + c = 1403$

- 17.** If $x^2 + x + 1 = 0$, then the value of $\left(x + \frac{1}{x}\right)^4 + \left(x^2 + \frac{1}{x^2}\right)^4 + \left(x^3 + \frac{1}{x^3}\right)^4 + \dots + \left(x^{25} + \frac{1}{x^{25}}\right)^4$ is :

(1) 128

(2) 162

(3) 175

(4) 145

Ans. (4)

Sol. $x^2 + x + 1 = 0$

$\Rightarrow x = \omega \text{ or } \omega^2$

$\therefore \alpha = \omega \text{ & } \beta = \omega^2$

$= (\omega + \omega^2)^4 + (\omega^2 + \omega^4)^4 + (\omega^3 + \omega^6)^4 + \dots + (\omega^{25} + \omega^{50})^4$

$= [(\omega + \omega^2)^4 + (\omega^2 + \omega^4)^4 + (\omega^4 + \omega^8)^4 + \dots + (\omega^{25} + \omega^{50})^4] + [(\omega^3 + \omega^6)^4 + (\omega^6 + \omega^{12})^4 + (\omega^9 + \omega^{18})^4 + \dots + (\omega^{24} + \omega^{48})^4]$

$= \underbrace{[1 + 1 + 1 + \dots + 1]}_{17 \text{ times}} + \underbrace{[(1+1)^4 + (1+1)^4 + \dots + (1+1)^4]}_{8 \text{ times}}$

$= 17 + 128$

$= 145$

- 18.** The value of $\operatorname{cosec} 10^\circ - \sqrt{3} \sec 10^\circ$ is equal to:

(1) 4

(2) 2

(3) 8

(4) 6

Ans. (1)

Sol.
$$= \frac{1}{\sin 10^\circ} - \frac{\sqrt{3}}{\cos 10^\circ}$$
$$= \frac{\cos 10^\circ - \sqrt{3} \sin 10^\circ}{\sin 10^\circ \cos 10^\circ}$$
$$= 4 \left[\frac{\frac{1}{2} \cos 10^\circ - \frac{\sqrt{3}}{2} \sin 10^\circ}{2 \sin 10^\circ \cos 10^\circ} \right]$$
$$= 4 \left[\frac{\sin(30^\circ - 10^\circ)}{\sin 20^\circ} \right]$$
$$= 4$$

- 19.** The sum of all the roots of the equation $(x-1)^2 - 5|x-1| + 6 = 0$, is:

(1) 4

(2) 3

(3) 1

(4) 5

Ans. (1)

Sol. Let $|x-1| = t$

$t^2 - 5t + 6 = 0$

$t = 2 \text{ & } t = 3$

$|x-1| = 2 \text{ & } |x-1| = 3$

$x-1 \pm 2 \text{ & } x-1 = \pm 3$

$x = 1 \pm 2 \text{ & } x = 1 \pm 3$

$\therefore \text{root} = 3, -1, 4, -2$

$\therefore \text{Sum of root} = 3 + (-1) + 4 + (-2) = 4.$

- 20.** Let O be the vertex of the parabola $x^2 = 4y$ and Q be any point on it. Let the locus of the point P, which divides the line segment OQ internally in the ratio 2:3 be the conic C. Then the equation of the chord of C, which is bisected at the point (1, 2), is:

(1) $5x - y - 3 = 0$

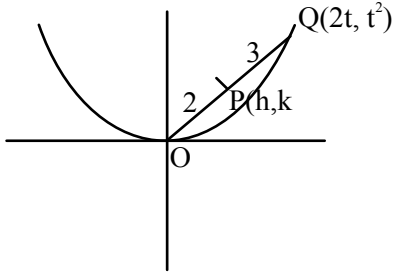
(2) $4x - 5y + 6 = 0$

(4) $x - 2y + 3 = 0$

(4) $5x - 4y + 3 = 0$

Ans. (4)

Sol. $h = \frac{4t}{5}$



$$k = \frac{2t^2}{5} = \frac{2}{5} \left(\frac{5h}{4} \right)^2$$

$$8k = 5h^2$$

$$\Rightarrow 5x^2 = 8y$$

$$T = S_1$$

$$5(xx_1) - 4(y + y_1) = 5x_1^2 - 8y_1$$

$$5(x) - 4(y + 2) = 5 - 8.2$$

$$5x - 4y + 3 = 0$$

SECTION-B

- 21.** Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be a twice differentiable function such that the quadratic equation $f(x)m^2 - 2f'(x)m + f''(x) = 0$ in m , has two equal roots for every $x \in \mathbb{R}$. If $f(0) = 1$, $f'(0) = 2$ and (α, β) is the largest interval in which the function $f(\log_e x - x)$ is increasing, then $\alpha + \beta$ is equal to

Ans. (1)

Sol. Given quadratic equation has equal roots, thus

$$D = 0 \Rightarrow (f'(x))^2 = f''(x) \cdot f(x)$$

$$\frac{f'(x)}{f(x)} = \frac{f''(x)}{f'(x)}$$

Integrate

$$\ln(f(x)) = \ln(f'(x)) + \ln C \Rightarrow f(x) = c \cdot f'(x)$$

Put $x = 0$

$$1 = c \cdot 2 \Rightarrow c = \frac{1}{2}$$

$$\text{Now } 2f(x) = f'(x)$$

$$\Rightarrow \frac{f'(x)}{f(x)} = 2$$

Integrate

$$\ln(f(x)) = 2x + d$$

$$\Rightarrow d = 0$$

$$\Rightarrow \ln(f(x)) = 2x \Rightarrow f(x) = e^{2x}$$

$$\text{Now let } g(x) = f(\ln x - x) = e^{2(\ln x - x)}$$

$$\therefore g'(x) = 2e^{2(\ln x - x)} \left(\frac{1}{x} - 1 \right) \geq 3$$

$$\Rightarrow \frac{1-x}{x} \geq 0$$

$$\Rightarrow x \in (0, 1]$$

$$\Rightarrow \alpha = 0, \beta = 1$$

$$\alpha + \beta = 1.$$

- 22.** Let $a_1 = 1$ and for $n \geq 1$, $a_{n+1} = \frac{1}{2}a_n + \frac{n^2 - 2n - 1}{n^2(n+1)^2}$. Then $\left| \sum_{n=1}^{\infty} \left(a_n - \frac{2}{n^2} \right) \right|$ is equal to _____.

Ans. (2)

Sol. $a_{n+1} - \frac{1}{2}a_n = \frac{n^2 - 2n - 1}{n^2(n+1)^2} = \frac{2n^2 - (n+1)^3}{n^2(n+1)^2}$

$$\Rightarrow a_{n+1} - \frac{1}{2}a_n = \frac{2}{(n+1)^2} - \frac{1}{n^2}$$

$$n=1 \quad a_2 - \frac{1}{2}a_1 = \frac{2}{2^2} - \frac{1}{1^2}$$

$$2 \left[a_3 - \frac{1}{2}a_2 = \frac{2}{3^2} - \frac{1}{2^2} \right]$$

$$2^2 \left[a_4 - \frac{1}{2}a_3 = \frac{2}{4^2} - \frac{1}{3^2} \right]$$

$\vdots$

$$2^{n-2} \left[a_n - \frac{1}{2}a_{n-1} = \frac{2}{n^2} - \frac{1}{(n-1)^2} \right]$$

$$2^{n-1} \left[a_{n+1} - \frac{1}{2}a_n = \frac{2}{(n+1)^2} - \frac{1}{n^2} \right]$$

Adding

$$a_{n+1} = \frac{2}{(n+1)^2} - \frac{1}{2^n} \Rightarrow a_n = \frac{2}{n^2} - \frac{1}{2^{n-1}}$$

$$\Rightarrow \left| \sum_{n=1}^{\infty} \left(a_n - \frac{2}{n^2} \right) \right| = \left| \sum_{n=1}^{\infty} -\frac{1}{2^{n-1}} \right| = 2$$



23. Let $S = \{(m, n) : m, n \in \{1, 2, 3, \dots, 50\}\}$. If the number of elements (m, n) in S such that $6^m + 9^n$ is a multiple of 5 is p and the number of elements (m, n) in S such that $m + n$ is a square of a prime number is q , then $p + q$ is equal to.....

Ans. (1333)

Sol. $S = \{1, 2, 3, \dots, 50\}$

$p = (6^m + 9^n)$ is divisible by 5

No. of ways

$$6^m = (5\lambda + 1)^m = 5k + 1$$

$$9^n = (10 - 1)^n = 10\mu - 1 \text{ if } n \text{ is odd}$$

$\Rightarrow n$ must be odd

$$10\mu + 1 \text{ if } n \text{ is even}$$

$$\Rightarrow \text{No. of ways} = 50 \times 25 = 1250$$

$q \Rightarrow (m + n)$ is square of a prime

	$m + n = 4$	$m + n = 9$	$m + n = 25$	$m + n = 49$
No. of	$\downarrow$	$\downarrow$	$\downarrow$	$\downarrow$
ways	3	8	24	48

$$q = 3 + 8 + 24 + 48 = 83$$

$$= p + q = 1250 + 83 = 1333$$

24. For some $\alpha, \beta \in \mathbb{R}$, let $A = \begin{bmatrix} \alpha & 2 \\ 1 & 2 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 1 \\ 1 & \beta \end{bmatrix}$ be such that $A^2 - 4A + 2I = B^2 - 3B + I = O$. Then $(\det(\text{adj}(A^3 - B^3)))^2$ is equal to

Ans. (225)

Sol. $\text{Tr}(A) = 4 \Rightarrow \alpha + 2 = 4 \Rightarrow \alpha = 2$

$$\text{Tr}(B) = 3 \Rightarrow \beta + 1 = 3 \Rightarrow \beta = 2$$

$$A^2 - 4A + 2I = O$$

$$A^3 = 4A^2 - 2A = 16A - 8I - 2A$$

$$14A - 8I$$

$$= \begin{bmatrix} 28 & 28 \\ 14 & 28 \end{bmatrix} + \begin{bmatrix} -8 & 0 \\ 0 & -8 \end{bmatrix}$$

$$= A^3 = \begin{bmatrix} 20 & 28 \\ 14 & 20 \end{bmatrix}$$

$$B^2 - 3B + I = O$$

$$B^2 = 3B - I$$

$$\Rightarrow B^3 = 3B^2 - B = 3(3B - I) - B = 8B - 3I$$

$$B^3 = \begin{pmatrix} 8 & 8 \\ 8 & 16 \end{pmatrix} + \begin{pmatrix} -3 & 0 \\ 0 & -3 \end{pmatrix} = \begin{pmatrix} 5 & 8 \\ 8 & 13 \end{pmatrix}$$

$$A^3 - B^3 = \begin{pmatrix} 20 & 28 \\ 14 & 20 \end{pmatrix} - \begin{pmatrix} 5 & 8 \\ 8 & 13 \end{pmatrix} = \begin{pmatrix} 15 & 20 \\ 6 & 7 \end{pmatrix}$$

$$\Rightarrow |A^3 - B^3| = 105 - 120 = -15$$

$$\Rightarrow |\text{adj}(A^3 - B^3)| = |A^3 - B^3| = -15$$

$$\Rightarrow |\text{adj}(A^3 - B^3)|^2 = 225$$

25. $6 \int_0^\pi (\sin 3x + \sin 2x + \sin x) dx$ is equal to.....

Ans. (17)

Sol. $6 \int_0^\pi |2 \sin 2x \cos x + \sin 2x| dx$

$$6 \int_0^\pi |4 \sin x \cos^2 x + 2 \sin x \cos x| dx$$

$$I = 12 \int_0^\pi \sin x |2 \cos^2 x + \cos x| dx$$

Put $\cos x = t$, $-\sin x dx = dt$

$$I = -12 \int_1^{-1} |2t^2 + t| dt$$

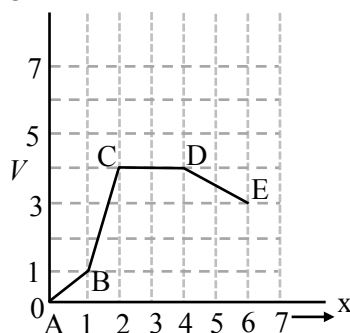
$$I =$$

$$12 \left(\int_{-1}^{-1/2} (2t^2 + t) dt + \int_{-1/2}^0 -(2t^2 + t) dt + \int_0^1 (2t^2 + t) dt \right)$$

$$I = 17$$

(HELD ON WEDNESDAY 21st JANUARY 2026)
TIME : 9:00 AM TO 12:00 NOON
PHYSICS
TEST PAPER WITH SOLUTION
SECTION-A

26. Potential energy (V) versus distance (x) is given by the graph, Rank various regions as per the magnitudes of the force (F) acting on a particle from high to low.



- (1) $F_{BC} > F_{CD} > F_{DE} > F_{AB}$
 (2) $F_{CD} > F_{AB} > F_{BC} > F_{DE}$
 (3) $F_{CD} > F_{DE} > F_{AB} > F_{BC}$
 (4) $F_{BC} > F_{AB} > F_{DE} > F_{CD}$

Ans. (4)

Sol. Slope of potential energy v/s position curve gives negative of force.

$$\therefore F_{BC} > F_{AB} > F_{DE} > F_{CD}$$

Correct option (4)

27. A gas based geyser heats water flowing at the rate of 5.0 litres per minute from 27°C to 87°C.

The rate of consumption of the gas is ____ g/s.

(Take heat of combustion of gas = 5.0×10^4 J/g)
 specific heat capacity of water = 4200 J/kg. °C

- (1) 2.1 (2) 4.2
 (3) 0.42 (4) 0.21

Ans. (3)

Sol. Water flow rate = 5 ℓ/min = $\frac{5}{60}$ kg/s

$$\therefore \text{Power of heater} = \frac{dm}{dt} S \Delta T = \frac{1}{12} \times 4200 \times 60 W$$

$\therefore$ Let rate of consumption of gas be x g/s.

$$\therefore x \times 5.0 \times 10^4 = \frac{1}{12} \times 4200 \times 60$$

$$\Rightarrow x = 4200 \times 10^{-4} = 0.42 \text{ g/s}$$

Correct option (3)

28. A conducting circular loop of area 1.0 m^2 is placed perpendicular to a magnetic field which varies as $B = \sin(100 t)$ Tesla. If the resistance of the loop is 100Ω , then the average thermal energy dissipated in the loop in one period is ____ J.

- (1) $\frac{\pi}{2}$ (2) 2π
 (3) π (4) π^2

Ans. (3)

Sol. Area of the loop = 1 m^2

$$B = \sin(100 t)$$

$$\therefore \phi = BA = \sin(100t)$$

$$\therefore \frac{d\phi}{dt} = 100 \cos(100t)$$

$$\therefore P = \frac{V^2}{R} = \frac{10^4 \cos^2(100t)}{100}$$

$\therefore$ Thermal energy dissipated in 1 time period

$$= \int_0^T P dt = \int_0^T 100 \cos^2(100t) dt$$

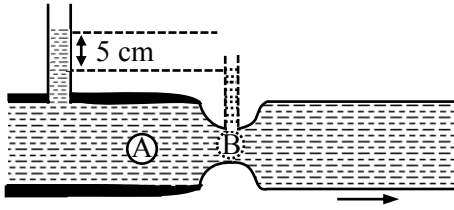
$$T = \frac{2\pi}{100} = \frac{\pi}{50} \text{ sec}$$

$$\begin{aligned} \therefore Q &= 100 \int_0^{\pi/50} \cos^2(100t) dt \\ &= 100 \int_0^{\pi/50} \frac{1 + \cos 200t}{2} dt \\ &= 100 \left[\frac{\pi}{100} \right] = \pi \end{aligned}$$

Correct option (3)

29. Water flows through a horizontal tube as shown in the figure. The difference in height between the water columns in vertical tubes is 5 cm and the area of cross-sections at A and B are 6 cm^2 and 3 cm^2 respectively.

The rate of flow will be ____ cm^3/s . (take $g = 10 \text{ m/s}^2$)



- (1) $\frac{200}{\sqrt{3}}$ (2) $200\sqrt{6}$
 (3) $200\sqrt{3}$ (4) $100\sqrt{3}$

Ans. (3)

Sol. From continuity equation

$$A_A V_A = A_B V_B \Rightarrow 6V_A = 3V_B \Rightarrow V_B = 2V_A$$

Applying Bernoulli's equation between A & B,

$$P_A + \frac{1}{2}\rho V_A^2 = P_B + \frac{1}{2}\rho V_B^2$$

$$\Rightarrow \rho g \times 0.05 = \frac{1}{2}\rho [V_B^2 - V_A^2] = \frac{1}{2}\rho (3V_A^2)$$

$$\Rightarrow V_A = \sqrt{\frac{2g \times 0.05}{3}} \text{ m/s} = \frac{1}{\sqrt{3}} \text{ m/s} = \frac{100}{\sqrt{3}} \text{ cm/s}$$

$$\Rightarrow \text{Volume flow rate} = A_A V_A = \frac{6 \times 100}{\sqrt{3}} \text{ cm}^3/\text{sec} \\ = 200\sqrt{3} \text{ cm}^3/\text{sec}$$

Correct option (3)

- 30.** In an experiment the values of two spring constants were measured as $k_1 = (10 \pm 0.2) \text{ N/m}$ and $k_2 = (20 \pm 0.3) \text{ N/m}$. If these springs are connected in parallel, then the percentage error in equivalent spring constant is :

- (1) 2.67% (2) 2.33%
 (3) 1.33% (4) 1.67%

Ans. (4)

Sol. For parallel combination of spring,

$$K_{eq} = K_1 + K_2 = 30 \text{ N/m}$$

$$\Delta K_{eq} = \Delta K_1 + \Delta K_2 = 0.2 + 0.3 = 0.5 \text{ N/m}$$

$$\therefore \% \text{Error in } K = \frac{0.5}{30} \times 100 = 1.67\%$$

Correct option (4)

- 31.** A 4 kg mass moves under the influence of a force $\vec{F} = (4t^3\hat{i} - 3t\hat{j}) \text{ N}$ where t is the time in second. If mass starts from origin at $t = 0$, the velocity and position after $t = 2\text{s}$ will be :

$$(1) \vec{v} = 3\hat{i} + \frac{3}{2}\hat{j} \quad \vec{r} = \frac{6}{5}\hat{i} + \hat{j}$$

$$(2) \vec{v} = 4\hat{i} - \frac{3}{2}\hat{j} \quad \vec{r} = \frac{8}{5}\hat{i} - \hat{j}$$

$$(3) \vec{v} = 4\hat{i} + \frac{5}{2}\hat{j} \quad \vec{r} = \frac{8}{5}\hat{i} + 2\hat{j}$$

$$(4) \vec{v} = 4\hat{i} - \frac{3}{2}\hat{j} \quad \vec{r} = \frac{6}{5}\hat{i} - \hat{j}$$

Ans. (2)

Sol. $\vec{F} = 4t^3\hat{i} - 3t\hat{j}$

$$\vec{a} = \frac{\vec{F}}{m} = t^3\hat{i} - \frac{3}{4}t\hat{j}$$

$$a_x = t^3$$

$$\frac{dv_x}{dt} = t^3$$

$$\int_{v_x=0}^{v_{x2}} dv_x = \int_{t=0}^{t=2} t^3 dt$$

$$v_{x2} - 0 = \left[\frac{t^4}{4} \right]_0^2$$

$$v_{x2} = 4$$

$$a_y = -\frac{3}{4}t$$

$$\frac{dv_y}{dt} = -\frac{3}{4}$$

$$\int_0^{v_{y2}} dv_y = \int_0^2 -\frac{3}{4}t dt$$

$$v_{y2} = -\frac{3}{4} \left[\frac{t^2}{2} \right]_0^2$$

$$v_{y2} = -\frac{3}{2}$$

$$\vec{v}_2 = 4\hat{i} - \frac{3}{2}\hat{j}$$

$$v_x = \frac{t^4}{4}$$

$$\int_0^{x_2} dx = \int_0^2 \frac{t^4}{4} dt$$

$$x_2 - 0 = \left[\frac{t^5}{20} \right]_0^2$$

$$x_2 = \frac{8}{5}$$

$$v_y = -\frac{3}{8}t^2$$

$$\int_0^{y_2} dy = -\frac{3}{8} \int_0^2 t^2 dt$$

$$y_2 - 0 = -\frac{3}{8} \left[\frac{t^3}{3} \right]_0^2$$

$$y_2 = -1$$

$$\vec{r} = \frac{8}{5}\hat{i} - \hat{j}$$

Correct option (2)

32. Consider a modified Bernoulli equation.

$$\left(P + \frac{A}{Bt^2}\right) + \rho g(h + Bt) + \frac{1}{2}\rho V^2 = \text{constant}$$

If t has the dimension of time then the dimensions of A and B are _____, _____ respectively.

- (1) $[ML^0T^{-1}]$ and $[M^0LT]$
 (2) $[ML^0T^{-1}]$ and $[M^0LT^{-1}]$
 (3) $[ML^0T^{-2}]$ and $[M^0LT^{-2}]$
 (4) $[ML^0T^{-2}]$ and $[M^0LT^{-1}]$

Ans. (2)

Sol. $\Rightarrow [P] = \left[\frac{A}{Bt^2}\right] \dots\dots(1)$

$\Rightarrow [h] = [Bt] \dots\dots(2)$

$\Rightarrow [B] = \left[\frac{h}{t}\right] = \left[\frac{L}{T}\right] = [LT^{-1}]$

Putting B in equation (1)

$$[ML^{-1}T^{-2}] = \left[\frac{A}{LT^{-1} \times T^2}\right]$$

$$[A] = [ML^0T^{-1}]$$

Correct option (2)

33. A current carrying is placed vertically and a particle of mass m with charge Q is released from rest. The particle moves along the axis of solenoid. If g is acceleration due to gravity then the acceleration (a) of the charged particle will satisfy :

- (1) $a = g$ (2) $a > g$
 (3) $a = 0$ (4) $0 < a < g$

Ans. (1)

Sol. Since the solenoid is placed vertically, the magnetic field inside the solenoid will be either along $-y$ or $+y$ axis.

$\Rightarrow$ Particle will gain velocity along $-y$ axis.

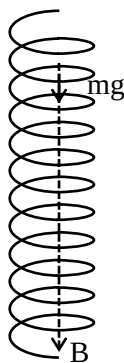
$$\Rightarrow \vec{F}_B = q(\vec{v} \times \vec{B})$$

$$\Rightarrow \vec{F}_B = 0$$

$$\Rightarrow \vec{F}_{\text{net}} = m\vec{g}$$

$$\Rightarrow a_{\text{net}} = g$$

Correct option (1)

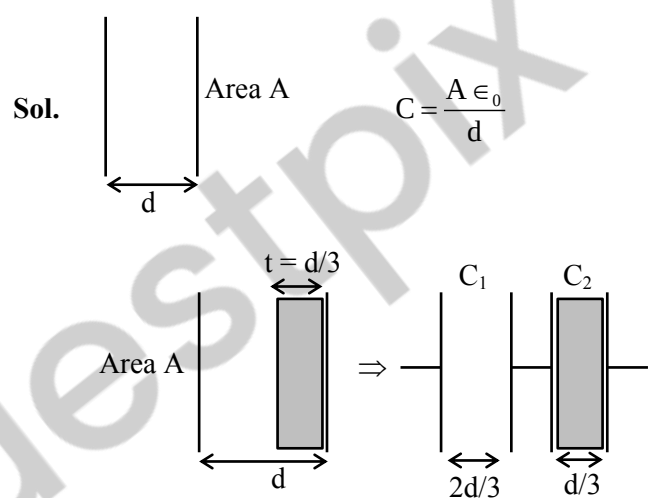


34. A parallel plate capacitor has capacitance C , when there is vacuum within the parallel plates.

A sheet having thickness $\left(\frac{1}{3}\right)^{\text{rd}}$ of the separation between the plates and relative permittivity K is introduced between the plates. The new capacitance of the system is :

- (1) $\frac{3KC}{2K+1}$ (2) $\frac{CK}{2+K}$
 (3) $\frac{3CK^2}{(2K+1)^2}$ (4) $\frac{4KC}{3K-1}$

Ans. (1)



$$C_1 = \frac{3A\epsilon_0}{2d}$$

$$C_2 = \frac{3A\epsilon_0 \times K}{d}$$

$$C_1 = \frac{3}{2}C$$

$$C_2 = 3KC$$

$$C_{\text{eq}} = \frac{C_1 C_2}{C_1 + C_2} = \frac{\frac{3}{2}C \times 3KC}{\frac{3}{2}C + 3KC}$$

$$C_{\text{eq}} = \frac{\frac{9}{2}KC^2}{\frac{3}{2}C(2K+1)} = \frac{3KC}{2K+1}$$

Correct option (1)

35. The electric field a plane electromagnetic wave is given by :

$$E_y = 69 \sin[0.6 \times 10^3 x - 1.8 \times 10^{11} t] \text{ V/m.}$$

The expression for magnetic field associated with this electromagnetic wave is _____ T.

- (1) $B_z = 2.3 \times 10^{-7} \sin[0.6 \times 10^3 x - 1.8 \times 10^{11} t]$
 (2) $B_z = 2.3 \times 10^{-7} \sin[0.6 \times 10^3 x + 1.8 \times 10^{11} t]$
 (3) $B_y = 69 \sin[0.6 \times 10^3 x + 1.8 \times 10^{11} t]$
 (4) $B_y = 2.3 \times 10^{-7} \sin[0.6 \times 10^3 x - 1.8 \times 10^{11} t]$

Ans. (1)

Sol. $\hat{B} = \hat{c} \times \hat{E}$

$\Rightarrow \hat{c} = \hat{i}$ because phase of electric field is function of x.

$\Rightarrow \hat{E} = \hat{j}$ (given)

$\Rightarrow \hat{B} = \hat{i} \times \hat{j} = \hat{k}$

$$|B| = \frac{|E|}{c} = \frac{69 \times 0.6 \times 10^3}{1.8 \times 10^{11}} = \frac{69}{3 \times 10^8}$$

$$|B| = 2.9 \times 10^{-7}$$

$$\vec{B}_2 = 2.9 \times 10^{-7} \sin(0.6 \times 10^3 x - 1.8 \times 10^{11} t)$$

(phase is same as that of electric field)

Correct option (1)

36. In a double slit experiment the distance between the slits is 0.1 cm and the screen is placed at 50 cm from the slits plane. When one slit is covered with a transparent sheet having thickness t and refractive index $n (= 1.5)$, the central fringe shifts by 0.2 cm. The value of t is _____ cm.

- (1) 8×10^{-4} (2) 6.0×10^{-3}
 (3) 5.6×10^{-4} (4) 5.0×10^{-3}

Ans. (1)

Sol. $d \sin \theta = (\mu - 1)t$

$$d \left[\frac{x}{D} \right] = (\mu - 1)t$$

$$t = \frac{xd}{D(\mu - 1)}$$

$$= \frac{(0.2)(0.1)}{50(1.5 - 1)}$$

$$t = 8 \times 10^{-4} \text{ cm}$$

Correct option (1)

37. A light wave described by $E = 60 \sin(3 \times 10^{15} t + \sin(12 \times 10^{15} t))$ (in SI units) falls on a metal surface of work function 2.8 eV. The maximum kinetic energy of ejected photoelectron is (approximately) _____ eV. ($h = 6.6 \times 10^{-34} \text{ J-s.}$ and $e = 1.6 \times 10^{-19} \text{ C}$)

- (1) 5.1 (2) 3.8
 (3) 6.0 (4) 7.8

Ans. (1)

Sol. $\omega_1 = 3 \times 10^{15} \text{ rad/sec}$

$$\omega_2 = 12 \times 10^{15} \text{ rad/sec}$$

$$\therefore v = \frac{\omega}{2\pi}$$

$$E_{\text{photon}} = hv = 6.6 \times 10^{-34} \times 1.91 \times 10^{15} \\ = 1.26 \times 10^{-18} \text{ J}$$

$$E_{\text{max}} = \frac{1.26 \times 10^{-18}}{1.6 \times 10^{-19}} \approx 7.9 \text{ eV}$$

$$K_{\text{max}} = E_{\text{max}} - \phi_0 \\ = 7.9 - 2.8$$

$$K_{\text{max}} = 5.1 \text{ eV}$$

Correct option (1)

38. If an alpha particle with energy 7.7 MeV is bombarded on a thin gold foil, the closest distance from nucleus it can reach is _____ m.

$$(\text{Atomic number of gold} = 79 \text{ and } \frac{1}{4\pi\epsilon_0} = 9 \times 10^9$$

in SI units)

- (1) 2.95×10^{-14} (2) 2.95×10^{-16}
 (3) 3.85×10^{-16} (4) 3.85×10^{-14}

Ans. (1)

Sol. Energy conservation

$$K_i + U_i = K_f + U_f$$

$$7.7 \times 10^6 \times 1.6 \times 10^{-19} + 0$$

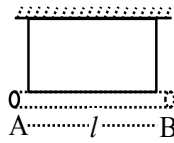
$$= 0 + \frac{9 \times 10^9 (1.6 \times 10^{-19}) (79 \times 1.6 \times 10^{-19})}{r}$$

$$r = 2.95 \times 10^{-14}$$

Correct option (1).



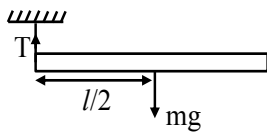
39. A uniform rod of mass m and length l suspended by means of two identical inextensible light strings as shown in figure. Tension in one string immediately after the other string is cut, is _____. (g acceleration due to gravity)



- (1) $mg/2$ (2) $mg/4$
(3) $mg/3$ (4) mg

Ans. (2)

Sol.



$$mg \frac{l}{2} = \frac{ml^2}{3} \alpha$$

$$\alpha = \frac{3g}{2l} \dots (1)$$

$$mg - T = ma_c$$

$$T = mg - ma_c$$

$$= mg - m \left(\frac{l}{2} \alpha \right)$$

$$= mg - m \left(\frac{l}{2} \cdot \frac{3g}{2l} \right)$$

$$T = \frac{mg}{4}$$

Correct option (2)

40. An aluminium and steel rods having same lengths and cross-sections are joined to make total length of 120 cm at 30°C . The coefficient of linear expansion of aluminium and steel are $24 \times 10^{-6}/^\circ\text{C}$ and $1.2 \times 10^{-5}/^\circ\text{C}$, respectively. The length of this composite rod when its temperature is raised to 100°C , is _____ cm.

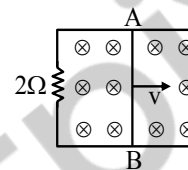
- (1) 120.20 (2) 120.15
(3) 120.03 (4) 120.06

Ans. (2)

Sol. $\ell_{\text{final}} = \ell_0(1 + \alpha_A \Delta T) + \ell_0(1 + \alpha_B \Delta T)$
 $= \ell_0 [2 + (\alpha_A + \alpha_B) \Delta T]$
 $= 60 [2 + (36 \times 10^{-6} + 1.2 \times 10^{-5}) \times 70]$
 $= 60 [2 + 0.0025]$
 $= 120.15 \text{ cm}$

Correct option (2)

41. A 1 m long metal rod AB completes the circuit as shown in figure. The area of circuit is perpendicular to the magnetic field of 0.10 T. If the resistance of the total circuit is 2Ω then the force needed to move the rod towards right with constant speed (v) of 1.5 m/s is _____ N.



- (1) 7.5×10^{-2} (2) 5.7×10^{-3}
(3) 5.7×10^{-2} (4) 7.5×10^{-3}

Ans. (4)

Sol. To maintain constant speed

$$F_{\text{ext}} = F_B$$

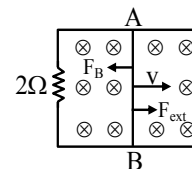
$$\Rightarrow F_{\text{ext}} = i l B$$

$$= \left(\frac{v B l}{R} \right) l B$$

$$= \frac{B^2 l^2 v}{R}$$

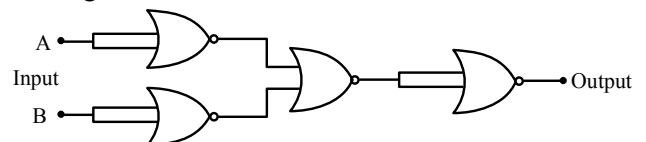
$$= \frac{(0.1)^2 \times (1)^2 \times 1.5}{2}$$

$$= 7.5 \times 10^{-3} \text{ N}$$



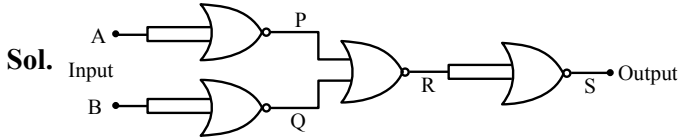
Correct option (4)

42. The given circuit works as :



- (1) AND gate (2) NOR gate
(3) NAND gate (4) OR gate

Ans. (3)



$$P = \bar{A}$$

$$Q = \bar{B}$$

$$R = \overline{\bar{A} + \bar{B}} = \overline{\bar{A}\bar{B}} = AB$$

$$S = \overline{AB} \Rightarrow \text{NAND Gate}$$

Correct option (3)

- 43.** Two strings (A, B) having linear densities $\mu_A = 2 \times 10^{-4} \text{ kg/m}$ and $\mu_B = 4 \times 10^{-4} \text{ kg/m}$ and lengths $L_A = 2.5 \text{ m}$ and $L_B = 1.5 \text{ m}$ respectively are joined. Free ends of A and B are tied to two rigid supports C and D, respectively creating a tension of 500 N in the wire. Two identical pulses, sent from C and D ends, take time t_1 and t_2 , respectively, to reach the joint. The ratio t_1/t_2 is :

- (1) 1.08 (2) 1.90
(3) 1.67 (4) 1.18

Ans. (4)

Sol. Given $L_A = 2.5 \text{ m}$,
 $L_B = 1.5 \text{ m}$,
 $T = 500 \text{ N}$

$$v_A = \sqrt{\frac{T}{\mu_A}} = \sqrt{\frac{500}{2 \times 10^{-4}}} = 5\sqrt{10} \times 10^2 \text{ m/s}$$

$$v_B = \sqrt{\frac{T}{\mu_B}} = \sqrt{\frac{500}{4 \times 10^{-4}}} = 5\sqrt{5} \times 10^2 \text{ m/s}$$

$$t_1 = \frac{L_A}{v_A} = \frac{2.5}{5\sqrt{10}} \times 10^{-2} \text{ s}$$

$$t_2 = \frac{L_B}{v_B} = \frac{1.5}{5\sqrt{5}} \times 10^{-2} \text{ s}$$

$$\therefore \frac{t_1}{t_2} = \frac{2.5}{5\sqrt{10}} \times \frac{5\sqrt{5}}{1.5} = \frac{5}{3} \times \frac{1}{\sqrt{2}} = \frac{1.66}{1.41} = 1.18$$

Correct Option (4)

- 44.** Initially a satellite of 100 kg is in a circular orbit of radius $1.5R_E$. This satellite can be moved to a circular orbit of radius $3R_E$ by supplying $\alpha \times 10^6 \text{ J}$ of energy. The value of α is _____.

(Take Radius of Earth $R_E = 6 \times 10^6 \text{ m}$ and $g = 10 \text{ m/s}^2$)

- (1) 150 (2) 500
(3) 100 (4) 1000

Ans. (4)

Sol. Energy of a satellite in a circular orbit is given as

$$E = \frac{-GM_E m}{2r}; r = \text{radius of circular orbit}$$

Required energy to be supplied = $\Delta E = E_f - E_i$

$$\Delta E = \left(\frac{-GM_E m}{2(3R_E)} \right) - \left(\frac{-GM_E m}{2(1.5R_E)} \right)$$

$$= \frac{GM_E m}{6R_E}$$

$$\text{Now, } g = \frac{GM_E}{R_E^2} \Rightarrow \frac{GM_E}{R_E} = gR_E$$

$$\therefore \Delta E = \frac{1}{6} g m R_E$$

$$= \frac{1}{6} \times 10 \times 100 \times 6 \times 10^6$$

$$= 1000 \times 10^6$$

$$\alpha = 1000$$

Correct option (4)

- 45.** A point charge of 10^{-8} C is placed at origin. The work done in moving a point charge $2 \mu\text{C}$ from point A(4, 4, 2) m to B(2, 2, 1) m is _____ J.

$$\left(\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ in SI units} \right)$$

- (1) 45×10^{-6}
(2) 0
(3) 30×10^{-6}
(4) 15×10^{-6}

Ans. (3)

Sol. Work done by external agent :

$$W_{\text{ext}} = \Delta U;$$

$\Delta U \rightarrow$ Change in potential energy in taking the charge from initial to final configuration

$$\Rightarrow W_{\text{ext}} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r_f} - \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r_i}$$

Now, $r_f = \sqrt{(2-0)^2 + (2-0)^2 + (1-0)^2} = 3 \text{ m}$

$r_i = \sqrt{(4-0)^2 + (4-0)^2 + (2-0)^2} = 6 \text{ m}$

$\therefore W_{\text{ext}} = (9 \times 10^9) \times (10^{-8} \times 2 \times 10^{-6}) \left[\frac{1}{3} - \frac{1}{6} \right]$

$= 3 \times 10^{-5}$

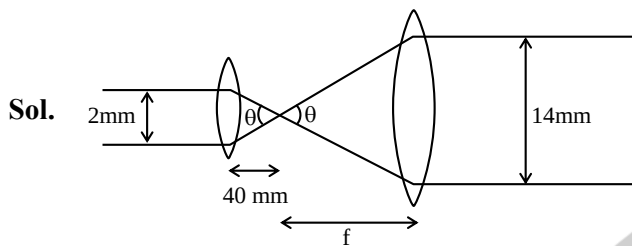
$= 30 \times 10^{-6} \text{ J}$

Correct Option (3)

SECTION - B

46. A collimated beam of light of diameter 2 mm is propagating along x-axis. The beam is required to be expanded in a collimated beam of diameter 14 mm using a system of two convex lenses. If first lens has focal length 40 mm, then the focal length of second lens is _____ mm.

Ans. (280)

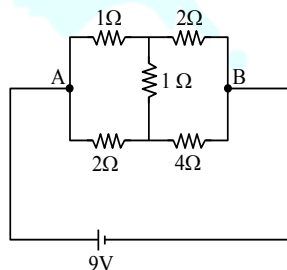


$\frac{40}{2} = \frac{f}{14}$

$\Rightarrow f = 280 \text{ mm}$

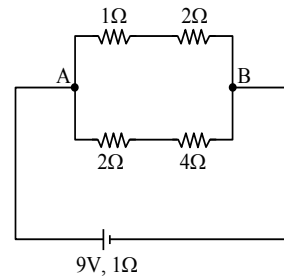
Correct Answer : 280

47. The heat generated in 1 minute between points A and B in the given circuit, when a battery of 9V with internal resistance of 1Ω is connected across these points is _____ J.

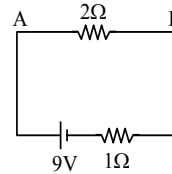


Ans. (1080)

Sol.



Balanced
Wheatstone
bridge



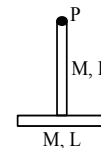
$i = \frac{9}{3} = 3 \text{ A}$

$\therefore H_{AB} = i^2 R_{AB} t$

$= (3)^2 \times 2 \times 60 = 1080 \text{ J}$

Correct Answer : 1080

48. Two identical thin rods of mass M kg and length L m are connected as shown in figure. Moment of inertia of the combined rod system about an axis passing through point P and perpendicular to the plane of the rods is $\frac{x}{2} ML^2 \text{ kg m}^2$. The value of x is _____.



Ans. (17)

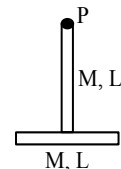
Sol. $I = \frac{ML^2}{3} + \left(\frac{ML^2}{12} + ML^2 \right)$

$= \frac{4ML^2 + ML^2 + 12ML^2}{12}$

$I = \frac{17}{12} ML^2$

$\therefore x = 17$

Correct Answer : 17





49. 10 mole of oxygen is heated at constant volume from 30°C to 40°C . The change in the internal energy of the gas is _____ cal. (The molecular specific heat of oxygen at constant pressure, $C_p = 7 \text{ cal./mol } ^{\circ}\text{C}$ and $R = 2 \text{ cal./mol } ^{\circ}\text{C}$.)

Ans. (500)

Sol. $\Delta U = nC_v\Delta T$
 $= n(C_p - R)\Delta T$
 $= 10(7 - 2)(40 - 30)$
 $\Delta U = 500$

Correct Answer : 500

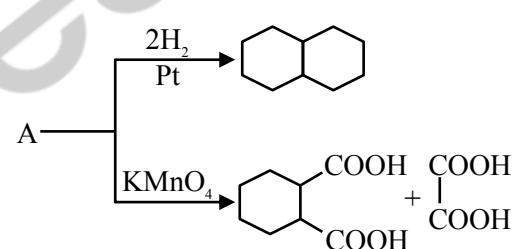
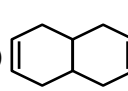
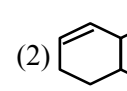
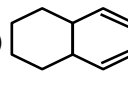
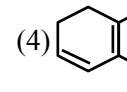
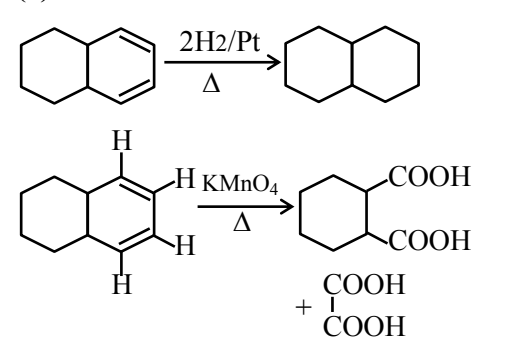
50. In a microscope the objective is having focal length $f_o = 2 \text{ cm}$ and eye-piece is having focal length $f_e = 4 \text{ cm}$. The tube length is 32 cm . The magnification produced by this microscope for normal adjustment is _____.

Ans. (100)

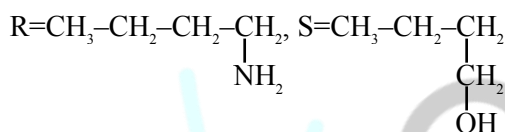
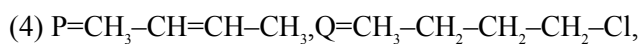
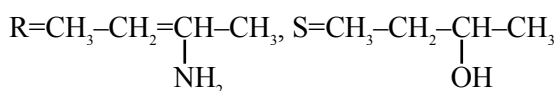
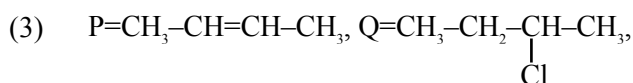
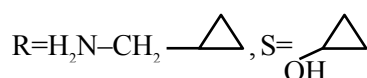
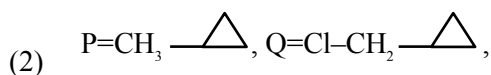
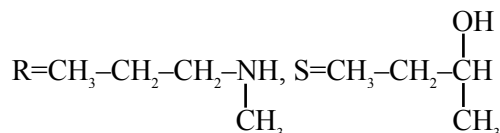
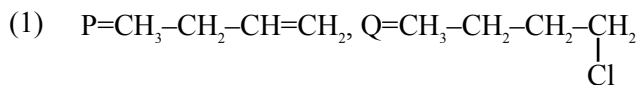
Sol. $m \approx \frac{LD}{f_o f_e}$
 $= \frac{32}{2} \times \frac{25}{4}$
 $m = 100$

Correct Answer : 100

(HELD ON WEDNESDAY 21st JANUARY 2026)
TIME : 9:00 AM TO 12:00 NOON

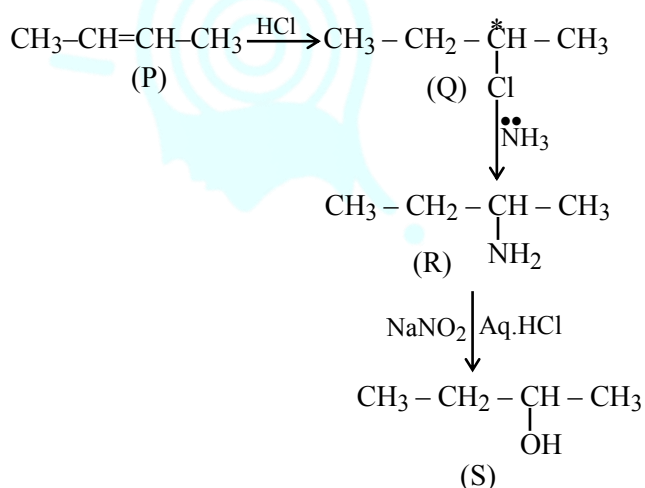
CHEMISTRY	TEST PAPER WITH SOLUTION
SECTION-A 51. Consider the following reactions. $\text{PbCl}_2 + \text{K}_2\text{CrO}_4 \rightarrow \text{A} + 2\text{KCl}$ (Hot solution) $\text{A} + \text{NaOH} \rightleftharpoons \text{B} + \text{Na}_2\text{CrO}_4$ $\text{PbSO}_4 + 4\text{CH}_3\text{COONH}_4 \rightarrow (\text{NH}_4)_2\text{SO}_4 + \text{X}$ In the above reactions, A, B and X are respectively. (1) $\text{Na}_2[\text{Pb}(\text{OH})_2]$, PbCrO_4 and $(\text{NH}_4)_2[\text{Pb}(\text{CH}_3\text{COO})_4]$ (2) PbCrO_4, $\text{Na}_2[\text{Pb}(\text{OH})_4]$ and $[\text{Pb}(\text{NH}_3)_4]\text{SO}_4$ (3) $\text{Na}_2[\text{Pb}(\text{OH})_2]$, PbCrO_4 and $[\text{Pb}(\text{NH}_3)_4]\text{SO}_4$ (4) PbCrO_4, $\text{Na}_2[\text{Pb}(\text{OH})_4]$ and $(\text{NH}_4)_2[\text{Pb}(\text{CH}_3\text{COO})_4]$ Ans. (4) Sol. $\text{PbCl}_2 + \text{K}_2\text{CrO}_4 \rightarrow \text{PbCrO}_4 + 2\text{KCl}$ (Hot solution) (A) $\text{PbCrO}_4 + 4\text{NaOH (excess)} \rightarrow \text{Na}_2[\text{Pb}(\text{OH})_4] + \text{Na}_2\text{CrO}_4$ (B) $\text{PbSO}_4 + 4\text{CH}_3\text{COONH}_4 \rightarrow (\text{NH}_4)_2[\text{Pb}(\text{CH}_3\text{COO})_4] + (\text{NH}_4)_2\text{SO}_4$ (X) 52. Which of the following represents the correct trend for the mentioned property ? A. $\text{F} > \text{P} > \text{S} > \text{B}$ – First Ionization Energy B. $\text{Cl} > \text{F} > \text{S} > \text{P}$ – Electron Affinity C. $\text{K} > \text{Al} > \text{Mg} > \text{B}$ – Metallic character D. $\text{K}_2\text{O} > \text{Na}_2\text{O} > \text{MgO} > \text{Al}_2\text{O}_3$ – Basic character Choose the correct answer from the option given below. (1) A, B and D only (2) A, B, C and D (3) A and B only (4) B and C only Ans. (1)	Sol. $\Rightarrow$ On moving left to right in a period IE increases and from top to bottom in a group IE decreases. $\text{F} > \text{P} > \text{S} > \text{B}$ (IE order) $\Rightarrow$ On moving left to right in a period metallic and basic character decreases. $\text{K} > \text{Mg} > \text{Al} > \text{B}$ (Metallic character order) $\Rightarrow$ On moving top to bottom in a group metallic and basic character increases. $\text{K}_2\text{O} > \text{Na}_2\text{O} > \text{MgO} > \text{Al}_2\text{O}_3$ $\Rightarrow \text{EA} : \text{Group 17} > \text{Group 16} > \text{Group 15}$ $\text{Cl} > \text{F} > \text{S} > \text{P}$ 53. Identify A in the following reaction.  (1)  (2)  (3)  (4)  Ans. (3) Sol. 

54. A hydrocarbon 'P' (C_4H_8) on reaction with HCl gives an optically active compound 'Q' (C_4H_9Cl) which on reaction with one mole of ammonia gives compound 'R' ($C_4H_{11}N$). 'R' on diazotization followed by hydrolysis gives 'S'. Identify P, Q, R and S.



Ans. (3)

Sol.



55. Given below are two statements :

Statement I : The number of pairs among $[SiO_2, CO_2]$, $[SnO, SnO_2]$, $[PbO, PbO_2]$ and $[GeO, GeO_2]$, which contain oxides that are both amphoteric is 2.

Statement II : BF_3 is an electron deficient molecule can act as a lewis acid, forms adduct with NH_3 and has a trigonal planar geometry.

In the light of the above statement, choose the correct answer from the option given below.

- (1) Both **Statement I** and **Statement II** are true.
 (2) Both **Statement I** and **Statement II** are false.
 (3) **Statement I** is true but **Statement II** is false.
 (4) **Statement I** is false **Statement II** is true.

Ans. (1)

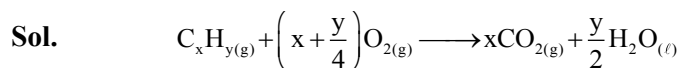
Sol. $\Rightarrow SiO_2, CO_2, GeO, GeO_2$ are acidic in nature.
 SnO, SnO_2, PbO, PbO_2 are amphoteric in nature.

$\Rightarrow BF_3$ is lewis acid according to lewis octet theory and has sp^2 hybridization with trigonal planar geometry and it can accept lone pair form ammonia to form adduct.

56. 80 mL of a hydrocarbon on mixing with 264 mL of oxygen in a closed U-tube undergoes complete combustion. The residual gases after cooling to 273 K occupy 224 mL. When the system is treated with KOH solution, the volume decreases to 64 mL. The formula of the hydrocarbon is :

- (1) C_2H_4 (2) C_4H_{10} (3) C_2H_2 (4) C_2H_6

Ans. (3)



$$t=0 \quad 80 \quad 264 \quad 0 \quad -$$

$$t=t_{\text{final}} \quad - \quad 264 - 80\left(x + \frac{y}{4}\right) \quad 80x \quad -$$

$$264 - 80\left(x + \frac{y}{4}\right) + 80x = 224$$

$$264 - \frac{80y}{4} = 224$$

$$40 = \frac{80y}{4} \Rightarrow y = 2$$

$$264 - 80\left(x + \frac{y}{4}\right) = 64$$

$$264 - 80\left(x + \frac{1}{2}\right) = 64$$

$$264 - 80x - 40 = 64$$

$$x = 2$$

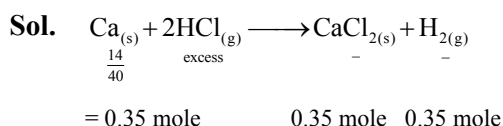
57. 14.0 g of calcium metal is allowed to react with excess HCl at 1.0 atm pressure and 273 K.

Which of the following statements is **incorrect** ?

[Given : Molar mass in g mol^{-1} of Ca-40, Cl-35.5, H-1]

- (1) 0.35 mol of H_2 gas is evolved.
- (2) 7.84 L of H_2 gas is evolved.
- (3) 33.3 of CaCl_2 is produced.
- (4) The limiting reagent is calcium metal.

Ans. (3)



Volume of $\text{H}_{2(g)}$ evolved = $0.35 \times 22.4 = 7.84 \text{ L}$

(3) is wrong because weight of $\text{CaCl}_2 = .35 \times 111 = 38.85 \text{ gm}$

58. In Carius method, 0.75 g of an organic compound gave 1.2 g of barium sulphate, find percentage of sulphur (molar mass 32 g mol^{-1}). Molar mass of barium sulphate is 233 g mol^{-1} .

- (1) 4.55%
- (2) 10.30%
- (3) 21.97%
- (4) 16.48%

Ans. (3)

Sol.
$$\frac{n_{\text{BaSO}_4} \times 32}{W_{(\text{unknown comp.})}} \times 100$$

$$= \frac{1.2 \times 32}{233} \times \frac{100}{0.75} = 21.97\%$$

59. Elements P and Q form two types of non-volatile, non-ionizable compounds PQ and PQ_2 . When 1 g of PQ is dissolved in 50 g of solvent 'A'. ΔT_b was 1.176 K while when 1 g of PQ_2 is dissolved in 50 g of solvent 'A', ΔT_b was 0.689 K. (K_b of 'A' = 5 K kg mol^{-1}). The molar masses of elements P and Q (in g mol^{-1}) respectively, are :

- (1) 70, 110
- (2) 65, 145
- (3) 60, 25
- (4) 25, 60

Ans. (4)

Sol. $(\Delta T_b)_{\text{PQ}} = K_b m$

$$1.176 = 5 \times \frac{1}{M_1} \times \frac{1000}{50}$$

$$M_1 = 85.03$$

$$(\Delta T_b)_{\text{PQ}_2} = 5 \times \frac{1}{M_2} \times \frac{1000}{50} = 0.689$$

$$M_2 = 145.13$$

Let molar mass of P & Q are M_p and M_q respectively

$$M_p + M_q = 85.03$$

$$M_p + 2M_q = 145.13$$

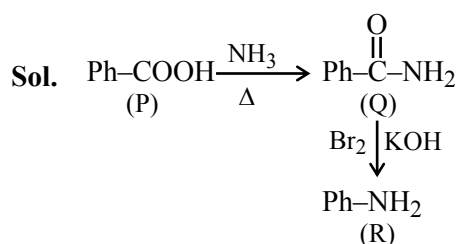
$$M_p = 24.93 \approx 25$$

$$M_q = 60.1 \approx 60$$

60. An organic compound (P) on treatment with aqueous ammonia under hot condition forms compound (Q) which on heating with Br_2 and KOH forms compound (R) having molecular formula $\text{C}_9\text{H}_7\text{N}$. Names of P, Q and R respectively are.

- (1) Benzoic acid, benzamide, aniline
- (2) Toluic acid, methylbenzamide, 2-methylaniline
- (3) Benzoic acid, 4-methylbenzamide, 4-methylaniline.
- (4) Phenylethanoic acid, phenylethanamide, benzamine

Ans. (1)

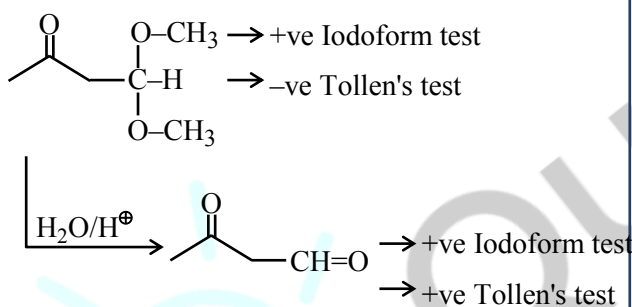


61. An organic compound "P" of molecular formula $C_6H_{12}O_3$ gives positive Iodoform test but negative Tollen's test. When "P" is treated with dilute acid, it produces "Q". "Q" gives positive Tollen's test and also iodoform test. The structure of "P" is :

- (1) $CH_3 - \overset{\overset{O}{\parallel}}{C} - \underset{\underset{OCH_3}{|}}{CH} - CH_2 - \underset{\underset{OCH_3}{|}}{CH_2}$
- (2) $CH_3 - \overset{\overset{O}{\parallel}}{C} - CH_2 - \underset{\underset{OCH_3}{|}}{CH} - OCH_3$
- (3) $H - \overset{\overset{O}{\parallel}}{C} - CH_2 - CH_2 - \underset{\underset{OCH_3}{|}}{CH} - OCH_3$
- (4) $CH_3 - \overset{\overset{O}{\parallel}}{C} - \underset{\underset{OCH_3}{|}}{C} - \underset{\underset{OCH_3}{|}}{CH_3}$

Ans. (2)

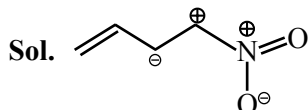
Sol.



62. From the following, the least stable structure is :

- (1) $CH_2=CH-CH=N^+-O^-$ (2) $CH_2=CH-CH=N^+=O$
- (3) $CH_2=CH-CH^+-N^+=O$ (4) $CH_2=CH-CH=N^+=O$

Ans. (3)

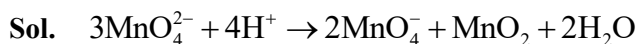


This resonating structure having +ve charge on adjacent atoms so it is least stable.

63. MnO_4^{2-} , in acidic medium, disproportionates to :

- (1) Mn_2O_7 and MnO_2
 (2) MnO_4^- and MnO
 (3) MnO_4^- and MnO_2
 (4) Mn_2O_7 and MnO

Ans. (3)



64. Given below are two statements:

Statement I: The number of species among SF_4 , NH_4^+ , $[NiCl_4]^-$, XeF_4 , $[PtCl_4]^{2-}$, SeF_4 and $[Ni(CN)_4]^{2-}$, that have tetrahedral geometry is 3.

Statement II: In the set $[NO_2]$, BeH_2 , BF_3 , $AlCl_3$, all the molecules have incomplete octet around central atom. In the light of the above statements, choose the correct answer from the options given below:

- (1) **Statement I** is true but **Statement II** is false
 (2) Both **Statement I** and **Statement II** are false
 (3) **Statement I** is false but **Statement II** is true
 (4) Both **Statement I** and **Statement II** are true

Ans. (3)

Sol. Statement-I

SF_4 (See-saw)

XeF_4 (square planar),

$[PtCl_4]^{2-}$ (square planar),

$[NiCl_4]^{2-}$ (Tetrahedral),

$[Ni(CN)_4]^{2-}$ (square planar),

SeF_4 (See-saw)

NH_4^+ (Tetrahedral)

Statement-II

NO_2 (seven electrons on N)

BeH_2 (four electrons on Be)

BF_3 (six electrons on B)

$AlCl_3$ (six electrons on Al)

65. Given below are two statements:

Statement I: Among $[\text{Cu}(\text{NH}_3)_4]^{2+}$, $[\text{Ni}(\text{en})_3]^{2+}$, $[\text{Ni}(\text{NH}_3)_6]^{2+}$ and $[\text{Mn}(\text{H}_2\text{O})_6]^{2+}$, $[\text{Mn}(\text{H}_2\text{O})_6]^{2+}$ has the maximum number of unpaired electrons.

Statement II: The number of pairs among $\{[\text{NiCl}_4]^{2-}, [\text{Ni}(\text{CO})_4]\}$, $\{[\text{NiCl}_4]^{2-}, [\text{Ni}(\text{CN})_4]^{2-}\}$ and $\{[\text{Ni}(\text{CO})_4], [\text{Ni}(\text{CN})_4]^{2-}\}$ that contain only diamagnetic species is two.

In the light of the above statements, choose the **correct** answer from the options given below:

- (1) **Statement I** is false but **Statement II** is true
- (2) Both **Statement I** and **Statement II** are true
- (3) Both **Statement I** and **Statement II** are false
- (4) **Statement I** is true but **Statement II** is false

Ans. (4)

Sol. $[\text{Cu}(\text{NH}_3)_4]^{2+} \Rightarrow d^9, \text{dsp}^2$ one unpaired electron
 $[\text{Ni}(\text{en})_3]^{2+} \Rightarrow d^8, \text{sp}^3\text{d}^2$ two unpaired electrons
 $[\text{Ni}(\text{NH}_3)_6]^{2+} \Rightarrow d^8, \text{sp}^3\text{d}^2$ two unpaired electrons
 $[\text{Mn}(\text{H}_2\text{O})_6]^{2+} \Rightarrow d^5, \text{sp}^3\text{d}^2$ five unpaired electrons
 $[\text{Ni}(\text{CO})_4]$ (diamagnetic)
 $[\text{NiCl}_4]^{2-}$ (paramagnetic)
 $[\text{Ni}(\text{CN})_4]^{2-}$ (diamagnetic)

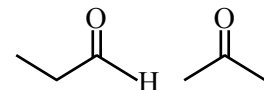
66. Identify correct statement from the following :

- A. Propanal and propanone are functional isomers.
- B. Ethoxyethane and methoxypropane are metamers.
- C. But-2-ene shows optical isomerism.
- D. But-1-ene and but-2-ene are functional isomers.
- E. Pentane and 2, 2-dimethyl propane are chain isomers.

Choose the **correct** answer from the options given below :

- (1) B, C and D only
- (2) A, B and C only
- (3) A, B and E only
- (4) C, D and E only

Ans. (3)

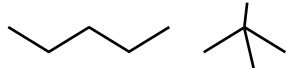
Sol.  are Functional isomer

$\text{CH}_3\text{-CH=CH-CH}_3$ & $\text{CH}_3\text{-CH}_2\text{-CH=CH}_2$

Are Positional isomer

$\text{CH}_3\text{-CH}_2\text{-O-CH}_2\text{-CH}_3$ & $\text{CH}_3\text{-CH}_2\text{-CH}_2\text{-O-CH}_3$
are Metamer

$\text{CH}_3\text{-CH=CH-CH}_3$ does not have optical isomer

 Chain isomer

67. Identify the correct statements.

- A. Arginine and Tryptophan are essential amino acids.
- B. Histidine does not contain heterocyclic ring in its structure.
- C. Proline is a six membered cyclic ring amino acid.
- D. Glycine does not have chiral centre.
- E. Cysteine has characteristic feature of side chain as $\text{MeS-CH}_2\text{-CH}_2\text{-}$.

Choose the **correct** answer from the options given below:

Option

- (1) C and E Only
- (2) B and E Only
- (3) C and D Only
- (4) A and D Only

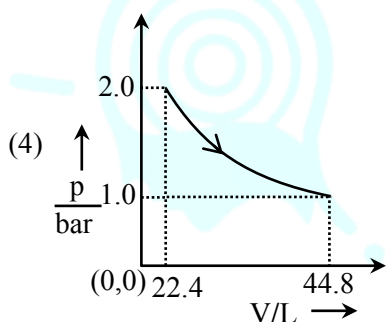
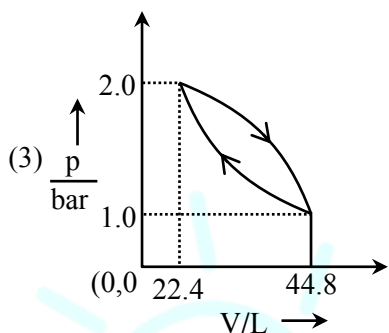
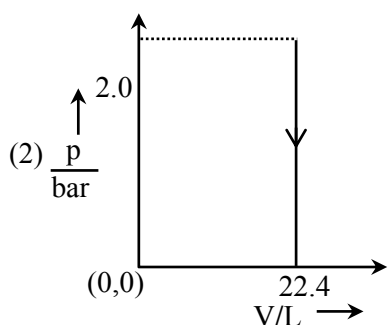
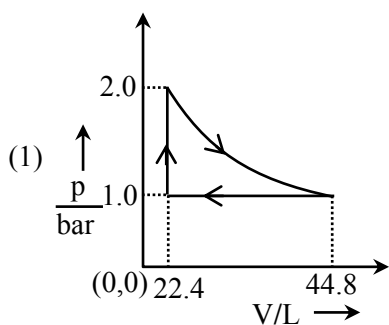
Ans. (4)

Sol. • Histidine does contain heterocyclic ring.

• Proline is a five membered cyclic ring amino acid.

• Cysteine has characteristic feature of side chain as $\text{CH}_2\text{-SMe}$

68. Which of the following graphs between pressure 'P' versus volume 'V' represent the maximum work done ?



Ans. (4)

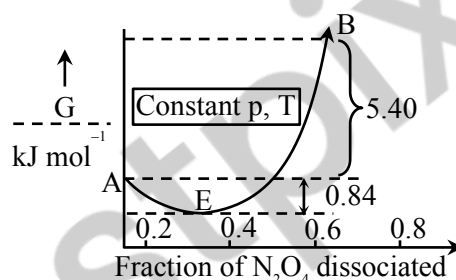
Sol. Area under the P v/s V curve, is equal to magnitude of work.

In option (2) work done is zero while in remaining options net work done is negative due to expansion.

NTA has given the answer without considering the negative sign that is considered only magnitude.

69. For the reaction, $\text{N}_2\text{O}_4 \rightleftharpoons 2\text{NO}_2$, graph is plotted as shown below. Identify correct statements.

- A. Standard free energy change for the reaction is $-5.40 \text{ kJ mol}^{-1}$.
 B. As $\Delta G^\ominus$ in graph is positive, N_2O_4 will not dissociate into NO_2 at all.
 C. Reverse reaction will go to completion.
 D. When 1 mole of N_2O_4 changes into equilibrium mixture, value of $\Delta G^\ominus = -0.84 \text{ kJ mol}^{-1}$
 E. When 2 mole of NO_2 , changes into equilibrium mixture, $\Delta G^\ominus$ for equilibrium mixture is $-6.24 \text{ kJ mol}^{-1}$.
 E. When 2 mole of NO_2 , changes into equilibrium mixture, $\Delta G^\ominus$ for equilibrium mixture is $-6.24 \text{ kJ mol}^{-1}$.

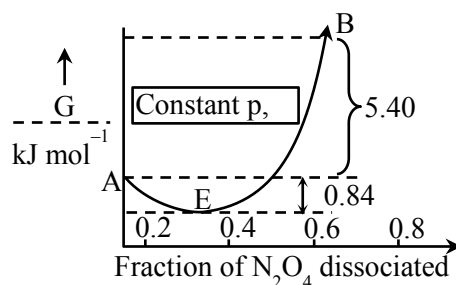


Choose the **correct** answer from the options given below :

- (1) D and E only (2) C and E only
 (3) A and D only (4) B and C only

Ans. (1)

Sol.



- (A) $\Delta_r G^\ominus = G_B^\ominus - G_A^\ominus = +ve$
 (B) $\Delta_r G^\ominus = +ve$, N_2O_4 will partially dissociates into NO_2 .
 (C) For reverse reaction
 It is partially completed as there is equilibrium at E.
 (D) For 1 mole N_2O_4 ; $\Delta_r G^\ominus = -0.84 \text{ kJ mol}^{-1}$
 (E) For 2 mole NO_2 ; $\Delta_r G^\ominus = -5.4 - 0.84$
 $= -6.24 \text{ kJ mol}^{-1}$

70. Given below are two statements:

Statement I: When an electric discharge is passed through gaseous hydrogen, the hydrogen molecules dissociate and the energetically excited hydrogen atoms produce electromagnetic radiation of discrete frequencies.

Statement II: The frequency of second line of Balmer series obtained from He^+ is equal to that of first line of Lyman series obtained from hydrogen atom.

In the light of the above statements, choose the correct answer from the options given below:

- (1) Both **Statement I** and **Statement II** are true
- (2) Both **Statement I** and **Statement II** are false
- (3) **Statement I** is false but **Statement II** is true
- (4) **Statement I** is true but **Statement II** is false

Ans. (1)

Sol. $\frac{1}{\lambda} = RZ^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$

For 1st line of Lyman series in H-atom

$$\frac{1}{\lambda} = R(1)^2 \left(\frac{1}{1^2} - \frac{1}{2^2} \right)$$

$$\frac{1}{\lambda} = \frac{3R}{4}$$

for 2nd line of Balmer series of He^+

$$\frac{1}{\lambda'} = R(2)^2 \left(\frac{1}{2^2} - \frac{1}{4^2} \right)$$

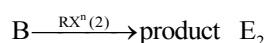
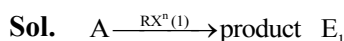
$$\frac{1}{\lambda'} = \frac{3R}{4}$$

As λ and λ' is equal so frequency of these lines will be also equal.

SECTION-B

71. Pre-exponential factors of two different reactions of same order are identical. Let activation energy of first reaction exceeds the activation energy of second reaction by 20 kJ mol^{-1} . If k_1 and k_2 are the rate constants of first and second reaction respectively at 300 K, then $\ln \frac{k_2}{k_1}$ will be
(nearest integer) [$R = 8.3 \text{ J K}^{-1} \text{ mol}^{-1}$]

Ans. (8)



Assuming 'A' same for both reaction.

$$\ln k_1 = \ln A - \frac{E_1}{300R}$$

$$\ln k_2 = \ln A - \frac{E_2}{300R}$$

$$\ln \left(\frac{k_2}{k_1} \right) = \frac{E_1 - E_2}{300R} = \frac{20 \times 1000}{300R}$$

$$= 8.032$$

72. The pH and conductance of a weak acid (HX) was found to be 5 and $4 \times 10^{-5} \text{ S}$, respectively. The conductance was measured under standard condition using a cell where the electrode plates having a surface area of 1 cm^2 were at a distance of 15 cm apart. The value of the limiting molar conductivity is $\text{S m}^2 \text{ mol}^{-1}$. (nearest integer)
(Given: degree of dissociation of the weak acid (α) $\ll 1$)

Ans. (6)

Sol. $\text{pH} = 5$

$$[\text{H}^+] = 10^{-5} = [\text{HX}] \cdot \alpha$$

$$= [\text{HX}] \cdot \frac{\Lambda_m}{\Lambda_m^\infty}$$

$$\Lambda_m = \frac{k \times 1000}{[\text{HX}]}$$

$$K = G \cdot G^* = 4 \times 10^{-5} \times \frac{15}{1} = 6 \times 10^{-4} \text{ S.cm}^{-1}$$

$$[\text{H}^+] = 10^{-5} = [\text{HX}] \times \frac{6 \times 10^{-4} \times 1000}{\Lambda_m^\infty \times [\text{HX}]}$$

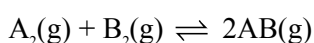
$$\Lambda_m^\infty = 60000 \text{ S.cm}^2 \text{ mol}^{-1}$$

$$\Lambda_m^\infty = 6 \text{ S.m}^2 \text{ mol}^{-1}$$

73. Use the following data :

Substance	$\Delta_f H^\ominus(500K)$ kJ mol^{-1}	$S^\ominus(500K)$ $\text{JK}^{-1} \text{mol}^{-1}$
AB(g)	32	222
A ₂ (g)	6	146
B ₂ (g)	X	280

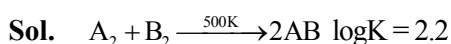
One mole each of A₂(g) and B₂(g) are taken in a 1L closed flask and allowed to establish the equilibrium at 500K.



The value of x (in kJ mol^{-1}) is (Nearest integer)

(Given: $\log K=2.2$ $R=8.3 \text{ JK}^{-1} \text{mol}^{-1}$)

Ans. (70)



$$\Delta H^\ominus = (2 \times 32) - (6 + x) = (58 - x) \text{ kJ}$$

$$\Delta S^\ominus = (2 \times 222) - (146 + 280) = 18 \text{ Joule}$$

$$\Delta G^\ominus = -RT \ln K$$

$$\Delta G^\ominus = -\frac{8.314 \times 500 \times 2.2 \times 2.303}{1000}$$

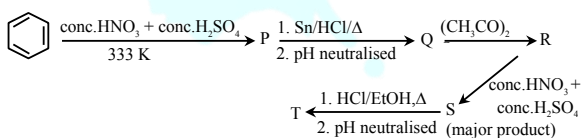
$$\Delta G^\ominus = -21.06$$

$$\Delta H^\ominus - T\Delta S^\ominus = -21.06$$

$$58 - x - 500 \left(\frac{18}{1000} \right) = -21.06$$

$$x = 70.06 \text{ KJ/mol}$$

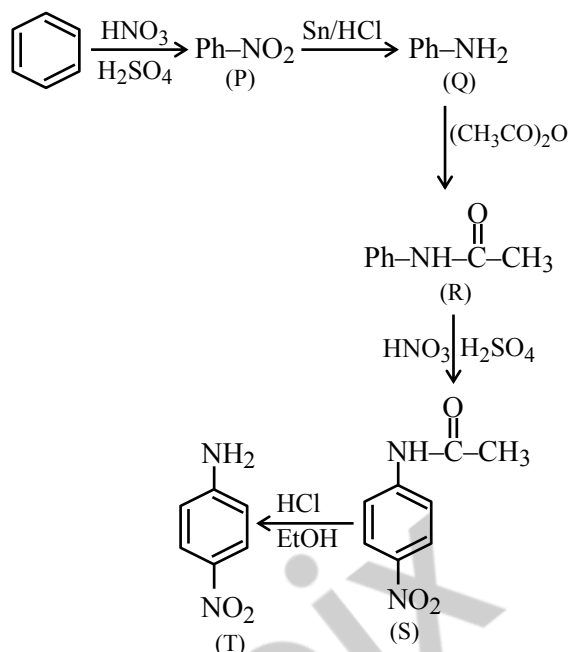
74. Consider the following reaction sequence



The percentage of nitrogen in product 'T' formed is _____. (Nearest integer)

(Given molar mass in g mol^{-1} H:1, C:12, N:14, O:16)

Ans. (20)

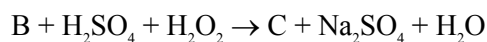
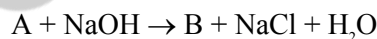
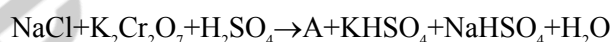


Sol.

$$\text{Mol. wt} = 6 \times 12 + (6 \times 1) + (2 \times 14) + (2 \times 16) = 138$$

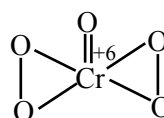
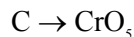
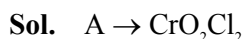
$$\%N = \frac{28}{138} \times 100 = 20.29\%$$

75. Consider the following reactions:



In the product 'C', 'X' is the number of O_2^{2-} units, 'Y' is the total number oxygen atoms present and 'Z' is the oxidation state of Cr. The value of $X + Y + Z$ is _____.

Ans. (13)



$$X = 2, Y = 5 \text{ and } Z = 6$$