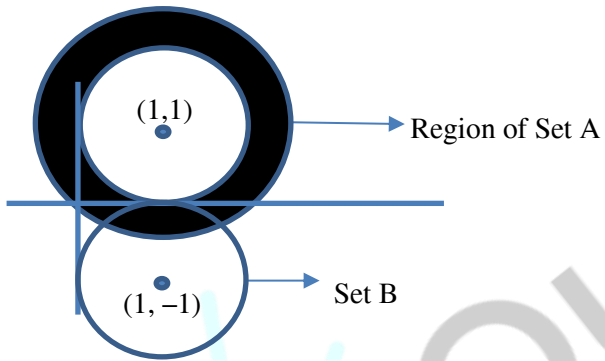


(Held On Friday 24th June, 2022)

TIME : 9 : 00 AM to 12 : 00 PM

MATHEMATICS	TEST PAPER WITH SOLUTION
SECTION-A 1. Let $A = \{z \in \mathbb{C} : 1 \leq z - (1 + i) \leq 2\}$ and $B = \{z \in A : z - (1 - i) = 1\}$. Then, B : (A) is an empty set (B) contains exactly two elements (C) contains exactly three elements (D) is an infinite set Official Ans. by NTA (D) QuestPix Ans. (D) Sol. $A = \{z \in \mathbb{C} : 1 \leq z - (1 + i) \leq 2\}$  $B = \{z \in A : z - (1 - i) = 1\}$. $A \cap B$ has infinite set. 2. The remainder when 3^{2022} is divided by 5 is (A) 1 (B) 2 (C) 3 (D) 4 Official Ans. by NTA (D) QuestPix Ans. (D) Sol. $3^{2022} = 9^{1011} = (10 - 1)^{1011} = 10m - 1 = 10m - 5 + 4$ $= 5(2m - 1) + 4$ (m is integer) Remainder = 4 3. The surface area of a balloon of spherical shape being inflated, increases at a constant rate. If initially, the radius of balloon is 3 units and after 5 seconds, it becomes 7 units, then its radius after 9 seconds is : (A) 9 (B) 10 (C) 11 (D) 12	Official Ans. by NTA (A) QuestPix Ans. (A) Sol. Let r be the radius of spherical balloon S = Surface area $S = 4\pi r^2$ $\frac{dS}{dt} = 8\pi r \times \frac{dr}{dt} = k \text{ (constant)}$ $4\pi r^2 = kt + C \text{ (C is constant of integration)}$ For $t = 0$, $r = 3 \Rightarrow 36\pi = C$ For $t = 5$, $r = 7 \Rightarrow K = 32\pi$ $4\pi r^2 = 32\pi t + 36\pi$ $r^2 = 8t + 9$ for $t = 9$ $r^2 = 81$ $r = 9$ 4. Bag A contains 2 white, 1 black and 3 red balls and bag B contains 3 black, 2 red and n white balls. One bag is chosen at random and 2 balls drawn from it at random, are found to be 1 red and 1 black. If the probability that both balls come from Bag A is $\frac{6}{11}$, then n is equal to ____. (A) 13 (B) 6 (C) 4 (D) 3 Official Ans. by NTA (C) QuestPix Ans. (C) Sol. E_1 = denotes selection for 1st bag E_2 = denotes selection for 2nd bag $P(E_1) = \frac{1}{2}, P(E_2) = \frac{1}{2}$ A = selected balls are 1 red & 1 black $P\left(\frac{A}{E_1}\right) = \frac{{}^3C_1 \times {}^1C_1}{{}^6C_2} = \frac{1}{5}$

$$P\left(\frac{A}{E_1}\right) = \frac{{}^3C_1 \times {}^2C_1}{(n+5)_{C_2}} = \frac{12}{(n+5)(n+4)}$$

$$P\left(\frac{E_1}{A}\right) = \frac{P(E_1) \times P\left(\frac{A}{E_1}\right)}{P(E_1) \times P\left(\frac{A}{E_1}\right) + P(E_2) \times P\left(\frac{A}{E_2}\right)}$$

$$= \frac{\frac{1}{10}}{\frac{1}{10} + \frac{6}{(n+5)(n+4)}} = \frac{6}{11}$$

$$\Rightarrow n = 4$$

5. Let $x^2 + y^2 + Ax + By + C = 0$ be a circle passing through $(0, 6)$ and touching the parabola $y = x^2$ at $(2, 4)$. Then $A + C$ is equal to _____.

- (A) 16 (B) 88/5
(C) 72 (D) -8

Official Ans. by NTA (A)

QuestPix Ans. (A)

Sol. $x^2 + y^2 + Ax + By + C = 0$ is passing through $(0, 6)$

$$\Rightarrow 6B + C = -36$$

The tangent of the parabola $y = x^2$ at $(2, 4)$ is

$$4x - y - 4 = 0 \quad \text{---(1)}$$

The tangent of circle $x^2 + y^2 + Ax + By + C = 0$ at $(2, 4)$ is

$$(4 + A)x + (8 + B)y + 2A + 4B + 2C = 0 \quad \text{---(2)}$$

From Equation (1) and (2)

$$\frac{4 + A}{4} = \frac{8 + B}{-1} = \frac{2A + 4B + 2C}{-4}$$

$$A + 4B = -36 \quad \text{---(3)}$$

$$3A + 4B + 2C = -4 \quad \text{---(4)}$$

From equation (3) and (4)

$$A + C = 16$$

6. The number of values of α for which the system of equations :

$$x + y + z = \alpha$$

$$\alpha x + 2\alpha y + 3z = -1$$

$$x + 3\alpha y + 5z = 4$$

is inconsistent, is

- (A) 0 (B) 1

- (C) 2 (D) 3

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. $x + y + z = \alpha$

$$\alpha x + 2\alpha y + 3z = -1$$

$$x + 3\alpha y + 5z = 4$$

Has inconsistent solution

$$D = \begin{vmatrix} 1 & 1 & 1 \\ \alpha & 2\alpha & 3 \\ 1 & 3\alpha & 5 \end{vmatrix} = 0$$

$$\Rightarrow (\alpha - 1)^2 = 0$$

$$\alpha = 1$$

For $\alpha = 1$

$$D_1 = \begin{vmatrix} 1 & 1 & 1 \\ -1 & 2 & 3 \\ 4 & 3 & 5 \end{vmatrix}$$

$$= (10 - 9) - (-5 - 12) + (-3 - 8)$$

$$= 1 + 17 - 11 \neq 0$$

For $\alpha = 1$ the system of equation has Inconsistent solution

7. If the sum of the squares of the reciprocals of the roots α and β of the equation $3x^2 + \lambda x - 1 = 0$ is 15, then $6(\alpha^3 + \beta^3)^2$ is equal to :

- (A) 18 (B) 24
(C) 36 (D) 96

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. Here α, β roots of equation $3x^2 + \lambda x - 1 = 0$

$$\alpha + \beta = \frac{-\lambda}{3}, \quad \alpha\beta = \frac{-1}{3}$$

$$\frac{1}{\alpha^2} + \frac{1}{\beta^2} = \frac{(\alpha + \beta)^2 - 2\alpha\beta}{\alpha^2\beta^2} = 15$$

$$\lambda^2 = 9$$

$$\text{Now } 6(\alpha^3 + \beta^3)^2 = 6\left((\alpha + \beta)\left((\alpha + \beta)^2 - 3\alpha\beta\right)\right)^2$$

$$= 6\left(\frac{\lambda^2}{9}\right)\left\{\frac{\lambda^2}{9} + 1\right\}^2 = 24$$

8. The set of all values of k for which $(\tan^{-1} x)^3 + (\cot^{-1} x)^3 = k\pi^3, x \in \mathbb{R}$, is the interval :

(A) $\left[\frac{1}{32}, \frac{7}{8}\right]$ (B) $\left(\frac{1}{24}, \frac{13}{16}\right)$
 (C) $\left[\frac{1}{48}, \frac{13}{16}\right]$ (D) $\left[\frac{1}{32}, \frac{9}{8}\right]$

Official Ans. by NTA (A)

QuestPix Ans. (A)

Let $S = (\tan^{-1} x)^3 + (\cot^{-1} x)^3$
 $= (\tan^{-1} x + \cot^{-1} x) - 3 \tan^{-1} x \cdot \cot^{-1} x (\tan^{-1} x + \cot^{-1} x)$
 $= \frac{\pi^3}{8} - \frac{3\pi}{2} \tan^{-1} x \left(\frac{\pi}{2} - \tan^{-1} x \right)$
 $= \frac{3\pi}{2} \left(\tan^{-1} x - \frac{\pi}{4} \right)^2 + \frac{\pi^3}{32}$
 $\Rightarrow \frac{\pi^3}{32} \leq S < \frac{7}{8} \pi^3$
 $= \frac{\pi^3}{32} \leq K\pi^3 < \frac{7}{8} \pi^3$
 $\frac{1}{32} \leq K < \frac{7}{8}$

9. Let $S = \{\sqrt{n} : 1 \leq n \leq 50 \text{ and } n \text{ is odd}\}$

Let $a \in S$ and $A = \begin{vmatrix} 1 & 0 & a \\ -1 & 1 & 0 \\ -a & 0 & 1 \end{vmatrix}$

If $\sum_{a \in S} \det(\text{adj} A) = 100\lambda$, then λ is equal to

(A) 218 (B) 221
 (C) 663 (D) 1717

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. $S = \{\sqrt{n} : 1 \leq n \leq 50 \text{ and } n \text{ is odd}\}$
 $= \{\sqrt{1}, \sqrt{3}, \sqrt{5}, \dots, \sqrt{49}\}$, 25 terms
 $|A| = 1 + a^2$
 $\sum_{a \in S} \det(\text{adj} A) = \sum_{a \in S} |A|^2 = \sum_{a \in S} (1 + a^2)^2$

$$= 22100 = 100\lambda$$

$$\lambda = 221$$

10. $f(x) = 4 \log_e(x-1) - 2x^2 + 4x + 5, x > 1$, which one of the following is NOT correct ?

(A) f is increasing in $(1, 2)$ and decreasing in $(2, \infty)$
 (B) $f(x) = -1$ has exactly two solutions
 (C) $f'(e) - f''(2) < 0$
 (D) $f(x) = 0$ has a root in the interval $(e, e+1)$

Official Ans. by NTA (C)

QuestPix Ans. (C)

Sol. $f(x) = 4 \log_e(x-1) - 2x^2 + 4x + 5, x > 1$

$$f'(x) = \frac{4}{x-1} - 4(x-1)$$

$$\text{For } 1 < x < 2 \Rightarrow f'(x) > 0$$

$$\text{For } x > 2 \Rightarrow f'(x) < 0 \text{ (option 1 is correct)}$$

$$f(x) = -1 \text{ has two solution (option 2 is correct)}$$

$$f(e) > 0$$

$$f(e+1) < 0$$

$$f(e) \cdot f(e+1) < 0 \text{ (option 4 is correct)}$$

$$f'(e) - f''(2) = \frac{4}{e-1} - 4(e-1) + 8 > 0$$

$$\text{(option C is incorrect)}$$

11. the tangent at the point (x_1, y_1) on the curve $y = x^3 + 3x^2 + 5$ passes through the origin, then (x_1, y_1) does NOT lie on the curve :

(A) $x^2 + \frac{y^2}{81} = 2$ (B) $\frac{y^2}{9} - x^2 = 8$
 (C) $y = 4x^2 + 5$ (D) $\frac{x}{3} - y^2 = 2$

Official Ans. by NTA (D)

QuestPix Ans. (D)

Sol. The tangent at (x_1, y_1) to the curve

$$y = x^3 + 3x^2 + 5$$

$$y - y_1 = (3x_1^2 + 6x_1)(x - x_1) \text{ passing through origin}$$

$$-y_1 = (3x_1^3 + 6x_1)(-x_1)$$

$$y_1 = (3x_1^3 + 6x_1^2) \text{ -----(1)}$$

And (x_1, y_1) lies on the curve

$$y = x^3 + 3x^2 + 5$$

$$y_1 = x_1^3 + 3x_1^2 + 5 \text{ ----(2)}$$

From equation (1) and (2)

$$2y_1 = 3x_1^2 + \frac{15}{2}$$

Hence the equation of curve $y = \frac{3}{2}x^2 + \frac{15}{2}$

This curve does not intersect $\frac{x}{3} - y^2 = 2$

12. The sum of absolute maximum and absolute minimum values of the function

$f(x) = |2x^2 + 3x - 2| + \sin x \cos x$ in the interval $[0, 1]$ is :

(A) $3 + \frac{\sin(1) \cos^2(\frac{1}{2})}{2}$ (B) $3 + \frac{1}{2} (1 + 2\cos(1)) \sin(1)$

(C) $5 + \frac{1}{2} (\sin(1) + \sin(2))$ (D) $2 + \sin\left(\frac{1}{2}\right) \cos\left(\frac{1}{2}\right)$

Official Ans. by NTA (B)

QuestPix Ans. (B)

$$f(x) = |2x^2 + 3x - 2| + \sin x \cos x$$

$$f(x) = |(2x - 1)(x + 2)| + \sin x \cos x$$

$$f'(x) = \begin{cases} 4x + 3 + \frac{\cos 2x}{4}, & \frac{1}{2} < x < 1 \\ -(4x + 3) + \frac{\cos 2x}{4}, & 0 \leq x < \frac{1}{2} \end{cases}$$

For $0 \leq x < \frac{1}{2} \Rightarrow f'(x) < 0$

For $\frac{1}{2} < x \leq 1 \Rightarrow f'(x) > 0$

$f(x)$ local minima at $x = \frac{1}{2}$ and

local maxima at $x = 1$

$$f\left(\frac{1}{2}\right) + f(1) = 3 + \frac{1}{2}(1 + 2\cos 1) \sin 1$$

13. If $\{a_i\}_{i=1}^n$ where n is an even integer, is an arithmetic progression with common difference 1,

and $\sum_{i=1}^n a_i = 192$, $\sum_{i=1}^{n/2} a_{2i} = 120$, then n is equal to:

- (A) 48 (B) 96
(C) 92 (D) 104

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. $\sum_{i=1}^n a_i = \frac{n}{2} \{2a_1 + (n+1)\} = 192$

$$\Rightarrow 2a_1 + (n-1) = \frac{384}{n} \text{ ----(1)}$$

$$\sum_{i=1}^{n/2} a_{2i} = \frac{n}{4} \left[2a_1 + 2 + \left(\frac{n}{2} - 1\right) 2 \right] = 120$$

$$2a_1 + n = \frac{480}{n} \text{ ----(2)}$$

From equation (2) and (1)

$$1 = \frac{480}{n} - \frac{384}{n}$$

$$n = 480 - 384 = 96$$

14. If $x = x(y)$ is the solution of the differential equation $y \frac{dx}{dy} = 2x + y^3(y+1)e^y$, $x(1) = 0$; then $x(e)$

is equal to :

- (A) $e^3(e^e - 1)$ (B) $e^e(e^3 - 1)$
(C) $e^2(e^e + 1)$ (D) $e^e(e^2 - 1)$

Official Ans. by NTA (A)

QuestPix Ans. (A)

Sol. $y \frac{dx}{dy} = 2x + y^3(y+1)e^y$, $x(1) = 0$

$$\frac{dx}{dy} - \frac{2}{y}x = y^2(y+1)e^y$$

$$I.f = e^{\int \frac{-2}{y} dy} = \frac{1}{y^2}$$

$$x \cdot \frac{1}{y^2} = \int (y+1)e^y dy$$

$$\frac{x}{y^2} = (y+1)e^y - e^y + c = y \cdot e^y + c$$

$$x = y^3 e^y + cy^2$$

For $x = 0$, $y = 1 \Rightarrow c = -e$

$$x = y^3 e^y - e \cdot y^2$$

$$x(e) = e^3(e^e - 1)$$

15. Let $\lambda x - 2y = \mu$ be a tangent to the hyperbola

$a^2x^2 - y^2 = b^2$. Then $\left(\frac{\lambda}{a}\right)^2 - \left(\frac{\mu}{b}\right)^2$ is equal to:

- (A) -2 (B) -4
(C) 2 (D) 4

Official Ans. by NTA (D)

QuestPix Ans. (D)

Sol. $\lambda x - 2y = \mu$ is a tangent to the curve

$a^2x^2 - y^2 = b^2$ then

$$a^2x^2 - \left(\frac{\lambda x - \mu}{2}\right)^2 = b^2$$

$$(4a^2 - \lambda^2)x^2 + 2\lambda\mu x - \mu^2 - 4b^2 = 0$$

Disc. = 0

$$4\lambda^2\mu^2 + 4(4a^2 - \lambda^2)(\mu^2 + 4b^2) = 0$$

$$4\lambda^2b^2 - 4a^2\mu^2 = 16a^2b^2$$

$$\frac{\lambda^2}{a^2} - \frac{\mu^2}{b^2} = 4$$

16. Let $\hat{a}, \hat{b}$ be unit vectors. If $\vec{c}$ be a vector such that the angle between $\hat{a}$ and $\vec{c}$ is $\frac{\pi}{12}$, and

$\hat{b} = \vec{c} + 2(\vec{c} \times \hat{a})$, then $|\vec{c}|^2$ is equal to

- (A) $6(3 - \sqrt{3})$ (B) $3 + \sqrt{3}$
(C) $6(3 + \sqrt{3})$ (D) $6(\sqrt{3} + 1)$

Official Ans. by NTA (C)

QuestPix Ans. (C)

Sol. $|\hat{b}|^2 = |\vec{c} + 2(\vec{c} \times \hat{a})|^2$

$$|\hat{b}|^2 = |\vec{c}|^2 + 4|\vec{c} \times \hat{a}|^2 + 4\vec{c} \cdot (\vec{c} \times \hat{a})$$

$$1 = |\vec{c}|^2 + 4|\vec{c}|^2 \sin^2 \frac{\pi}{12} + 0$$

$$1 = |\vec{c}|^2 + 4|\vec{c}|^2 \left(\frac{\sqrt{3}-1}{2\sqrt{2}}\right)^2$$

$$|\vec{c}|^2 = \frac{1}{3-\sqrt{3}} = \frac{3+\sqrt{3}}{6}$$

$$\text{So } 6^2 |\vec{c}|^2 = 6(3+\sqrt{3})$$

17. If a random variable X follows the Binomial distribution B (33, p) such that $3P(X=0) = P(X=1)$,

then the value of $\frac{P(X=15)}{P(X=18)} - \frac{P(X=16)}{P(X=17)}$ is equal

to

- (A) 1320 (B) 1088
(C) $\frac{120}{1331}$ (D) $\frac{1088}{1089}$

Official Ans. by NTA (A)

QuestPix Ans. (A)

Sol. $n = 33$, let probability of success is p and $q = 1 - p$

$$3p(x=0) = p(x=1)$$

$$3 \cdot {}^{33}C_0(q)^{33} = {}^{33}C_1pq^{32}$$

$$p = \frac{1}{12}, q = \frac{11}{12}, \frac{q}{p} = 11$$

$$\frac{p(x=15)}{p(x=18)} - \frac{p(x=16)}{p(x=17)}$$

$$\frac{{}^{33}C_{15}p^{15}q^{18}}{{}^{33}C_{18}p^{18}q^{15}} - \frac{{}^{33}C_{16}p^{16}q^{17}}{{}^{33}C_{17}p^{17}q^{16}} = \left(\frac{q}{p}\right)^3 - \left(\frac{q}{p}\right)$$

$$= (11)^3 - 11$$

$$= 1320$$

18. The domain of the function

$$f(x) = \frac{\cos^{-1}\left(\frac{x^2 - 5x + 6}{x^2 - 9}\right)}{\log_e(x^2 - 3x + 2)} \text{ is}$$

$$(A) (-\infty, 1) \cup (2, \infty)$$

$$(B) (2, \infty)$$

$$(C) \left[-\frac{1}{2}, 1\right) \cup (2, \infty)$$

$$(D) \left[-\frac{1}{2}, 1\right) \cup (2, \infty) - \left\{\frac{3+\sqrt{5}}{2}, \frac{3-\sqrt{5}}{2}\right\}$$

Official Ans. by NTA (DROP)

QuestPix Ans. (D)

Sol. $-1 \leq \frac{x^2 - 5x + 6}{x^2 - 9} \leq 1$

$$\frac{x^2 - 5x + 6}{x^2 - 9} - 1 \leq 0$$

$$\frac{1}{x+3} \geq 0$$

$$x \in (-3, \infty) \dots\dots(1)$$

$$\frac{x^2 - 5x + 6}{x^2 - 9} + 1 \geq 0$$

$$\frac{2x+1}{x+3} \geq 0$$

$$x \in (-\infty, -3) \cup \left[-\frac{1}{2}, \infty\right) \dots\dots(2)$$

after taking intersection

$$x \in \left[-\frac{1}{2}, \infty\right)$$

$$x^2 - 3x + 2 > 0$$

$$x \in (-\infty, 1) \cup (2, \infty)$$

$$x^2 - 3x + 2 \neq 1$$

$$x \neq \frac{3 \pm \sqrt{5}}{2}$$

after taking intersection of each solution

$$\left[-\frac{1}{2}, 1\right) \cup (2, \infty) - \left\{\frac{3+\sqrt{5}}{2}, \frac{3-\sqrt{5}}{2}\right\}$$

19. Let

$$S = \left\{ \theta \in [-\pi, \pi] - \left\{ \pm \frac{\pi}{2} \right\} : \sin \theta \tan \theta + \tan \theta = \sin 2\theta \right\}.$$

If $T = \sum_{\theta \in S} \cos 2\theta$, then $T + n(S)$ is equal

(A) $7 + \sqrt{3}$ (B) 9

(C) $8 + \sqrt{3}$ (D) 10

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. $\sin \theta \tan \theta + \tan \theta = \sin 2\theta$

$$\tan \theta (\sin \theta + 1) = \frac{2 \tan \theta}{1 + \tan^2 \theta}$$

$$\tan \theta = 0 \Rightarrow \theta = -\pi, 0, \pi$$

$$(\sin \theta + 1) = 2 \cos^2 \theta = 2(1 + \sin \theta)(1 - \sin \theta)$$

$\sin \theta = -1$ which is not possible

$$\sin \theta = \frac{1}{2} \quad \theta = \frac{\pi}{6}, \frac{5\pi}{6}$$

$$n(s) = 5$$

$$T = \cos 0 + \cos 2\pi + \cos 2\pi + \cos \frac{\pi}{3} + \cos \frac{5\pi}{3}$$

$$T = 4$$

$$T + n(s) = 9$$

20. The number of choices of $\Delta \in \{\wedge, \vee, \Rightarrow, \Leftrightarrow\}$, such that $(p\Delta q) \Rightarrow ((p\Delta \sim q) \vee ((\sim p)\Delta q))$ is a tautology, is

(A) 1 (B) 2

(C) 3 (D) 4

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. For tautology $((p\Delta \sim q) \vee ((\sim p)\Delta q))$ must be true.

This is possible only when $\Delta = \vee \& \Rightarrow$

SECTION-B

21. The number of one-one function $f : \{a, b, c, d\} \rightarrow \{0, 1, 2, \dots, 10\}$ such that $2f(a) - f(b) + 3f(c) + f(d) = 0$ is _____.

Official Ans. by NTA (31)

QuestPix Ans. (31)

Sol. $2f(a) + 3f(c) = f(d) - f(b)$

Using fundamental principle of counting

Number of one-one function is 31

22. In an examination, there are 5 multiple choice questions with 3 choices, out of which exactly one is correct. There are 3 marks for each correct answer, -2 marks for each wrong answer and 0 mark if the question is not attempted. Then, the number of ways a student appearing in the examination gets 5 marks is _____.

Official Ans. by NTA (40)

QuestPix Ans. (40)

Sol. $x_1 + x_2 + x_3 + x_4 + x_5 = 5$

Only one possibilities 3, 3, 3, -2, -2

$$\text{Number of ways is } = \frac{5!}{3!2!} \times 2 \times 2 = 40$$

23. Let $A\left(\frac{3}{\sqrt{a}}, \sqrt{a}\right)$ $a > 0$, be a fixed point in the xy-plane. The image of A in y-axis be B and the image of B in x-axis be C. If $D(3 \cos \theta, a \sin \theta)$ is a point in the fourth quadrant such that the maximum area of ΔACD is 12 square units, then a is equal to _____.

Official Ans. by NTA (8)

QuestPix Ans. (8)

Sol. $A = \left(\frac{3}{\sqrt{a}}, \sqrt{a} \right)$

$$B = \left(\frac{-3}{\sqrt{a}}, \sqrt{a} \right)$$

$$C = \left(-\frac{3}{\sqrt{a}}, -\sqrt{a} \right)$$

Area of ACD

$$\frac{1}{2} \begin{vmatrix} \frac{3}{\sqrt{a}} & \sqrt{a} \\ -\frac{3}{\sqrt{a}} & -\sqrt{a} \\ 3\cos\theta & a\sin\theta \end{vmatrix}$$

$$\frac{1}{2} 6\sqrt{a}(\cos\theta - \sin\theta)$$

$$3\sqrt{a}(\cos\theta - \sin\theta)$$

max values of function is $3\sqrt{a}\sqrt{2}$

$$3\sqrt{a}\sqrt{2} = 12$$

$$2a = 16$$

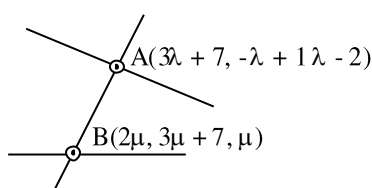
$$a = 8$$

- 24.** Let a line having direction ratios 1, -4, 2 intersect the lines $\frac{x-7}{3} = \frac{y-1}{-1} = \frac{z+2}{1}$ and $\frac{x}{2} = \frac{y-7}{3} = \frac{z}{1}$ at the point A and B. Then $(AB)^2$ is equal to ____.

Official Ans. by NTA (84)

QuestPix Ans. (84)

Sol.



DR's of AB

$$(3\lambda - 2\mu + 7, -\lambda - 3\mu - 6, \lambda - \mu - 2)$$

$$\frac{3\lambda - 2\mu + 7}{1} = \frac{-\lambda - 3\mu - 6}{-4} = \frac{\lambda - \mu - 2}{2}$$

Taking first (2) $-12\lambda + 8\mu - 28 = -\lambda - 3\mu - 6$

$$\lambda - \mu + 2 = 0$$

Taking second & third

$$-2\lambda - 6\mu - 12 = -4\lambda + 4\mu + 8$$

$$\lambda - 5\mu - 10 = 0$$

After solving above two equation $\lambda = -5, \mu = -3$

$$A = (-8, 6, 7)$$

$$B = (-6, -2, -3)$$

$$(AB)^2 = 4 + 64 + 16 = 84$$

- 25.** The number of points where the function

$$f(x) = \begin{cases} |2x^2 - 3x - 7| & \text{if } x \leq -1 \\ [4x^2 - 1] & \text{if } -1 < x < 1 \\ |x+1| + |x-2| & \text{if } x \geq 1 \end{cases}$$

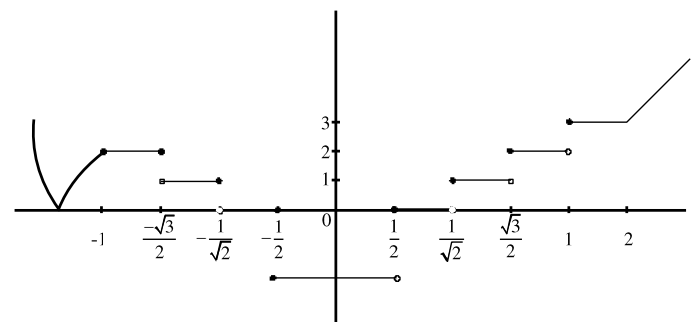
$[t]$ denotes the greatest integer $\leq t$, is

discontinuous is ____.

Official Ans. by NTA (7)

QuestPix Ans. (7)

Sol.



- 26.** Let $f(\theta) = \sin\theta + \int_{-\pi/2}^{\pi/2} (\sin\theta + t\cos\theta)f(t)dt$. Then the value of $\left| \int_0^{\pi/2} f(\theta)d\theta \right|$ is ____.

Official Ans. by NTA (1)

QuestPix Ans. (1)

Sol. $f(\theta) = \sin \theta + \int_{-\pi/2}^{\pi/2} (\sin \theta + t \cos \theta) f(t) dt$

$$f(\theta) = \sin \theta + \sin \theta \int_{-\pi/2}^{\pi/2} f(t) dt + \cos \theta \int_{-\pi/2}^{\pi/2} t f(t) dt$$

Let $A = \int_{-\pi/2}^{\pi/2} f(t) dt$, $B = \int_{-\pi/2}^{\pi/2} t f(t) dt$

$$f(\theta) = \sin \theta + A \sin \theta + B \cos \theta$$

$$f(\theta) = (A+1) \sin \theta + B \cos \theta$$

$$A = \int_{-\pi/2}^{\pi/2} (A+1) \sin t + B \cos t dt$$

$$A = 2B \quad \dots\dots(1)$$

$$B = \int_{-\pi/2}^{\pi/2} t((A+1) \sin t + B \cos t) dt$$

$$B = \int_{-\pi/2}^{\pi/2} t(A+1) \sin t dt$$

$$B = (A+1) 2 \int_0^{\pi/2} t \sin t dt$$

$$B = (A+1) 2.1$$

$$2A + 2 - B = 0 \quad \dots\dots(2)$$

After solving

$$B = -\frac{2}{3}, A = -\frac{4}{3}$$

$$\left| \int_0^{\pi/2} f(\theta) d\theta \right| = \left| \int_0^{\pi/2} -\frac{1}{3} \sin \theta - \frac{2}{3} \cos \theta \right|$$

$$= 1$$

27. Let $\text{Max}_{0 \leq x \leq 2} \left\{ \frac{9-x^2}{5-x} \right\} = \alpha$ and $\text{Min}_{0 \leq x \leq 2} \left\{ \frac{9-x^2}{5-x} \right\} = \beta$

If $\int_{\beta-\frac{8}{3}}^{2\alpha-1} \text{Max} \left\{ \frac{9-x^2}{5-x}, x \right\} dx = \alpha_1 + \alpha_2 \log_e \left(\frac{8}{15} \right)$ then

$$\alpha_1 + \alpha_2 \text{ is equal to } \underline{\hspace{2cm}}$$

Official Ans. by NTA (34)

QuestPix Ans. (34)

Sol. $y = \frac{9-x^2}{5-x} = 5 + x + \frac{16}{x-5}$

$$\frac{dy}{dx} = 1 - \frac{16}{(x-5)^2}$$

So critical point is $x = 1$ in $[0, 2]$

$$y(0) = \frac{9}{5}, y(1) = 2, y(2) = \frac{5}{3}$$

So $\alpha = 2$ and $\beta = \frac{5}{3}$

$$I = \int_{-1}^3 \max \left(\frac{9-x^2}{5-x}, x \right) dx$$

$$I = \int_{-1}^{9/5} \frac{9-x^2}{5-x} dx + \int_{9/5}^3 x dx$$

$$I = \int_{-1}^{9/5} 5 + x + \frac{16}{x-5} dx + \int_{9/5}^3 x dx$$

After solving

$$I = 14 + \frac{28}{25} + 16 \ln \left(\frac{8}{15} \right) + \frac{72}{25}$$

$$\alpha_1 = 18 \text{ and } \alpha_2 = 16$$

- 28.** If two tangents drawn from a point (α, β) lying on the ellipse $25x^2 + 4y^2 = 1$ to the parabola $y^2 = 4x$ are such that the slope of one tangent is four times the other, then the value of

$$(10\alpha + 5)^2 + (16\beta^2 + 50)^2 \text{ equals } \underline{\hspace{2cm}}$$

Official Ans. by NTA (2929)

QuestPix Ans. (2929)

Sol. $\alpha = \frac{1}{5} \cos \theta, \beta = \frac{1}{2} \sin \theta$

Equation of tangent to $y^2 = 4x$

$$y = mx + \frac{1}{m}$$

It passes through (α, β)

$$\frac{1}{2} \sin \theta = m \frac{1}{5} \cos \theta + \frac{1}{m}$$

$$m^2 \left(\frac{\cos \theta}{5} \right) - m \left(\frac{1}{2} \sin \theta \right) + 1 = 0$$

It has two roots m_1 and m_2 where $m_1 = 4m_2$

$$m_1 + m_2 = \frac{\frac{1}{2} \sin \theta}{\frac{\cos \theta}{5}}$$

$$m_1 m_2 = \frac{5}{\cos \theta}$$

After eliminating m_1 and m_2



$$\cos \theta = \frac{-5 \pm \sqrt{29}}{2}$$

$$\alpha = \frac{-5 \pm \sqrt{29}}{10} \Rightarrow 10\alpha + 5 = \pm \sqrt{29}$$

$$\beta^2 = \frac{1}{4} \sin^2 \theta \Rightarrow 16\beta^2 = -50 \pm 10\sqrt{29}$$

$$(10\alpha + 5)^2 + (16\beta^2 + 50)^2 = 2929$$

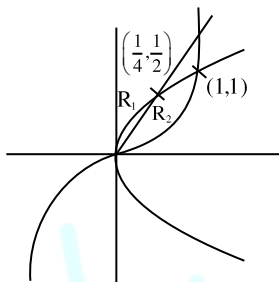
29. Let S be the region bounded by the curves $y = x^3$ and $y^2 = x$. The curve $y = 2|x|$ divides S into two regions of areas R_1 and R_2 .

If $\max \{R_1, R_2\} = R_2$, then $\frac{R_2}{R_1}$ is equal to ____.

Official Ans. by NTA (19)

QuestPix Ans. (19)

Sol.



$$S = \int_0^1 \sqrt{x} - x^3$$

$$= \left[\frac{2x^{3/2}}{3} - \frac{x^4}{4} \right]_0^1$$

$$= \frac{5}{12}$$

$$R_1 = \int_0^{1/4} (\sqrt{x} - 2x) dx$$

$$= \left[\frac{2x^{3/2}}{3} - x^2 \right]_0^{1/4} = \frac{1}{48}$$

$$\therefore R_2 = \frac{19}{48}$$

$$\text{So, } \frac{R_2}{R_1} = 19$$

30. If the shortest distance between the line

$$\vec{r} = (-\hat{i} + 3\hat{k}) + \lambda(\hat{i} - a\hat{j}) \text{ and}$$

$$\vec{r} = (-\hat{j} + 2\hat{k}) + \mu(\hat{i} - \hat{j} + \hat{k}) \text{ is } \sqrt{\frac{2}{3}}, \text{ then the integral}$$

value of a is equal to

Official Ans. by NTA (2)

QuestPix Ans. (2)

$$\text{Sol. } a_1 = (-1, 0, 3)$$

$$a_2 = (0, -1, 2)$$

$$b_1 = (1, -a, 0) \text{ dr's of line (1)}$$

$$b_2 = (1, -1, 1) \text{ dr's of line (2)}$$

$$\vec{a}_2 - \vec{a}_1 = (1, -1, -1)$$

$$\vec{b}_1 \times \vec{b}_2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -a & 0 \\ 1 & -1 & 1 \end{vmatrix}$$

$$\vec{b}_1 \times \vec{b}_2 = \hat{i}(-a) - \hat{j} + \hat{k}(a-1)$$

$$|\vec{b}_1 \times \vec{b}_2| = \sqrt{a^2 + 1 + (a-1)^2}$$

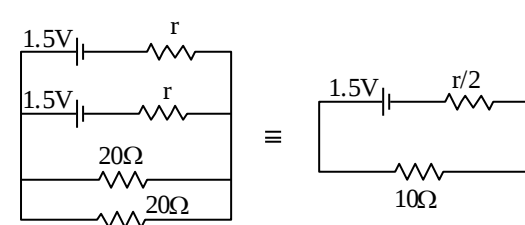
$$a_2 - a_1 \cdot \vec{b}_1 \times \vec{b}_2 = 2 - 2a$$

$$\frac{2(1-a)}{\sqrt{a^2 + 1 + (a-1)^2}} = \sqrt{\frac{2}{3}}$$

Squaring on both the side

$$\text{After solving } a = 2, \frac{1}{2}$$

(Held On Friday 24th June, 2022)
TIME : 9 : 00 AM to 12 : 00 PM

PHYSICS	TEST PAPER WITH SOLUTION
SECTION-A 31. The bulk modulus of a liquid is $3 \times 10^{10} \text{ Nm}^{-2}$. The pressure required to reduce the volume of liquid by 2% is : (A) $3 \times 10^8 \text{ Nm}^{-2}$ (B) $9 \times 10^8 \text{ Nm}^{-2}$ (C) $6 \times 10^8 \text{ Nm}^{-2}$ (D) $12 \times 10^8 \text{ Nm}^{-2}$ Official Ans. by NTA (C) QuestPix Ans. (C) Sol. $B = 3 \times 10^{10}$ $-\frac{\Delta V}{V} = 0.02$ $B = \frac{\Delta P}{-\frac{\Delta V}{V}} \Rightarrow \Delta P = -B \left(\frac{\Delta V}{V} \right)$ $= (3 \times 10^{10})(0.02)$ $= 6 \times 10^8 \text{ N / m}^2$ 32. Given below are two statements : One is labelled as Assertion (A) and the other is labelled as Reason (R). Assertion (A) : In an uniform magnetic field, speed and energy remains the same for a moving charged particle. Reason (R) : Moving charged particle experiences magnetic force perpendicular to its direction of motion. (A) Both (A) and (R) are true and (R) is the correct explanation of (A) (B) Both (A) and (R) are true but (R) is NOT the correct explanation of (A) (C) (A) is true but (R) is false (D) (A) is false but (R) is true. Official Ans. by NTA (A) QuestPix Ans. (A)	Sol. $\vec{F} = q(\vec{v} \times \vec{B})$ $\vec{F} \perp \vec{v}$ Work done $= \vec{F} \cdot \vec{S}$ Work done $= 0$ 33. Two identical cells each of emf 1.5 V are connected in parallel across a parallel combination of two resistors each of resistance 20Ω. A voltmeter connected in the circuit measures 1.2 V. The internal resistance of each cell is (A) 2.5Ω (B) 4Ω (C) 5Ω (D) 10Ω Official Ans. by NTA (C) QuestPix Ans. (C) Sol.  $V = E - ir/2$ $1.2 = 1.5 - i \left(\frac{r}{2} \right)$ $i \frac{r}{2} = 0.3$ $i = \frac{1.5}{10 + \frac{r}{2}} \Rightarrow 10i + \frac{ir}{2} = 1.5$ $10i = 1.5 - 0.3$ $i = 0.12 \text{ A}$ $\Rightarrow r = \frac{0.6}{0.12} = 5\Omega$

34. Identify the pair of physical quantities which have different dimensions :

(A) Wave number and Rydberg's constant
 (B) Stress and Coefficient of elasticity
 (C) Coercivity and Magnetisation
 (D) Specific heat capacity and Latent heat

Official Ans. by NTA (D)

QuestPix Ans. (D)

Sol. $S = \frac{Q}{m\Delta T} = \frac{J}{Kg^{\circ}C}$

$$L = \frac{Q}{m} = \frac{J}{Kg}$$

35. A projectile is projected with velocity of 25 m/s at an angle θ with the horizontal. After t seconds its inclination with horizontal becomes zero. If R represents horizontal range of the projectile, the value of θ will be : [use $g = 10 \text{ m/s}^2$]

(A) $\frac{1}{2} \sin^{-1} \left(\frac{5t^2}{4R} \right)$ (B) $\frac{1}{2} \sin^{-1} \left(\frac{4R}{5t^2} \right)$
 (C) $\tan^{-1} \left(\frac{4t^2}{5R} \right)$ (D) $\cot^{-1} \left(\frac{R}{20t^2} \right)$

Official Ans. by NTA (D)

QuestPix Ans. (D)

Sol. $R = \frac{V^2 (2 \sin \theta \cos \theta)}{g}$

$$t = \frac{V \sin \theta}{g} \Rightarrow V = \frac{gt}{\sin \theta}$$

$$\Rightarrow R = \frac{g^2 t^2}{\sin^2 \theta} \cdot \frac{2 \sin \theta \cos \theta}{g}$$

$$\tan \theta = \frac{2gt^2}{R} = \frac{20t^2}{R}$$

$$\cot \theta = \frac{R}{20t^2}$$

36. A block of mass 10 kg starts sliding on a surface with an initial velocity of 9.8 ms^{-1} . The coefficient of friction between the surface and block is 0.5. The distance covered by the block before coming to rest is : [use $g = 9.8 \text{ ms}^{-2}$]

(A) 4.9 m (B) 9.8 m
 (C) 12.5 m (D) 19.6 m

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. $a = -\mu g = -0.5 \times 9.8 = -4.9 \text{ m/s}^2$

$$d = \frac{v^2}{2a} = \frac{9.8 \times 9.8}{2(4.9)}$$

$$= 9.8 \text{ m}$$

37. A boy ties a stone of mass 100 g to the end of a 2 m long string and whirls it around in a horizontal plane. The string can withstand the maximum tension of 80 N. If the maximum speed with which the stone can revolve is $\frac{K}{\pi} \text{ rev./min}$. The value of

K is : (Assume the string is massless and unstretchable)

(A) 400 (B) 300
 (C) 600 (D) 800

Official Ans. by NTA (C)

QuestPix Ans. (C)

Sol. $T = M\omega^2 R$

$$T = 80 \text{ N} \quad M = 0.1 \quad \omega = ? \quad R = 2 \text{ m}$$

$$80 = 0.1 \omega^2 (2)$$

$$\omega^2 = 400$$

$$\omega = 20$$

$$2\pi f = 20$$

$$f = \frac{10 \text{ rev}}{\pi \text{ s}}$$

$$= \frac{600 \text{ rev}}{\pi \text{ min}}$$

38. A vertical electric field of magnitude $4.9 \times 10^5 \text{ N/C}$ just prevents a water droplet of a mass 0.1 g from falling. The value of charge on the droplet will be :

(Given $g = 9.8 \text{ m/s}^2$)

- (A) $1.6 \times 10^{-9} \text{ C}$ (B) $2.0 \times 10^{-9} \text{ C}$
(C) $3.2 \times 10^{-9} \text{ C}$ (D) $0.5 \times 10^{-9} \text{ C}$

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. $Mg = qE$

$$(0.1 \times 10^{-3})(9.8) = 4.9 \times 10^5 q$$

$$\frac{2 \times 10^{-4}}{10^5} = q$$

$$q = 2 \times 10^{-9} \text{ C}$$

39. A particle experiences a variable force $\vec{F} = (4x\hat{i} + 3y^2\hat{j})$ in a horizontal x-y plane. Assume distance in meters and force is newton. If the particle moves from point (1, 2) to point (2, 3) in the x-y plane, the Kinetic Energy changes by

- (A) 50.0 J (B) 12.5 J
(C) 25.0 J (D) 0 J

Official Ans. by NTA (C)

QuestPix Ans. (C)

Sol. $F = 4x\hat{i} + 3y^2\hat{j}$

$$WD = \Delta KE$$

$$W = \int \vec{F} \cdot (dx\hat{i} + dy\hat{j})$$

$$= \int_1^2 4x dx + \int_2^3 3y^2 dy$$

$$= (2x^2)_1^2 + (y^3)_2^3$$

$$= (8 - 2) + (27 - 8)$$

$$= 6 + 19 = 25 \text{ J}$$

40. The approximate height from the surface of earth at which the weight of the body becomes $\frac{1}{3}$ of its weight on the surface of earth is : [Radius of earth $R = 6400 \text{ km}$ and $\sqrt{3} = 1.732$]

- (A) 3840 km (B) 4685 km
(C) 2133 km (D) 4267 km

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. $Mg' = \frac{M}{3}g$

$$g' = \frac{g}{3}$$

$$g' = g \left(\frac{R}{R+h} \right)^2 = \frac{g}{3}$$

$$\frac{R}{R+h} = \frac{1}{\sqrt{3}}$$

$$h = (\sqrt{3} - 1)R$$

$$= (1.732 - 1)6400$$

$$h = 4685 \text{ km}$$

41. A resistance of 40Ω is connected to a source of alternating current rated 220 V , 50 Hz . Find the time taken by the current to change from its maximum value to rms value :

- (A) 2.5 ms (B) 1.25 ms
(C) 2.5 s (D) 0.25 s

Official Ans. by NTA (A)

QuestPix Ans. (A)

Sol. Considering sinusoidal AC.

$$\text{Phase at maximum value} = \frac{\pi}{2}$$

$$\text{Phase at rms value} = \frac{3\pi}{4}$$

$$\text{Thus phase change} = \frac{3\pi}{4} - \frac{\pi}{2} = \frac{\pi}{4}$$

$$\text{Now } \omega = 2\pi f$$

$$= 2\pi \times 50$$

$$= 100\pi$$

$$\text{time taken } t = \frac{\theta}{\omega} = \frac{\pi/4}{100\pi} = \frac{1}{400} \text{ s}$$

$$t = 2.5 \times 10^{-3} = 2.5 \text{ ms}$$

42. The equations of two waves are given by :

$$y_1 = 5 \sin 2\pi(x - vt) \text{ cm}$$

$$y_2 = 3 \sin 2\pi(x - vt + 1.5) \text{ cm}$$

These waves are simultaneously passing through a string. The amplitude of the resulting wave is

- (A) 2 cm (B) 4 cm
(C) 5.8 cm (D) 8 cm

Official Ans. by NTA (A)

QuestPix Ans. (A)

Sol. $A_1 = 5 \quad A_2 = 3$

$$\Delta\theta = 2\pi(1.5) = 3\pi$$

$$A_{\text{net}} = \sqrt{A_1^2 + A_2^2 + 2A_1A_2 \cos(3\pi)}$$

$$= |A_1 - A_2|$$

$$= 2 \text{ cm}$$

43. A plane electromagnetic wave travels in a medium of relative permeability 1.61 and relative permittivity 6.44. If magnitude of magnetic intensity is $4.5 \times 10^{-2} \text{ Am}^{-1}$ at a point, what will be the approximate magnitude of electric field intensity at that point ?

(Given : permeability of free space $\mu_0 = 4\pi \times 10^{-7} \text{ NA}^{-2}$, speed of light in vacuum $c = 3 \times 10^8 \text{ ms}^{-1}$)

- (A) 16.96 Vm^{-1} (B) $2.25 \times 10^{-2} \text{ Vm}^{-1}$
(C) 8.48 Vm^{-1} (D) $6.75 \times 10^6 \text{ Vm}^{-1}$

Official Ans. by NTA (C)

QuestPix Ans. (Bonus)

Sol. $\mu_r = 1.61 \quad \epsilon_r = 6.44$

$$B = 4.5 \times 10^{-2}$$

$$E = ?$$

$$C = \frac{1}{\sqrt{\mu_0 \epsilon_0}} \quad V = \frac{1}{\sqrt{\mu \epsilon}}$$

$$\frac{C}{V} = \sqrt{\mu_r \epsilon_r} = \sqrt{1.61 \times 6.44}$$

$$\frac{E}{B} = V = \frac{3 \times 10^8}{\sqrt{1.61 \times 6.44}} = 9.32 \times 10^7 \text{ m/s}$$

$$E = 4.5 \times 10^{-2} \times 9.32 \times 10^7$$

$$= 4.2 \times 10^6$$

44. Choose the correct option from the following options given below :

- (A) In the ground state of Rutherford's model electrons are in stable equilibrium. While in Thomson's model electrons always experience a net-force.
(B) An atom has a nearly continuous mass distribution in a Rutherford's model but has a highly non-uniform mass distribution in Thomson's model
(C) A classical atom based on Rutherford's model is doomed to collapse.
(D) The positively charged part of the atom possesses most of the mass in Rutherford's model but not in Thomson's model.

Official Ans. by NTA (C)

QuestPix Ans. (C)

- Sol.** According to Rutherford, e^- revolves around nucleus in circular orbit. Thus e^- is always accelerating (centripetal acceleration). An accelerating charge emits EM radiation and thus e^- should lose energy and finally should collapse in the nucleus.

45. Nucleus A is having mass number 220 and its binding energy per nucleon is 5.6 MeV. It splits in two fragments 'B' and 'C' of mass numbers 105 and 115. The binding energy of nucleons in 'B' and 'C' is 6.4 MeV per nucleon. The energy Q released per fission will be :

- (A) 0.8 MeV (B) 275 MeV
(C) 220 MeV (D) 176 MeV

Official Ans. by NTA (D)

QuestPix Ans. (D)

Sol. $Q = (B.E)_p - (B.E)_r$
 $= (105 + 115)(6.4) - (220)(5.6)$
 $= 176 \text{ MeV}$

46. A baseband signal of 3.5 MHz frequency is modulated with a carrier signal of 3.5 GHz frequency using amplitude modulation method. What should be the minimum size of antenna required to transmit the modulated signal ?

- (A) 42.8 m (B) 42.8 mm
(C) 21.4 mm (D) 21.4 m

Official Ans. by NTA (C)

QuestPix Ans. (C)

Sol. $f_c = 3.5\text{GHz}$ $f_m = 3.5\text{MHz}$

Side band frequencies are $f_c - f_m$ & $f_c + f_m$. which are almost f_c

$$\lambda = \frac{c}{f_c}$$

Minimum length of antenna =

$$\frac{c}{f_c \cdot 4} = \frac{\lambda}{4} = \frac{3 \times 10^8}{3.5 \times 10^9 \times 4}$$

$$= 21.4 \text{ mm}$$

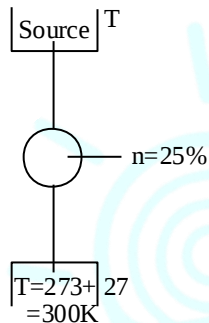
- 47.** A Carnot engine whose heat sinks at 27°C , has an efficiency of 25%. By how many degrees should the temperature of the source be changed to increase the efficiency by 100% of the original efficiency ?

- (A) Increases by 18°C (B) Increase by 200°C
(C) Increase by 120°C (D) Increase by 73°

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol.



$$1 - \frac{300}{T} = 0.25$$

$$\frac{300}{T} = 0.75$$

$$T = 400\text{K}$$

If efficiency increased by 100% then new efficiency $\Rightarrow n' = 50\%$

$$1 - \frac{300}{T'} = 0.5$$

$$T' = 600\text{K}$$

$$\begin{aligned} \text{Increase in temp} &= 600 - 400 \\ &= 200 \text{ K or } 200^\circ\text{C} \end{aligned}$$

- 48.** A parallel plate capacitor is formed by two plates each of area $30\pi \text{ cm}^2$ separated by 1 mm. A material of dielectric strength $3.6 \times 10^7 \text{ Vm}^{-1}$ is filled between the plates. If the maximum charge that can be stored on the capacitor without causing any dielectric breakdown is $7 \times 10^{-6} \text{ C}$, the value of dielectric constant of the material is :

$$\left\{ \text{Use : } \frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ Nm}^2\text{C}^{-2} \right\}$$

- (A) 1.66 (B) 1.75
(C) 2.25 (D) 2.33

Official Ans. by NTA (D)

QuestPix Ans. (D)

Sol. $K = \frac{q}{A \epsilon_0 E} = \frac{7 \times 10^{-6}}{30\pi \times 10^{-4} \times \frac{1}{4\pi \times 9 \times 10^9} \times 3.6 \times 10^7}$

$$K = \frac{36 \times 7}{30 \times 3.6} = 2.33$$

- 49.** The magnetic field at the centre of a circular coil of radius r , due to current I flowing through it, is B . The magnetic field at a point along the axis at a distance $\frac{r}{2}$ from the centre is :

- (A) $B/2$ (B) $2B$
(C) $\left(\frac{2}{\sqrt{5}}\right)^3 B$ (D) $\left(\frac{2}{\sqrt{3}}\right)^3 B$

Official Ans. by NTA (C)

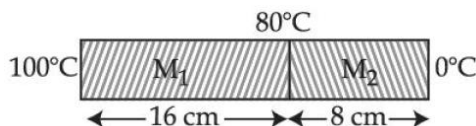
QuestPix Ans. (C)

Sol. $B_c = \frac{\mu_0 I}{2r}, B_a = \frac{\mu_0 I r^2}{2(x^2 + r^2)^{3/2}}$

$$\text{At } x = \frac{r}{2}$$

$$\begin{aligned} B_a &= \frac{\mu_0 I r^2}{2\left(\frac{r^2}{4} + r^2\right)^{3/2}} \\ &= \frac{\mu_0 I r^2}{2\left(\frac{5}{4}r^2\right)^{3/2}} = \frac{\mu_0 I}{2r} \left(\frac{4}{5}\right)^{3/2} \\ &= \frac{\mu_0 I}{2r} \left(\frac{2}{\sqrt{5}}\right)^3 \end{aligned}$$

50. Two metallic blocks M_1 and M_2 of same area of cross-section are connected to each other (as shown in figure). If the thermal conductivity of M_2 is K then the thermal conductivity of M_1 will be : [Assume steady state heat conduction]



- (A) 10 K (B) 8 K
(C) 12.5 K (D) 2 K

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. $\Delta T \propto R \propto \frac{\ell}{k}$,

$$\frac{\Delta T_1}{\Delta T_2} = \frac{\ell_1}{k_1} \times \frac{k_2}{\ell_2} = \frac{16}{k_1} \times \frac{k}{8}$$

$$\frac{20}{80} = \frac{16}{k_1} \times \frac{k}{8} \rightarrow k_1 = 8k$$

SECTION-B

51. 0.056 kg of Nitrogen is enclosed in a vessel at a temperature of 127°C . The amount of heat required to double the speed of its molecules is _____ k cal. (Take $R = 2 \text{ cal mole}^{-1}\text{K}^{-1}$)

Official Ans. by NTA (12)

QuestPix Ans. (12)

Sol. $0.056 \text{ kg } N_2 = 56 \text{ gm of } N_2 = 2 \text{ mole of } N_2$

$$T_1 = 400 \text{ K, } v \propto \sqrt{T} \text{ so } T_2 = 4T_1 = 1600\text{K}$$

$$Q = \frac{f}{2} n R \Delta T$$

$$f = 5$$

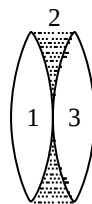
$$Q = 12 \text{ k cal}$$

52. Two identical thin biconvex lenses of focal length 15 cm and refractive index 1.5 are in contact with each other. The space between the lenses is filled with a liquid of refractive index 1.25. The focal length of the combination is _____ cm.

Official Ans. by NTA (10)

QuestPix Ans. (10)

Sol.



$$\frac{1}{f_1} = \frac{1}{15} = \left(\frac{3}{2} - 1 \right) \left[\frac{2}{R} \right]$$

$$\frac{1}{R} = \frac{1}{15}$$

$$\frac{1}{f_{eq}} = \frac{1}{f_1} + \frac{1}{f_2} + \frac{1}{f_3}$$

$$= \frac{1}{15} + \left(\frac{5}{4} - 1 \right) \left[\frac{-2}{R} \right] + \frac{1}{15}$$

$$= \frac{1}{15} - \frac{1}{30} + \frac{1}{15}$$

$$= \frac{2 - 1 + 2}{30}$$

$$= \frac{3}{30} = \frac{1}{10}$$

$$= 10$$

53. A transistor is used in common-emitter mode in an amplifier circuit. When a signal of 10 mV is added to the base-emitter voltage, the base current changes by 10 μA and the collector current changes by 1.5 mA. The load resistance is 5 k Ω . The voltage gain of the transistor will be _____.

Official Ans. by NTA (750)

QuestPix Ans. (750)

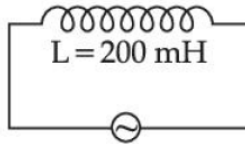
Sol. $r_i = \frac{10\text{mV}}{10\mu\text{A}} = 10^3 \Omega$

$$\beta = \frac{1.5\text{mA}}{10\mu\text{A}} = 150$$

$$A_v = \left(\frac{R_o}{r_i} \right) \beta = \left(\frac{5000}{1000} \right) \times 150 = 750$$



54. As shown in the figure an inductor of inductance 200 mH is connected to an AC source of emf 220 V and frequency 50 Hz. The instantaneous voltage of the source is 0 V when the peak value of current is $\frac{\sqrt{a}}{\pi}$ A. The value of a is _____.



Official Ans. by NTA (242)

QuestPix Ans. (242)

Sol. $f = 50 \text{ Hz}$
 $X_L = 2\pi fL$
 $= 2\pi(50)(200 \times 10^{-3})$
 $= 20\pi \Omega$
 $i_0 = \frac{V_0}{X_L} \Rightarrow \frac{V_{\text{rms}}\sqrt{2}}{X_L}$
 $= \frac{(220)\sqrt{2}}{20\pi} = \frac{11\sqrt{2}}{\pi}$
 $i_0 = \frac{\sqrt{242}}{\pi}$

55. Sodium light of wavelengths 650 nm and 655 nm is used to study diffraction at a single slit of aperture 0.5 mm. The distance between the slit and the screen is 2.0 m. The separation between the positions of the first maxima of diffraction pattern obtained in the two cases is _____ $\times 10^{-5}$ m.

Official Ans. by NTA (3)

QuestPix Ans. (3)

Sol. $a \sin \theta = \frac{3\lambda}{2}$
 $\frac{y}{L} = \theta = \frac{3\lambda}{2a}$ $L = 2 \text{ m}$
 $y_1 = \frac{3\lambda_1 L}{2a}$ $\lambda_2 = 655 \text{ nm}$
 $y_2 = \frac{3\lambda_2 L}{2a}$ $\lambda_1 = 650 \text{ nm}$
 $a = 0.5 \text{ mm}$
 $\Delta y = y_2 - y_1 = \frac{3(\lambda_2 - \lambda_1)}{2a} L$
 $= \frac{3(655 - 650)}{2 \times 0.5 \times 10^{-3}} \times 2 \times 10^{-9}$
 $= \frac{3 \times 5 \times 2}{1 \times 10^{-3}} \times 10^{-9}$
 $= 3 \times 10^{-5}$

56. When light of frequency twice the threshold frequency is incident on the metal plate, the maximum velocity of emitted electron is v_1 . When the frequency of incident radiation is increased to five times the threshold value, the maximum velocity of emitted electron becomes v_2 . If $v_2 = x v_1$, the value of x will be _____.

Official Ans. by NTA (2)

QuestPix Ans. (2)

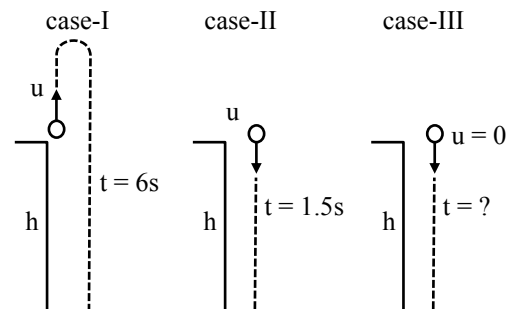
Sol. $h\nu = h\nu_{\text{th}} + \frac{1}{2}mv^2$
 $v = 2v_{\text{th}}$
 $2h\nu_{\text{th}} = h\nu_{\text{th}} + \frac{1}{2}mv_1^2 \dots (1)$
 $v = 5v_{\text{th}}$
 $5h\nu_{\text{th}} = h\nu_{\text{th}} + \frac{1}{2}mv_2^2 \dots (2)$
 $\frac{\frac{1}{2}mv_1^2}{\frac{1}{2}mv_2^2} = \frac{h\nu_{\text{th}}}{4h\nu_{\text{th}}}$
 $\left(\frac{v_1}{v_2}\right)^2 = \frac{1}{4} \Rightarrow v_2 = 2v_1$

57. From the top of a tower, a ball is thrown vertically upward which reaches the ground in 6 s. A second ball thrown vertically downward from the same position with the same speed reaches the ground in 1.5 s. A third ball released, from the rest from the same location, will reach the ground in _____ s.

Official Ans. by NTA (3)

QuestPix Ans. (3)

- Sol.** Let height of tower be h and speed of projection in first two cases be u.



For case-I : 2nd equation $s = ut + \frac{1}{2}at^2$

$$h = -u(6) + \frac{1}{2}g(6)^2$$

$$H = -6u + 18g \dots (i)$$

$$\text{For case-II : } h = u(1.5) + \frac{1}{2}g(1.5)^2$$

$$h = 1.5u + \frac{2.25g}{2} \dots (ii)$$

Multiplying equation (ii) by 4 we get

$$4h = 6u + 4.5g \dots (iii)$$

equation (i) + equation (iii) we get $5h = 22.5g$

$$h = 4.5g \dots (iv)$$

For case-III :

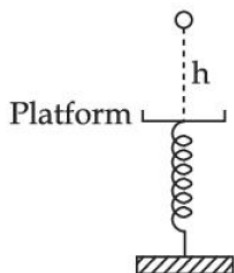
$$h = 0 + \frac{1}{2}gt^2 \dots (v)$$

Using equation (4) & equation (5)

$$4.5g = \frac{1}{2}gt^2$$

$$t^2 = 9 \Rightarrow t = 3s$$

- 58.** A ball of mass 100 g is dropped from a height $h = 10$ cm on a platform fixed at the top of vertical spring (as shown in figure). The ball stays on the platform and the platform is depressed by a distance $\frac{h}{2}$. The spring constant is _____ Nm^{-1} . (Use $g = 10 \text{ ms}^{-2}$)



Official Ans. by NTA (120)

QuestPix Ans. (120)

Sol. By energy conservation

$$PE = KE$$

$$mg\left(H + \frac{H}{2}\right) = \frac{1}{2}kx^2 \left(x = \frac{H}{2}\right)$$

$$0.100 \times 10 \times \frac{3}{2}(0.10) = \frac{1}{2}k(0.05 \times 0.05)$$

$$k = \frac{3 \times 0.10}{0.05 \times 0.05}$$

$$= \frac{3 \times 1000}{25} = 120 \text{ N/m}$$

- 59.** In a potentiometer arrangement, a cell gives a balancing point at 75 cm length of wire. This cell is now replaced by another cell of unknown emf. If the ratio of the emf's of two cells respectively is 3 : 2, the difference in the balancing length of the potentiometer wire in above two cases will be _____ cm.

Official Ans. by NTA (25)

QuestPix Ans. (25)

Sol. $\frac{\varepsilon_1}{\varepsilon_2} = \frac{\ell_1}{\ell_2}$

$$\frac{3}{2} = \frac{75 \text{ cm}}{\ell_2}$$

$$\ell_2 = 50 \text{ cm}$$

$$\ell_1 - \ell_2 = 75 - 50$$

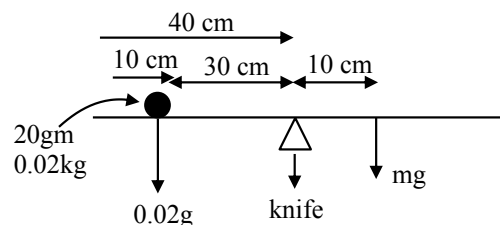
$$= 25 \text{ cm}$$

- 60.** A metre scale is balanced on a knife edge at its centre. When two coins, each of mass 10 g are put one on the top of the other at the 10.0 cm mark the scale is found to be balanced at 40.0 cm mark. The mass of the metre scale is found to be $x \times 10^{-2}$ kg. The value of x is

Official Ans. by NTA (6)

QuestPix Ans. (6)

Sol. Let mass of meter scale be m .



Balancing torque about knife edge

$$(0.02g) \times (30 \times 10^{-2}) = mg \times (10 \times 10^{-2})$$

$$m = 0.06 \text{ kg} = 6 \times 10^{-2} \text{ kg}$$

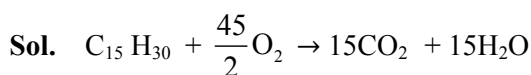
(Held On Friday 24th June, 2022)
TIME : 9 : 00 AM to 12 : 00 PM
CHEMISTRY
SECTION-A

61. If a rocket runs on a fuel ($C_{15}H_{30}$) and liquid oxygen, the weight of oxygen required and CO_2 released for every litre of fuel respectively are:
(Given: density of the fuel is 0.756 g/mL)

- (A) 1188 g and 1296 g (B) 2376 g and 2592 g
(C) 2592g and 2376 g (D) 3429 g and 3142 g

Official Ans. by NTA (C)

QuestPix Ans. (C)



$$\text{Mass of fuel} = 0.756 \times 1000 \text{ g}$$

$$\text{No. of moles of fuel} = \frac{0.756 \times 1000}{210}$$

$$\text{Wt. of oxygen} = \frac{0.756 \times 1000}{210} \times \frac{45}{2} \times 32 = 2592 \text{ g}$$

$$\text{Wt of } CO_2 = \frac{0.756 \times 1000}{210} \times 15 \times 44 = 2376 \text{ g}$$

62. Consider the following pairs of electrons

(A) (a) $n = 3, l = 1, m_l = 1, m_s = +\frac{1}{2}$

(b) $n = 3, l = 2, m_l = 1, m_s = +\frac{1}{2}$

(B) (a) $n = 3, l = 2, m_l = -2, m_s = -\frac{1}{2}$

(b) $n = 3, l = 2, m_l = -1, m_s = -\frac{1}{2}$

(C) (a) $n = 4, l = 2, m_l = 2, m_s = +\frac{1}{2}$

(b) $n = 3, l = 2, m_l = 2, m_s = +\frac{1}{2}$

The pairs of electron present in degenerate orbitals is/are:

- (A) Only A
(B) Only B
(C) Only C
(D) (B) and (C)

TEST PAPER WITH SOLUTION

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. Based on “ $n + l$ ” rule only (B) has pair of electron in degenerate orbitals

63. Match List – I with List - II

List – I		List – II	
(A)	$[PtCl_4]^{2-}$	(I)	sp^3d
(B)	BrF_5	(II)	d^2sp^3
(C)	PCl_5	(III)	dsp^2
(D)	$[Co(NH_3)_6]^{3+}$	(IV)	sp^3d^2

(A) (A)→(II), (B)→(IV), (C)→(I), (D)→(III)

(B) (A)→(III), (B)→(IV), (C)→(I), (D)→(II)

(C) (A)→(III), (B)→(I), (C)→(IV), (D)→(II)

(D) (A)→(II), (B)→(I), (C)→(IV), (D)→(III)

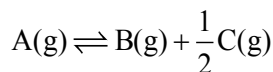
Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. Answer (B)

List – I		List – II	
(A)	$[PtCl_4]^{2-}$	(III)	dsp^2
(B)	BrF_5	(IV)	sp^3d^2
(C)	PCl_5	(I)	sp^3d
(D)	$[Co(NH_3)_6]^{3+}$	(II)	d^2sp^3

64. For a reaction at equilibrium



the relation between dissociation constant (K), degree of dissociation (α) and equilibrium pressure (p) is given by :

$$(A) K = \frac{\alpha^{\frac{1}{2}} p^{\frac{3}{2}}}{\left(1 + \frac{3}{2}\alpha\right)^{\frac{1}{2}} (1-\alpha)}$$

$$(B) K = \frac{\alpha^{\frac{3}{2}} p^{\frac{1}{2}}}{(2 + \alpha)^{\frac{1}{2}} (1-\alpha)}$$

$$(C) K = \frac{(\alpha p)^{\frac{3}{2}}}{\left(1 + \frac{3}{2}\alpha\right)^{\frac{1}{2}} (1-\alpha)}$$

$$(D) K = \frac{(\alpha p)^{\frac{3}{2}}}{(1 + \alpha)(1-\alpha)^{\frac{1}{2}}}$$

Official Ans. by NTA (B)

QuestPix Ans. (B)



Initial : P_i **0** **0**

At eq.: $P_i(1-\alpha)$ $P_i \cdot \alpha$ $P_i \frac{\alpha}{2}$

Now, equilibrium pressure (p) ,

$$P = P_i \times \left(1 + \frac{\alpha}{2}\right)$$

$$\therefore P_A = \left(\frac{1-\alpha}{1 + \frac{\alpha}{2}}\right) P$$

$$P_B = \left(\frac{\alpha}{1 + \frac{\alpha}{2}}\right) P$$

$$P_C = \left(\frac{\frac{\alpha}{2}}{1 + \frac{\alpha}{2}}\right) P$$

$$\therefore K = \frac{P_C^{\frac{1}{2}} \times P_B}{P_A}$$

$$K = \frac{\alpha^{\frac{3}{2}} p^{\frac{1}{2}}}{(2 + \alpha)^{\frac{1}{2}} (1-\alpha)}$$

65. Given below are two statements :

Statement I : Emulsions of oil in water are unstable and sometimes they separate into two layers on standing.

Statement II :For stabilisation of an emulsion, excess of electrolyte is added.

In the light of the above statements, choose the most appropriate answer from the options given below :

- (A) Both Statement I and Statement II are correct.
- (B) Both Statement I and Statement II are incorrect.
- (C) Statement I is correct but Statement II is incorrect.
- (D) Statement I is incorrect but Statement II is correct.

Official Ans. by NTA (C)

QuestPix Ans. (C)

Sol. Statement I : Fact

Statement II: The principle emulsifying agents for O/W emulsions are proteins, gums natural and synthetic soaps etc...

66. Given below are the oxides:



Number of amphoteric oxides is:

- (A) 0 (B) 1
- (C) 2 (D) 3

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. Na_2O = Basic As_2O_3 = Amphoteric
 N_2O = Neutral NO = Neutral
 Cl_2O_7 = Acidic

67. Match List – I with List – II

	List - I		List - II
(A)	Sphalerite	(I)	FeCO ₃
(B)	Calamine	(II)	PbS
(C)	Galena	(III)	ZnCO ₃
(D)	Siderite	(IV)	ZnS

Choose the most appropriate answer from the options given below:

- (A) (A) - (IV), (B) - (III), (C) - (II), (D) - (I)
 (B) (A) - (IV), (B) - (I), (C) - (II), (D) - (III)
 (C) (A) - (II), (B) - (III), (C) - (I), (D) - (IV)
 (D) (A) - (III), (B) - (IV), (C) - (II), (D) - (I)

Official Ans. by NTA (A)

QuestPix Ans. (A)

Sol.

	List - I		List - II
(A)	Sphalerite	(IV)	ZnS
(B)	Calamine	(III)	ZnCO ₃
(C)	Galena	(II)	PbS
(D)	Siderite	(I)	FeCO ₃

68. The highest industrial consumption of molecular hydrogen is to produce compounds of element:

- (A) Carbon (B) Nitrogen
 (C) Oxygen (D) Chlorine

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. Nitrogen . Around 55% of hydrogen around would goes to ammonia production

69. Which of the following statements are correct ?

- (A) Both LiCl and MgCl₂ are soluble in ethanol.
 (B) The oxides Li₂O and MgO combine with excess of oxygen to give superoxide.
 (C) LiF is less soluble in water than other alkali metal fluorides.
 (D) Li₂O is more soluble in water than other alkali metal oxides.

Choose the most appropriate answer from the options given below:

- (A) (A) and (C) only (B) (A), (C) and (D) only
 (C) (B) and (C) only (D) (A) and (C) only

Official Ans. by NTA (A)

QuestPix Ans. (A)

Sol. (A) Both LiCl and MgCl₂ are soluble in ethanol

(B) Li and Mg do not form superoxide

(C) LiF has high lattice energy

(D) Li₂O is least soluble in water than other alkali metal oxides

70. Identify the correct statement for B₂H₆ from those given below.

(A) In B₂H₆, all B-H bonds are equivalent.

(B) In B₂H₆ there are four 3-centre-2-electron bonds.

(C) B₂H₆ is a Lewis acid.

(D) B₂H₆ can be synthesized from both BF₃ and NaBH₄.

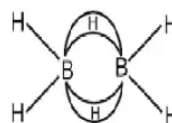
(E) B₂H₆ is a planar molecule.

Choose the most appropriate answer from the options given below :

- (A) (A) and (E) only (B) (B), (C) and (E) only
 (C) (C) and (D) only (D) (C) and (E) only

Official Ans. by NTA (C)

QuestPix Ans. (C)



Sol. (A) (B)

Two 3 centre – 2 – electron bonds

(C) B₂H₆ is e⁻ deficient species

(E) B₂H₆ is non – Planar molecule

(D) BF₃ + LiAlH₄ → 2B₂H₆ + 3LiF + 3AlF₃

NaBH₄ + I₂ → B₂H₆ + 2NaI + H₂

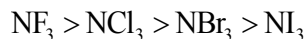
71. The most stable trihalide of nitrogen is:

- (A) NF₃ (B) NCl₃
 (C) NBr₃ (D) NI₃

Official Ans. by NTA (A)

QuestPix Ans. (A)

Sol. Order of stability: -



72. Which one of the following elemental forms is not present in the enamel of the teeth?

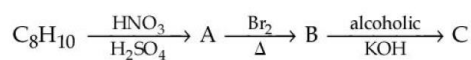
- (A) Ca^{2+} (B) P^{3+}
(C) F^- (D) P^{5+}

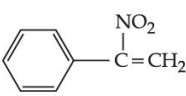
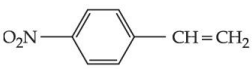
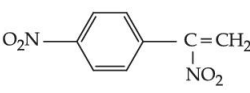
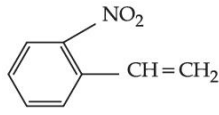
Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. Calcium and phosphate are the major components of teeth enamel

73. In the given reactions sequence, the major product 'C' is :

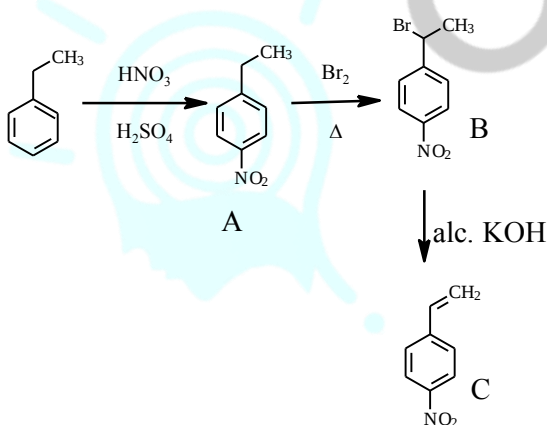


- (A)  (B) 
(C)  (D) 

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. C_8H_{10} DU = $9 - 5 = 4$



74. Two statements are given below :

Statement I: The melting point of monocarboxylic acid with even number of carbon atoms is higher than that of with odd number of carbon atoms acid immediately below and above it in the series.

Statement II : The solubility of monocarboxylic acids in water decreases with increase in molar mass.

Choose the most appropriate option:

- (A) Both Statement I and Statement II are correct.
(B) Both Statement I and Statement II are incorrect.
(C) Statement I is correct but Statement II is incorrect.
(D) Statement I is incorrect but Statement II is correct.

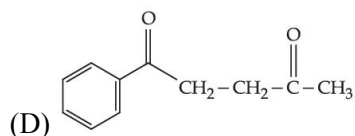
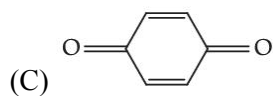
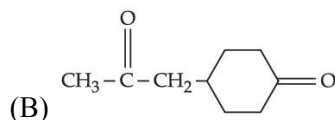
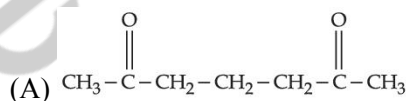
Official Ans. by NTA (A)

QuestPix Ans. (A)

Sol. I . Better packing efficiency of monocarboxylic acids with even number of carbon atoms results in higher M.P

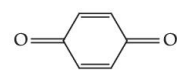
II. As molar mass increases hydrophobic part size increase hence solubility decreases.

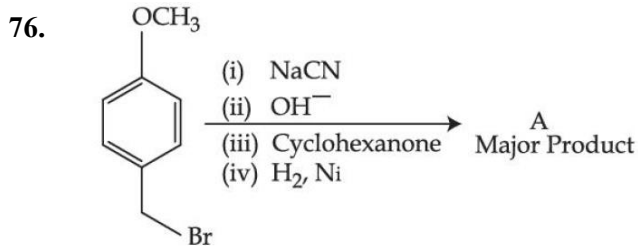
75. Which of the following is an example of conjugated diketone?



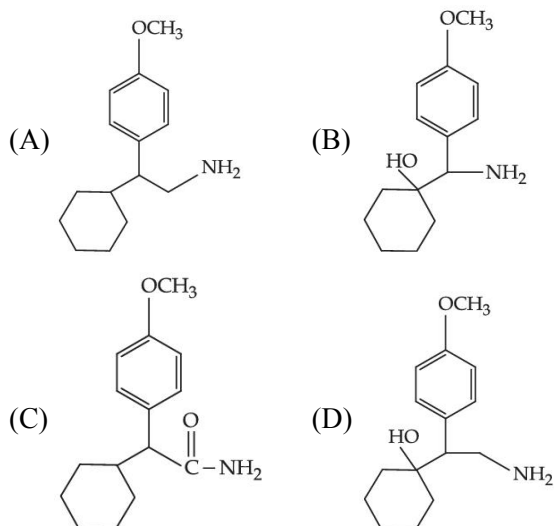
Official Ans. by NTA (C)

QuestPix Ans. (C)

Sol.  is a conjugated diketone



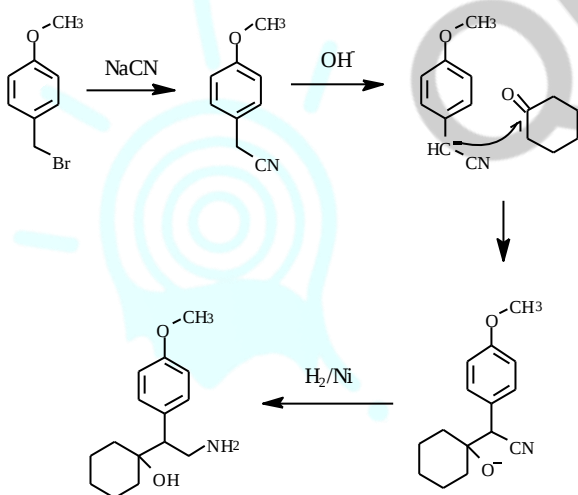
The major product of the above reaction is



Official Ans. by NTA (D)

QuestPix Ans. (D)

Sol.



77. Which of the following is an example of polyester?

- (A) Butadiene-styrene copolymer
 (B) Melamine polymer
 (C) Neoprene
 (D) Poly- β -hydroxybutyrate-co- β -hydroxy valerate

Official Ans. by NTA (D)

QuestPix Ans. (D)

Sol. Factual

78. A polysaccharide 'X' on boiling with dil H_2SO_4 at 393 K under 2-3 atm pressure yields 'Y'.

'Y' on treatment with bromine water gives gluconic acid. 'X' contains β -glycosidic linkages only.

Compound 'X' is :

- (A) starch (B) cellulose
 (C) amylose (D) amylopectin

Official Ans. by NTA (B)

QuestPix Ans. (B)

Sol. Cellulose contains β - glycosidic linkages only

79. Which of the following is not a broad spectrum antibiotic?

- (A) Vancomycin (B) Ampicillin
 (C) Ofloxacin (D) Penicillin G

Official Ans. by NTA (D)

QuestPix Ans. (D)

Sol. Penicillin G following is a narrow spectrum antibiotic

80. During the qualitative analysis of salt with cation y^{2+} , addition of a reagent (X) to alkaline solution of the salt gives a bright red precipitate. The reagent (X) and the cation (y^{2+}) present respectively are:

- (A) Dimethylglyoxime and Ni^{2+}
 (B) Dimethylglyoxime and Co^{2+}
 (C) Nessler's reagent and Hg^{2+}
 (D) Nessler's reagent and Ni^{2+}

Official Ans. by NTA (A)

QuestPix Ans. (A)

Sol. $\text{Ni}^{2+} + \text{DMG}^- \rightarrow [\text{Ni}(\text{DMG})_2] \downarrow$
 (Bright red precipitate)

SECTION-B

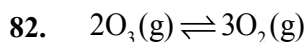
81. Atoms of element X form hcp lattice and those of element Y occupy $\frac{2}{3}$ of its tetrahedral voids. The percentage of element X in the lattice is _____
 (Nearest integer)

Official Ans. by NTA (43)

QuestPix Ans. (43)

Sol. $X \rightarrow 6$ $Y \rightarrow \frac{2}{3} \times 2 \times 6 = 8$

$$\% X = \frac{6}{14} \times 100 = 42.8 \simeq 43\%$$

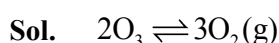


At 300 K, ozone is fifty percent dissociated. The standard free energy change at this temperature and 1 atm pressure is (–) ___ J mol^{–1} (Nearest integer)

[Given: $\ln 1.35 = 0.3$ and $R = 8.3 \text{ J K}^{-1} \text{ mol}^{-1}$]

Official Ans. by NTA (747)

QuestPix Ans. (747)



$$\frac{2}{5} \quad \frac{3}{5}$$

$$K_p = \frac{P_{O_2}^3}{P_{O_3}^2}$$

$$K_p = 1.35$$

$$\Delta G^\circ = -RT \ln K_p$$

$$= -8.3 \times 300 \times \ln 1.35$$

$$= -747 \text{ J/mol}$$

83. The osmotic pressure of blood is 7.47 bar at 300 K. To inject glucose to a patient intravenously, it has to be isotonic with blood. The concentration of glucose solution in gL^{–1} is ____ (Molar mass of glucose = 180 g mol^{–1})

$$R = 0.083 \text{ L bar K}^{-1} \text{ mol}^{-1} \text{ (Nearest integer)}$$

Official Ans. by NTA (54)

QuestPix Ans. (54)

Sol. $\pi = C.R.T$

$$7.47 = C \times 0.083 \times 300$$

$$C = 0.3 \text{ M}$$

$$= 0.3 \times 180 \text{ gL}^{-1}$$

$$= 54 \text{ gL}^{-1}$$

84. The cell potential for the following cell

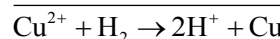
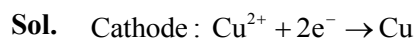
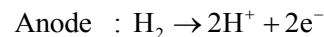


is 0.576 V at 298 K. The pH of the solution is ____.

(Nearest integer)

Official Ans. by NTA (5)

QuestPix Ans. (5)

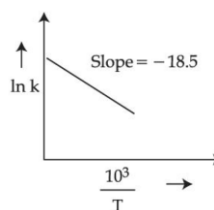


$$E_{\text{cell}} = E_{\text{cell}}^0 - \frac{0.06}{2} \log \frac{[H^+]^2}{[Cu^{2+}]}$$

$$0.576 = 0.34 - \frac{0.06}{2} \log \left\{ \frac{[H^+]^2}{(0.01)} \right\}$$

$$+ 3.93 - \log(H^+) + \log 0.1 \Rightarrow \text{pH} = 4.93 \simeq 5$$

85. The rate constants for decomposition of acetaldehyde have been measured over the temperature range 700–1000 K. The data has been analysed by plotting $\ln k$ vs $\frac{10^3}{T}$ graph. The value of activation energy for the reaction is ___ kJ mol^{–1}. (Nearest integer) (Given : $R = 8.31 \text{ J K}^{-1} \text{ mol}^{-1}$)



Official Ans. by NTA (154)

QuestPix Ans. (154)

Sol. $\ln k = \ln A - \frac{E_a}{10^3 RT} \times 10^3 = \ln A + \frac{10^3}{T} \left[-\frac{E_a}{10^3 RT} \right]$

From the graph

$$\frac{-E_a}{10^3 \times R} = -18.5$$

$$E_a = 153.735 \text{ kJ/mol}$$

$$\sim 154$$

86. The difference in oxidation state of chromium in chromate and dichromate salts is ____

Official Ans. by NTA (0)

QuestPix Ans. (0)

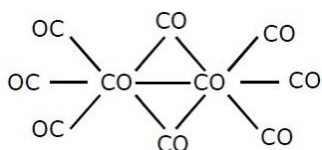
Sol. CrO_4^{2-} , $\text{Cr}_2\text{O}_7^{2-}$ difference is zero

87. In the cobalt-carbonyl complex: $[\text{Co}_2(\text{CO})_8]$, number of Co-Co bonds is "X" and terminal CO ligands is "Y". $X + Y =$ _____

Official Ans. by NTA (7)

QuestPix Ans. (7)

Sol.



$$X = 1$$

$$Y = 6$$

88. A 0.166 g sample of an organic compound was digested with cone. H_2SO_4 and then distilled with NaOH. The ammonia gas evolved was passed through 50.0 mL of 0.5 N H_2SO_4 . The used acid required 30.0 mL of 0.25 N NaOH for complete neutralization. The mass percentage of nitrogen in the organic compound is _____.

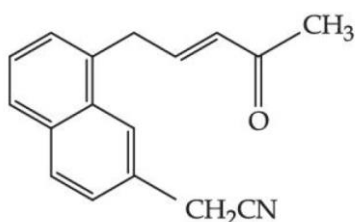
Official Ans. by NTA (63)

QuestPix Ans. (Bonus)

Sol. m_{eq} of NaOH used = 30×0.25
 m_{eq} of H_2SO_4 taken = 50×0.5
 $\therefore m_{\text{eq}}$ of H_2SO_4 used
 $= 50 \times 0.25 \times 30 \times 0.25 = 17.5 \text{ m mol of NH}_3$
 $\therefore \% \text{ N} = \frac{17.5 \times 10^{-3} \times 14}{0.166} \times 100 = 147.59\%$

(Not possible)

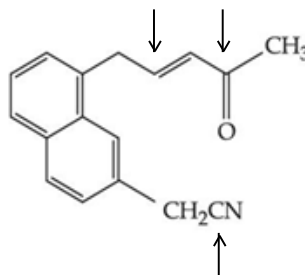
89. Number of electrophilic centre in the given compound is _____



Official Ans. by NTA (3)

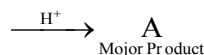
QuestPix Ans. (3)

Sol.



90. The major product 'A' of the following given reaction has _____ sp^2 hybridized carbon atoms.

2,7 - Dimethyl - 2, 6 - octadiene



Official Ans. by NTA (2)

QuestPix Ans. (2)

Sol. Answer (2)

