

(HELD ON FRIDAY 24th JANUARY 2025)

	MATHEMATICS	
	SECTION-A	
1.	The equation of the chord, of the ellipse	
	$\frac{2}{25} + \frac{y}{16}$ 1, whose mid-point is (3,1) is :	
	(1) $48x + 25y = 169$ (2) $4x + 122y = 134$	
	$(3) 25x + 101y = 176 \qquad (4) 5x + 16y = 31$	
Ans.	(1)	
Sol.	Equation of chord with given middle point	
	$T = S_1$	
	$\Rightarrow \frac{3x}{25} + \frac{y}{16} - 1 = \frac{9}{25} + \frac{1}{16} - \frac{9}{16} + \frac{1}{16} + + $	
	48x + 25y = 144 + 25	
	48x + 25y = 169 Ans.	
2.	The function $f : (-\infty, \infty) \to (-\infty, 1)$, defined by	
	$f(x) = \frac{2^{x}}{x^{x} + 2^{-x}}$ is :	
	(1) One-one but not onto	
	(2) Onto but not one-one	
	(3) Both one-one and onto	
	(4) Neither one-one nor onto	
Ans.	(1)	
Sol.	$f(x) = \frac{2^{2x} - \frac{1}{2^{2x} + \frac{1}{2^{2x$	
	$=1-\frac{2}{2^{2x}+}$	
	f'(x) = $\frac{2}{(2^{2x} + 1)^2}$.2.2 ^{2x} .ln2 i.e always +ve	
	so $f(x)$ is \uparrow function	
	\therefore f($-\infty$) = -1	
	$f(\infty) = 1$	

TIME : 3:00 PM TO 6:00 PM

TEST PAPER WITH SOLUTION

∴ $f(x) \in (-1, 1) \neq$ co-domain so function is one-one but not onto

3. If
$$\alpha > \beta > \gamma > 0$$
, then the expression

$$\cot^{-1}\left\{\beta + \frac{(1+\beta^2)}{(\alpha-\beta)}\right\} + \cot^{-1}\left\{\gamma + \frac{(1+\gamma^2)}{(\beta-\gamma)}\right\}$$
$$+ \cot^{-1}\left\{\alpha + \frac{(1+\alpha^2)}{(\gamma-\alpha)}\right\} \text{ is equal to:}$$
$$(1) \ \frac{\pi}{2} - (\alpha+\beta+\gamma) \qquad (2) \ 3\pi$$

(3) 0 (4)
$$\pi$$

Ans. (4)

Sol.
$$\Rightarrow \cot^{-1}\left(\frac{\alpha\beta+1}{\alpha-\beta}\right) + \cot^{-1}\left(\frac{\beta\gamma+1}{\beta-\gamma}\right) + \cot^{-1}\left(\frac{\alpha\gamma+1}{\gamma-\alpha}\right)$$
$$\Rightarrow \tan^{-1}\left(\frac{\alpha-\beta}{1+\alpha\beta}\right) + \tan^{-1}\left(\frac{\beta-\gamma}{1+\beta\gamma}\right) + \pi + \tan^{-1}\left(\frac{\gamma-\alpha}{1+\gamma\alpha}\right)$$
$$\Rightarrow (\tan^{-1}\alpha - \tan^{-1}\beta) + (\tan^{-1}\beta - \tan^{-1}\gamma) + (\pi + \tan^{-1}\gamma - \tan^{-1}\alpha)$$
$$\Rightarrow \pi$$

4. Let $f : (0, \infty) \rightarrow \mathbf{R}$ be a function which is differentiable at all points of its domain and satisfies the condition $x^2 f'(x) = 2xf(x) + 3$, with f(1) = 4. Then 2f(2) is equal to: (1) 29 (2) 19 (3) 39 (4) 23 Ans. (3)

Sol.
$$x^{2}f'(x) - 2x f(x) = 3$$

$$\left|\frac{x^{2}f'(x) - 2xf(x)}{(x^{2})^{2}}\right| = \frac{3}{()}$$
$$\Rightarrow \frac{d}{dx} \left(\frac{f(x)}{2} = \frac{1}{x}\right)$$

Integrating both sides

$$\frac{f(x)}{2} = -\frac{1}{x} + C$$
$$f(x) = -\frac{1}{x} + Cx^{2}$$
$$put x = 1$$

Questpix

6.

Final JEE-Main Exam January, 2025/24-01-2025/Evening Session

 $4 = -1 + C \implies C = 5$ $f(x) = -\frac{1}{x} + 5x^2$ Now $2 \times f(2) = 2 \times \left| -\frac{1}{2} + 5 \times 2^2 \right|$ = 39 5. Let $A = \left\{ x \in (0, \pi) - \left\{ \frac{\pi}{2} \right\} : \log_{(2/\pi)} \left| \sin x \right| + \log_{(2/\pi)} \left| \cos x \right| = 2 \right\}$ and $\mathbf{B} = \left\{ x \ge 0 : \sqrt{x} (\sqrt{x} - 4) - 3 \left| \sqrt{x} - 2 \right| + 6 = 0 \right\}.$ Then $n(A \cup B)$ is equal to: (1)4(2) 2(3) 8(4) 6Ans. (3) **Sol.** A : $\log_{2\pi} |\sin x| + \log_{2\pi} |\cos x| = 2$ $\Rightarrow \log_{2\pi} (|\text{sinx} \cdot \text{cosx}|) = 2$ $\Rightarrow |\sin 2x| = \frac{8}{-2}$ $\pi/2$ π Number of solution 4 B : let $\sqrt{x} = t < 2$ Then $\sqrt{x}(\sqrt{x}-4)+3(\sqrt{x}-2)+6=0$ \Rightarrow t² - 4t + 3t - 6 + 6 = 0 \Rightarrow t² - t = 0, t = 0, t = 1 x = 0, x = 1again let $\sqrt{x} = t > 2$ then $t^2 - 4t - 3t + 6 + 6 = 0$ \Rightarrow t² - 7t + 12 = 0 \Rightarrow t = 3, 4 x = 9, 16Total number of solutions $n(A \cup B) = 4 + 4 = 8$

Let the position vectors of three vertices of a be $4\vec{p} + \vec{q} - 3\vec{r}, -5\vec{p} + \vec{q} + 2\vec{r}$ triangle and $2\vec{p} - \vec{q} + 2\vec{r}$. If the position vectors of the orthocenter and the circumcenter of the triangle are $\frac{\vec{p} + \vec{q} + \vec{r}}{4}$ and $\alpha \vec{p} + \beta \vec{q} + \gamma \vec{r}$ respectively, then $\alpha + 2\beta + 5\gamma$ is equal to: (1)3(2)1(3) 6(4) 4Ans. (1) We know that Sol. O (orthocentre) $\frac{\vec{p} + \vec{q} + \vec{r}}{4}$ C (circum centre) $\alpha \vec{p} + \beta \vec{q} + \gamma \vec{r}$ C (centroid) = $\frac{\vec{p} + \vec{q} + \vec{r}}{2}$ by relation $\Rightarrow 2\left(\alpha \vec{p} + \beta \vec{q} + \gamma \vec{r}\right) + \frac{\vec{p} + \vec{q} + \vec{r}}{4} = 3\left(\frac{\vec{p} + \vec{q} + \vec{r}}{4}\right)$ $\Rightarrow 8(\alpha \vec{p} + \beta \vec{q} + \gamma \vec{r}) = 3(\vec{p} + \vec{q} + \vec{r})$ $\Rightarrow 8\alpha = 3, 8\beta = 3, 8\gamma = 3$ $\alpha = \frac{3}{2}, \beta = \frac{3}{2}, \gamma = \frac{3}{2}$ $\therefore \alpha + 2\beta + 3\gamma$ $\frac{3}{6} + \frac{6}{6} + \frac{15}{8} = \frac{24}{8} = 3$ Let [x] denote the gereatest integer function, and

- 7. let m and n respectively be the numbers of the points, where the function f(x) = [x] + |x - 2|, -2 < x < 3, is not continuous and not differentiable. Then m + n is equal to:
 - (2)9(1) 6
 - (3) 8(4)7



Ans. (3)

Sol. f(x) = [x] + |x - 2| -2 < x < 3

$$f(x) = \begin{cases} -x, & -2 < x < -1 \\ -x + 1, & -1 \le x < 0 \\ -x + 2, & 0 \le x < 1 \\ -x + 3, & 1 \le x < 2 \\ x, & 2 \le x < 3 \end{cases}$$

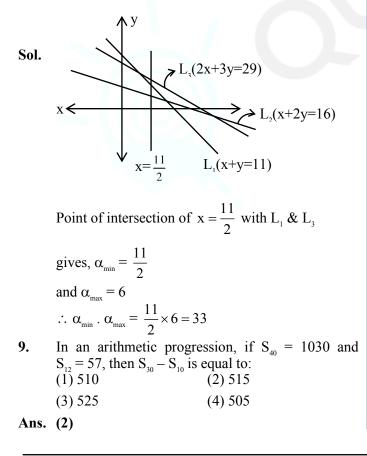
So f(x) is not continuous at 4 points and not differentiable at 4 point

So m + n = 4 + 4 = 8

8. Let the points $\left(\frac{11}{2}, \alpha\right)$ lie on or inside the triangle with sides x + y = 11, x + 2y = 16 and 2x + 3y = 29. Then the product of the smallest and the largest values of α is equal to :

(1) 22	(2) 44
(3) 33	(4) 55

Ans. (3)



Sol. Let a & d are first term and common diff of an AP.

$$S_{40} = \frac{40}{2} [2a + 39d] = 1030 \qquad \dots (1)$$

$$S_{12} = \frac{12}{2} [2a + 11d] = 57 \qquad \dots (2)$$

by (1) & (2)

$$a = -\frac{7}{2} \qquad d = \frac{3}{2}$$

$$\therefore S_{30} - S_{10} = \frac{30}{2} [2a + 29d] - \frac{10}{2} [2a + 9d]$$

$$= 20a - 390d$$

$$= 515$$

10. If
$$7 = 5 + \frac{1}{7}(5 + \alpha) + \frac{1}{7^2}(5 + 2\alpha) + \frac{1}{7^3}(5 + 3\alpha) + \frac{1}{7^3}(5 + 3\alpha)$$

...... ∞ , then the value of α is:

(1) 1
(2)
$$\frac{6}{7}$$

(3) 6
(4) $\frac{1}{7}$

Ans. (3)

Sol. Let
$$S = 5 + \frac{1}{7} (5 + \alpha) + \frac{1}{7^2} (5 + 2\alpha) + ...$$

 $\frac{1}{7}S = \frac{1}{7}(5) + \frac{1}{7^2}(5 + \alpha) + ... \infty$
 $\frac{6}{7}(\) = 5 + \frac{1}{7}\alpha \Big| \frac{1}{1 - \frac{1}{7}} \Big|$
 $6 = 5 + \frac{\alpha}{6} \Rightarrow \alpha = 6$
11. If the system of equations
 $x + 2y - 3z = 2$
 $2x + \lambda y + 5z = 5$
 $14x + 3y + \mu z = 33$
has infinitely many solutions, then $\lambda + \mu$ is equal
to:
(1) 13 (2) 10

(3) 11 (4) 12

Ans. (4)



in

is

Sol.
$$D = \begin{vmatrix} 1 & 2 & -3 \\ 2 & \lambda & 5 \\ 14 & 3 & \mu \end{vmatrix} = 0, \lambda\mu + 42\lambda - 4\mu + 107 = 0$$

$$D_{1} = 2\lambda\mu + 99\lambda - 10\mu + 255$$

$$D_{2} = 13 - \mu$$

$$D_{3} = 5\lambda + 5$$

$$D_{2} = 0 \Rightarrow \mu = 13 \& D_{3} = 0 \Rightarrow \lambda = -1$$

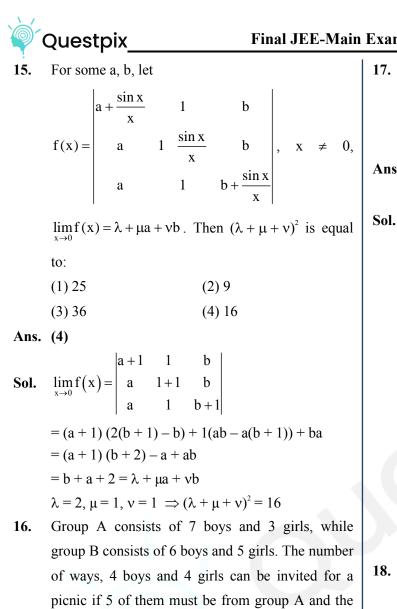
check & verify for these values D & D_{2} = 0
12. Let (2, 3) be the largest open interval in which the
function $f(x) = 2 \log_{x}(x - 2) - x^{2} + ax + 1$ is strictly
increasing and (b, c) be the largest open interval, in
which the function $g(x) = (x - 1)^{3}(x + 2 - a)^{2}$ is
strictly decreasing. Then $100(a + b - c)$ is equal to:
(1) 280 (2) 360
(3) 420 (4) 160
Ans. (2)
Sol. $f'(x) = \frac{2}{x - 2} - 2x + a \ge 0$
 $f''(x) \downarrow$
 $f'(3) \ge 0$
 $2 - 6 + a \ge 0$
 $a \ge 4$
 $a_{min} = 4$
 $g(x) = (x - 1)^{3} (x + 2 - a)^{2}$
 $g'(x) = (x - 1)^{3} (x - 2)^{2}$
 $g'(x) = (x - 1)^{3} (x - 2)^{2}$
 $g'(x) = (x - 1)^{3} (2x - 2) + (x - 2)^{2} 3(x - 1)^{2}$
 $= (x - 1)^{2} (x - 2) (5x - 8) < 0$
 $x \in \frac{8}{5}, 2$
 $100(a + b - c) = 100 \left(4 + \frac{8}{5} - 1\right) = 360$

Suppose A and B are the coefficients of 30th and 13. 12th terms respectively in the binomial expansion of $(1 + x)^{2n-1}$. If 2A = 5B, then n is equal to: (1) 22(2) 21(3) 20(4) 19

Ans. (2) Sol. $A = {}^{2n-1}C_{29} \quad B = {}^{2n-1}C_{11}$ $2 \; {}^{2n-1}C_{29} = 5 \; {}^{2n-1}C_{11}$ $2\frac{(2n-1)!}{29!(2n-30)!} = 5\frac{(2n-1)!}{(2n-12)!11!}$ $\frac{1}{29...12 \cdot 5} = \frac{1}{(2n-12)(2n-13)...(2n-29)2}$ $\frac{1}{30 \cdot 29 \dots 12} = \frac{1}{(2n-12)(2n-13)\dots(2n-29)12}$ 2n - 12 = 30n = 21 Let $\vec{a} = 3\hat{i} - \hat{j} + 2\hat{k}$, $\vec{b} = \vec{a} \times (\hat{i} - 2\hat{k})$ and $\vec{c} = \vec{b} \times \hat{k}$. 14.

Then the projection of $\vec{c} - 2\hat{j}$ on \vec{a} is:

(1) $3\sqrt{7}$ (2) $\sqrt{14}$ (3) $2\sqrt{14}$ (4) $2\sqrt{7}$ Ans. (3) **Sol.** $\vec{b} = \vec{a} \times (\hat{i} - 3\hat{k})$ $=\begin{vmatrix}\hat{i} & \hat{j} & \hat{k} \\ 3 & -1 & 2 \\ 1 & 0 & -2\end{vmatrix} = 2\hat{i} + 8\hat{j} + \hat{k}$ $\vec{c} = \vec{b} \times \hat{k} = 8\hat{i} - 2\hat{j}$ $\vec{c} - 2\hat{j} = 8\hat{i} - 4\hat{j}$ Projection of $(\hat{i} - 2\hat{j})$ on \vec{a} $(\vec{c}-2\hat{j})\hat{a} = \frac{\langle 8,-4,0\rangle,\langle 3,1,2\rangle}{\sqrt{14}}$ $=\frac{28}{\sqrt{14}}$ $2\sqrt{14}$



(1) 8575	(2) 9100
(3) 8925	(4) 8750

remaining 3 from group B, is equal to:

Ans. (3)

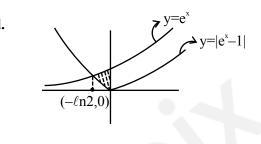
Sol.

	(7B,3G)	6B,5G	
	\mathbf{I}	↓ ▼	
	5	3	
C-I	(3G & 2B) &	& (1G & 2B)	
C-II	(2G & 3B) &	& (2G & 1B)	
C-III	(1G & 4B) &	& (3G & 0B)	
Total = C-I	+ C-II -	+ C-III	
$= {}^{7}C_{2} \cdot {}^{3}C_{3} \cdot {}^{6}C_{3}$	$C_2 \cdot {}^5C_1 + {}^7C_3 \cdot {}^3C_4$	$C_2 \cdot {}^6C_1 \cdot {}^5C_2 + {}^7C_4 \cdot {}^3$	$C_1 \cdot {}^6C_0 \cdot {}^5C_3$
= 8925			

17. The area of the region enclosed by the curves $y = e^x$, $y = |e^x - 1|$ and y-axis is: (1) $1 + \log_e 2$ (2) $\log_e 2$ (3) $2 \log_e 2 - 1$ (4) $1 - \log_e 2$

ns (1)

Ans. (4)



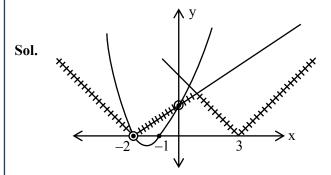
For Area $\int_{-\ell_{n2}}^{0} \left[e \left(1 - e^{x} \right) \right] dx$

$$\int_{-\ell_{n2}}^{0} (2e^{x} - 1) dx = \left[2e^{x} - x \right]_{-\ell_{n2}}^{0}$$

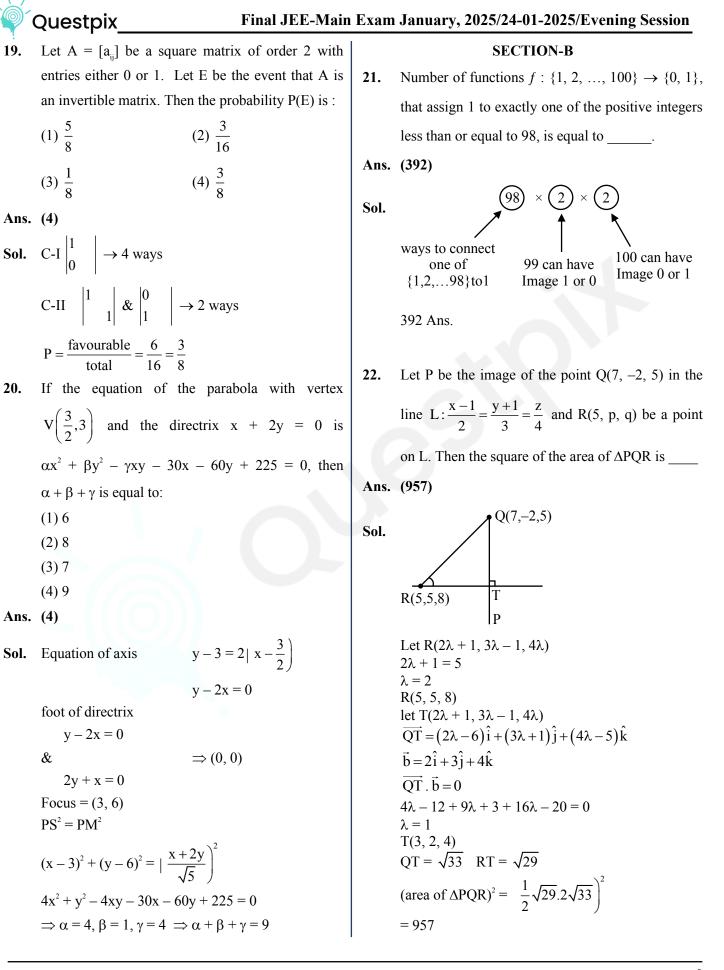
$$= (2 - (1 + \ell n2))$$

$$= 1 - \ell n^2$$

18. The number of real solution(s) of the equation $x^{2} + 3x + 2 = \min\{|x - 3|, |x + 2|\}$ is : (1) 2 (2) 0 (3) 3 (4) 1 Ans. (1)



Only 2 solutions.





Let y = y(x) be the solution of the differential 23. equation 2 $\cos \frac{dy}{dx} = \sin 2x - 4y \sin x, x \in \left(0, \frac{\pi}{2}\right).$ If $y\left(\frac{\pi}{3}\right) = -$, then $y'\left(\frac{\pi}{4}\right) + y\left(\frac{\pi}{2}\right)$ is equal to _____. Ans. (1) **Sol.** $\frac{dy}{dx} + 2y \tan x = \sin x$ $I.F. = e^{2\int \tan x \, dx} = \sec^2 x$ $ysec^2 x = \int \frac{\sin x}{\cos^2 x} dx$ $=\int \tan x \sec x \, dx$ = secx + C C = -2 $y = \cos x - 2\cos^2 x$ $y\left(\frac{\pi}{4}\right) = \frac{1}{\sqrt{2}} - 1$ $y' = -\sin x + 4\cos x \sin x$ $y'\left(\frac{\pi}{4}\right) = -\frac{1}{\sqrt{2}} +$ $y'\left(\frac{\pi}{4}\right) + y\left(\frac{\pi}{2}\right) = 1$ Let $H_1: \frac{x^2}{a^2} - \frac{1}{1}$ and $H_2: -\frac{x^2}{A^2} + \frac{1}{1} = 1$ be two 24. hyperbolas having length of latus rectums $15\sqrt{2}$ and $12\sqrt{5}$ respectively. Let their eccentricities be $e_1 = \sqrt{\frac{5}{2}}$ and e_2 respectively. If the product of the lengths of their transverse axes is $100\sqrt{10}$, then $25e_2^2$ is equal to _____

Ans. (55)
Sol.
$$\frac{2b^2}{2} = 1$$

bl.
$$\frac{2b^2}{a} = 15\sqrt{2}$$

 $1 + \frac{b^2}{a^2} = \frac{1}{2}$

a =
$$5\sqrt{2}$$

b = $5\sqrt{3}$
 $\frac{2A^2}{B} = 12\sqrt{5}$
2a.2B = $100\sqrt{10}$
2. $5\sqrt{2}.2B = 100\sqrt{10}$
B = $5\sqrt{5}$
A = $5\sqrt{6}$
 $\frac{2}{2} = 1 + \frac{A^2}{B^2}$
 $= 1 + \frac{150}{125}$
 $e_2^2 = 1 + \frac{30}{25}$
 $25e_2^2 = 55$
25. If $\int \frac{2x^2 + 5x + 9}{\sqrt{x^2 + x + 1}} dx = x\sqrt{x^2 + x + 1} + \alpha\sqrt{x^2 + x + 1} + \beta \log_e \left| x + \frac{1}{2} + \sqrt{x^2 + x + 1} \right| + C$, where C is the constant of integration, then $\alpha + 2\beta$ is equal to _____

Ans. (16)
Sol.
$$2x^2 + 5x + 9 = A(x^2 + x + 1) + B(2x + 1) + C$$

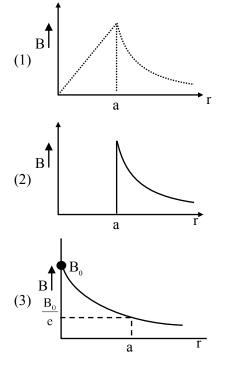
 $A = 2$ $B = \frac{3}{2}$ $C = \frac{11}{2}$
 $2\int \sqrt{x^2 + x + 1} \, dx + \frac{3}{2} \int \frac{2x + 1}{\sqrt{x + x + 1}} \, dx + \frac{11}{2} \int \frac{dx}{\sqrt{x^2 + x + 1}}$
 $2\sqrt{x + \frac{1}{2}} + \left(\frac{\sqrt{3}}{2}\right)^2 \, dx + 3\sqrt{x^2 + x + 1} + \frac{11}{2} \int \frac{dx}{\sqrt{x + \frac{1}{2}}} + \left(\frac{\sqrt{3}}{2}\right)^2 \, dx + 3\sqrt{x^2 + x + 1} + \frac{11}{2} \int \frac{dx}{\sqrt{x + \frac{1}{2}}} + \left(\frac{\sqrt{3}}{2}\right)^2 \, dx + 3\sqrt{x^2 + x + 1} + \frac{11}{2} \int \frac{dx}{\sqrt{x + \frac{1}{2}}} + \left(\frac{\sqrt{3}}{2}\right)^2 \, dx + 3\sqrt{x^2 + x + 1} + \frac{11}{2} \int \frac{dx}{\sqrt{x^2 + x + 1}} + \frac{3}{8} \ln \left(x + \frac{1}{2} + \sqrt{x^2 + x + 1}\right) + 3\sqrt{x^2 + x + 1} + \frac{11}{2} \ln \left(x + \frac{1}{2} + \sqrt{x^2 + x + 1}\right) + C$
 $a = \frac{7}{2}$ $\beta = \frac{25}{4}$
 $a + 2\beta = 16$

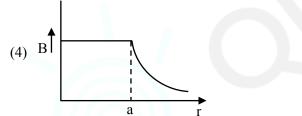


(HELD ON FRIDAY 24 th JANUARY 2025)			TIME: 3:00 PM TO 6:00 PM
	PHYSICS		TEST PAPER WITH SOLUTION
26. Ans. Sol. 27.	SECTION-A Young's double slit interference apparatus is immersed in a liquid of refractive index 1.44. It has slit separation of 1.5mm. The slits are illuminated by a parallel beam of light whose wavelength in air is 690 nm. The fringe-width on a screen placed behind the plane of slits at a distance of 0.72m, will be : (1) 0.23 mm (2) 0.33 mm (3) 0.63 mm (4) 0.46 mm (1) $\beta = \left(\frac{\lambda_0}{\mu}\right) \times \frac{D}{d} = \frac{690 \times 10^{-9} \ 0.72}{1.44 \times 1.5 \times 10^{-3}} = 0.23 \text{ mm}$ Arrange the following in the ascending order of wavelength (λ) : (A) Microwaves (λ_1) (B) Ultraviolet rays (λ_2) (C) Infrared rays (λ_3) (D) X-rays (λ_4) Choose the most appropriate answer from the options given below :- (1) $\lambda_4 < \lambda_3 < \lambda_2 < \lambda_1$ (2) $\lambda_3 < \lambda_4 < \lambda_2 < \lambda_1$ (3) $\lambda_4 < \lambda_2 < \lambda_3 < \lambda_1 < \lambda_2$	28. Ans. Sol. 29.	$\overline{F} = q(\overline{v} \times \overline{B})$ $\overline{F} = 0$ $\overline{V} \overline{B}$ $\theta = 0 \text{ or } 180$ A solid sphere is rolling without slipping on a horizontal plane. The ratio of the linear kinetic energy of the centre of mass of the sphere and rotational kinetic energy is : (1) $\frac{2}{5}$ (2) $\frac{5}{2}$ (3) $\frac{3}{4}$ (4) $\frac{4}{3}$ (2) Linear KE $-\frac{1}{2}mv_{cm}^2$
Ans. Sol.	(3) $ \frac{\gamma - rays}{\gamma - rays} X - rays U.V Visible IR Micro Radio waves waves}{rays} x - rays Visible Radio waves waves} \longrightarrow \lambda^{\uparrow} $	Sol.	$\overline{\text{Rotational K.E}} = \frac{2}{\frac{1}{2}I\omega^2}$ $\frac{\text{mv}_{cm}^2}{\frac{2}{5}\text{mR}^2\omega} = \frac{5}{2} \qquad (\text{V} = \omega \text{ R})$



30. A long straight wire of a circular cross-section with radius 'a' carries a steady current I. The current I is a uniformly distributed across this cross-section. The plot of magnitude of magnetic field B with distance r from the centre of the wire is given by





Ans. (1)

Sol.

$$B_{in} = \frac{\mu_0 \left(\overline{J} \times \overline{r}\right)}{2}$$

$$B_{in} \propto$$

$$B_{out} = \frac{\mu_0 I}{2\pi r}$$

$$B_{net} \propto \frac{1}{r}$$

ΛI

31. Given below are two statements. One is labelled as Assertion (A) and the other is labelled as Reason(R).

Assertion (A) : In an insulated container, a gas is adiabatically shrunk to half of its initial volume. The temperature of the gas decreases.

Reason (R) : Free expansion of an ideal gas is an irreversible and an adiabatic process.

In the light of the above statement, choose the **correct** answer from the options given below :

(1) Both (A) and (R) are true and (R) is the correct explanation of (A)

(2) (A) is true but (R) is false

(3) (A) is false but (R) is true

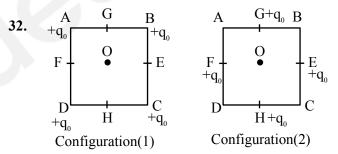
(4) Both (A) and (R) are true but (R) is NOT the correct explanation of (A)

Ans. (3)

Sol. (A) $T_1 V_1^{\gamma - 1} = T_2 V_2^{\gamma - 1}$

Temp increases

R) Free expansion is assumed fast, so Adiabatic



In the first configuration (1) as shown in the figure, four identical charges (q_0) are kept at the corners A,B,C and D of square of side length 'a'. In the second configuration (2), the same charges are shifted to mid points G,E,H and F, of the square, If

 $K = \frac{1}{4\pi_0}$, the difference between the potential

energies of configuration (2) and (1) is given by :

(1)
$$\frac{\mathrm{Kq}_{0}^{2}}{\mathrm{a}} \left(4\sqrt{2} - 2 \right)$$
 (2) $\frac{\mathrm{Kq}_{0}^{2}}{\mathrm{a}} \left(3 - \sqrt{2} \right)$
(3) $\frac{\mathrm{Kq}_{0}^{2}}{\mathrm{a}} \left(4 - 2\sqrt{2} \right)$ (4) $\frac{\mathrm{Kq}_{0}^{2}}{\mathrm{a}} \left(3\sqrt{2} - 2 \right)$

Ans. (4)



- Sol. $U_{1} = \frac{4Kq_{0}^{2}}{a} + \frac{2Kq_{0}^{2}}{\sqrt{2}a} = \frac{Kq_{0}^{2}}{a} \left(4 + \sqrt{2}\right)$ $U_{2} = \frac{Kq_{0}^{2}}{\left(\frac{a}{\sqrt{2}}\right)} \left(4 + \sqrt{2}\right) = \frac{Kq_{0}^{2}}{a} \left(4\sqrt{2} + 2\right)$ $U_{2} U_{1} = \frac{Kq_{0}^{2}}{a} \left(3\sqrt{2} 2\right)$
- 33. The position vector of a moving body at any instant of time is given as $\vec{r} = (5t^2\hat{i} 5t\hat{j})m$. The magnitude and direction of velocity at t = 2s is,
 - (1) $5\sqrt{15}$ m/s, making an angle of tan⁻¹ 4 with -ve Y axis
 - (2) $5\sqrt{15}$ m/s, making an angle of tan⁻¹ 4 with +ve X axis
 - (3) $5\sqrt{17}$ m/s, making an angle of tan⁻¹ 4 with -ve Y axis
 - (4) $5\sqrt{17}$ m/s, making an angle of tan⁻¹ 4 with +ve X axis

Ans. (3)

Sol.
$$\vec{r} = 5t^2\hat{i} - 5t\hat{j}$$

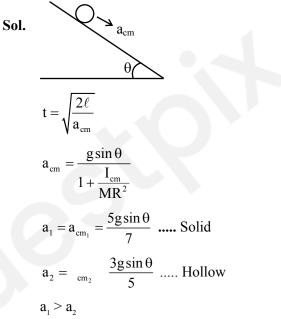
 $\vec{v} = 10t\hat{i} - 5\hat{j}$
 $\vec{v} = 20\hat{i} - 5\hat{j}$ at $t = 2sec$
 \hat{j}
 $v_x = 20\hat{i}$
 $v_y = -5\hat{j}$
 $tan \theta = \frac{20}{5} = 4$
 $\theta = tan^{-1} 4$
From -veY-axis

34. A solid sphere and a hollow sphere of the same mass and of same radius are rolled on an inclined plane. Let the time taken to reach the bottom by the solid sphere and the hollow sphere be t_1 and t_2 , respectively, then

(1)
$$t_1 < t_2$$

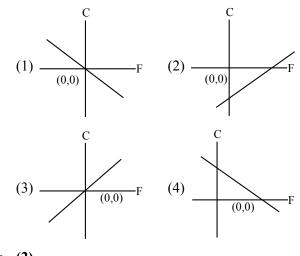
(2) $t_1 = t_2$
(3) $t_1 = 2t_2$
(4) $t_1 > t_2$

Ans. (1)

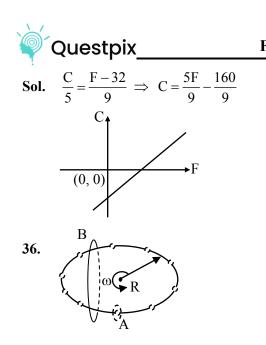


$$t_1 < t_2$$

35. Which of the following figure represents the relation between Celsius and Fahrenheit temperatures?



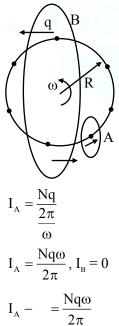
Ans. (2)



N equally spaced charges each of value q, are placed on a circle of radius R. The circle rotates about its axis with an angular velocity ω as shown in the figure. A bigger Amperian loop B encloses the whole circle where as a smaller Amperian loop A encloses a small segment. The difference between enclosed currents, $I_A - I_B$, for the given Amperian loops is

(1)
$$\frac{N^2}{2\pi} q\omega$$
 (2) $\frac{2\pi}{N} q\omega$
(3) $\frac{N}{2\pi} q\omega$ (4) $\frac{N}{\pi} q\omega$

Ans. (3) Sol.



- Final JEE-Main Exam January, 2025/24-01-2025/Evening Session
 - **37.** In photoelectric effect, the stopping potential (V_0) v/s frequency (v) curve is plotted.

(h is the Planck's constant and ϕ_0 is work function of metal)

(A) $V_0 v/s v$ is linear

- (B) The slope of V₀ v/s v curve = $\frac{\phi_0}{h}$
- (C) h constant is related to the slope of $V_{_0} \ v/s \ \nu$ line
- (D) The value of electric charge of electron is not required to determine h using the V_0 v/s v curve.
- (E) The work function can be estimated without knowing the value of h.

Choose the **correct** answer from the options given below :

(1) (A),(B) and (C) only

- (2)(C) and (D) only
- (3) (A),(C) and (E) only
- (4) (D) and (E) only

Ans. (3)

Sol.
$$hv = \phi + KE_{max}$$

$$KE_{max} = eV_0$$
$$V_0 = \frac{hv - \phi}{hv - \phi}$$

$$v_0 = \frac{1}{e}$$

(A) $V_0 v/s V$ is linear correct

(B) Slope

$$v_0 = \left(\frac{h}{e}\right) - \frac{\phi}{e}$$
 Wrong

Slope
$$\frac{h}{e}$$

(C) Correct

(D) Incorrect

(E) Correct

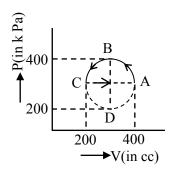


Sol.

40.

Sol.

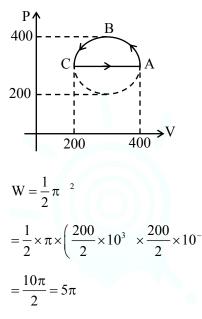
The magnitude of heat exchanged by a system for 38. the given cyclic process ABCA (as shown in figure) is (in SI unit)



(1) 10π (2) 5π (3) zero (4) 40π

Ans. (2)

Sol.



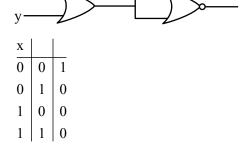
A photograph of a landscape is captured by a drone 39. camera at a height of 18 km. The size of the camera film is 2 cm \times 2 cm and the area of the landscape photographed is 400 km². The focal length of the lens in the drone camera is :

> (1) 1.8 cm (2) 2.8 cm

(3) 2.5 cm (4) 0.9 cm

Ans. (1)

 $(2 \times 2) \times 10^{-4} m^2$ Lens 18cm Х $400 \times 10^6 \text{m}^2$ H = 18 kmSize of camera film = 2cm \times 2cm $A_{image} = 400 \text{ km}^2$ $x = 20 \times 10^3 \text{ m} = 2 \times 10^4 \text{ m}$ $y = 2 \times 10^{-2} m$ $\frac{x}{x} = 10^6 = \frac{18Km}{f}$ $f = 18 \times 10^{-3} m = 18 mm$ f = 1.8 cmThe output of the circuit is low (zero) for : X (A) X = 0, Y = 0(B) X = 0, Y = 1(D) X = 1, Y = 1(C) X = 1, Y = 0Choose the **correct** answer from the options given below : (1) (A), (C) and (D) only (2) (A), (B) and (C) only (3) (B), (C) and (D) only (4) (A), (B) and (D) only Ans. (3) v





41. The temperature of a body in air falls from 40°C to 24°C in 4 minutes. The temperature of the air is 16°C. The temperature of the body in the next 4 minutes will be :

(1)
$$\frac{14}{3}$$
 °C
(2) $\frac{28}{3}$ °C
(3) $\frac{56}{3}$ °C
(4) $\frac{42}{3}$ °C

Ans. (3)

Sol.
$$\frac{T_2 - T_1}{t} = K \Big[T_{avg} - T_s \Big]$$
$$T_1 = 24^{\circ}C; T_2 = 40^{\circ}C, t = 4, T_s = 16^{\circ}C$$
$$\frac{40 - 24}{4} = K \Big[32 - 16 \Big]$$
$$K == \frac{4}{16} = \frac{1}{4}$$
$$Now \ \frac{24 - T}{4} = K \Big[\frac{T - 24}{2} - 16 \Big]$$
$$24 - T = \frac{T - 16}{2} + 16$$
$$\frac{3T}{2} = 28$$
$$T = \frac{56}{3}$$

42. The energy E and momentum p of a moving body of mass m are related by some equation. Given that c represents the speed of light, identify the correct equation.

(1)
$$E^2 = pc^2 + m^2c^4$$
 (2) $E^2 = pc^2 + m^2c^2$
(3) $E^2 = p^2c^2 + m^2c^2$ (4) $E^2 = p^2c^2 + m^2c^4$

Ans. (4)

Sol. [E] =
$$M^{1}L^{2}T^{-2}$$

[Pc] = $M^{1}L^{1}T^{-1}$. $L^{1}T^{-1} = M^{1}L^{2}T^{-2}$
[mc²] = $M^{1}L^{2}T^{-2}$
 $E^{2} = M^{1}L^{2}T^{-2}$
 $E^{2} = P^{2}c^{2} + m^{2}c^{4}$

43. A small uncharged conducting sphere is placed in contact with an identical sphere but having 4×10^{-8} C charge and then removed to a distance such that the force of repulsion between them is 9×10^{-3} N. The distance between them is (Take as $4\pi\varepsilon_0$ $9 \times 10^{\circ}$ in SI units) $(1) 2 \, \text{cm}$ (2) 3 cm (3) 4 cm(4) 1 cm Ans. (1) $Q = 4 \times 10^{-8}$ Q/2 Q/2 Sol. Q/2 Q/2 $9 \times 10 \times (4 \times 10^{-8}) \times 4 \times 10^{-10}$

$$9 \times 10^{-3} \quad \frac{9 \times 10^{-3} \times (4 \times 10^{-3}) \times 4 \times 10^{-3}}{4 \times r^2}$$
$$r^2 = \frac{9 \times 10^9 \times 16 \times 10^{-16}}{4 \times 9 \times 10^{-3}} = 4 \times 10^{-3}$$
$$r = 2 \times 10^{-2} \text{ m} \implies 2 \text{ cm}$$

44. A particle oscillates along the x-axis according to the law, $x(t) = x_0 \sin^2\left(\frac{t}{2}\right)$ where $x_0 = 1$ m. The kinetic energy (K) of the particle as a function of x



Sol.
$$x = x_0 \sin^2 \frac{t}{2}$$
 $x_0 \left(\frac{1 - \cos t}{2}\right)$
 $x - \frac{x_0}{2} = \frac{-\cos t}{2}$
where $x_0 = 1$
 $x - \frac{1}{2} = \frac{-\cos t}{2}$

Particle is oscillating between x = 0 to x = 1

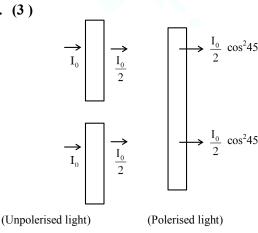
45. In a Young's double slit experiment, three polarizers are kept as shown in the figure. The transmission axes of P_1 and P_2 are orthogonal to each other. The polarizer P₃ covers both the slits with its transmission axis at 45° to those of P₁ and P_{2} . An unpolarized light of wavelength λ and intensity $\mathbf{I}_{_{0}}$ is incident on $\mathbf{P}_{_{1}}$ and $\mathbf{P}_{_{2}}$. The intensity at a point after P₃ where the path difference between the light waves from s_1 and s_2 is $\frac{\lambda}{3}$, is

(1)
$$\frac{I_0}{2}$$
 (2) $\frac{I_0}{4}$
(3) I_0 (4) $\frac{I_0}{3}$

Ans. (3)

Sol.

(



after passing through third poleriser, Intensity of

both the waves must be
$$\frac{I_0}{4}$$

now, at a point where path diff is $\frac{\lambda}{3}$, phase difference

$$\Delta \phi = 2K \left(\frac{\Delta x}{\lambda}\right) = \frac{2\pi}{3}$$
$$\therefore I_{res} = \sqrt{\left(\frac{I_0}{4}\right)^2 + \left(\frac{I_0}{4}\right)^2 + 2\left(\frac{I_0}{4}\right)^2} \cos \frac{2\pi}{3}$$
$$= \frac{I_0}{4}$$

A tightly wound long solenoid carries a current of 46. 1.5 A. An electron is executing uniform circular motion inside the solenoid with a time period of 75ns. The number of turns per metre in the solenoid is

> [Take mass of electron $m_e = 9 \times 10^{-31}$ kg, charge of electron $|q_e| = 1.6 \times 10^{-19}$ C,

$$\mu_0 = 4\pi \times 10^{-7} \ \frac{N}{A^2}$$
, 1 ns = 10⁻⁹ s]

Ans. (250)

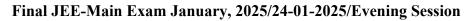
Since time period of a revolving charge is $\frac{2\pi m}{r}$ Sol.

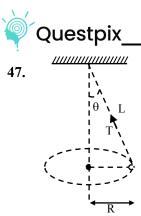
> Where B = magnetic field due to a solenoid = $\mu_0 nI$

$$\therefore T = \frac{2\pi m}{q(\mu_0 nI)}$$

$$75 \times 10^{-9} = \frac{(2\pi)(9 - 10^{-31})}{1.6 \times 10^{-19} \times 4\pi \times 10^{-7} \times n \times 1.5}$$

$$N = 250$$

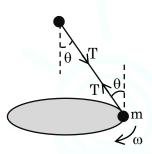




A string of length L is fixed at one end and carries a mass of M at the other end. The mass makes $\left(\frac{3}{\pi}\right)$ rotations per second about the vertical axis passing through end of the string as shown. The tension in the string is _____ ML.

Ans. (36)

Sol.



- $T \cos \theta = mg \qquad \dots (1)$
- $T\sin\theta = M\omega^2 R \qquad \dots (2)$

Using equation (2)

 $T\sin\theta = M\omega^2(L\sin\theta)$

$$T = M\omega^{2}L = M \left| \frac{3}{\pi} \times 2\pi \right|^{2} L$$

T = 36 ML

48. The ratio of the power of a light source S_1 to that the light source S_2 is 2. S_1 is emitting 2 × 10¹⁵ photons per second at 600 nm. If the wavelength of the source S_2 is 300 nm, then the number of photons per second emitted by S_2 is____×10¹⁴.

Ans. (5)

$$= \frac{\text{Total energy emitted}}{\text{time}}$$
$$= \frac{(E_1 \text{ photon}) \times \text{Number of photons(N)}}{t}$$
$$P_1 = (E_1)n$$
$$\frac{P_1}{P_2} = \frac{(E_1)n_1}{(E_2)n_2} = \frac{\left(\frac{hC}{\lambda_1}\right)n_1}{\left(\frac{hC}{\lambda_2}\right)n_2}$$
$$-\frac{1}{2} = \left(\frac{\lambda_2}{\lambda_1}\right)\frac{n_1}{n_2}$$

Substituting the given values

2
$$\frac{300}{600}$$
 $\times \frac{2 \times 10^{15}}{n_2}$
 $n_2 = \frac{1}{2} \times 10^{15} = 5 \times 10^{14}$ Photon/sec

49. The increase in pressure required to decrease the volume of a water sample by 0.2% is $P \times 10^5 Nm^{-2}$. Bulk modulus of water is $2.15 \times 10^9 Nm^{-2}$. The value of P is _____.

Ans. (43)

Sol. Since bulk modulus is given as

$$B = \frac{-\Delta P}{\left(\frac{\Delta V}{V}\right)}$$

$$2.15 \times 10^9 \quad \frac{-\Delta P}{-\frac{0.2}{100}}$$

$$\Delta P = 2.15 \times 10^9 \times 2 \times 10^{-3}$$

$$= 4.3 \times 10^6 = 43 \times 10^5 \text{ N/m}^2$$



50. Acceleration due to gravity on the surface of earth is 'g'. If the diameter of earth is reduced to one third of its original value and mass remains unchanged, then the acceleration due to gravity on the surface of the earth is ____g.

Ans. (9)

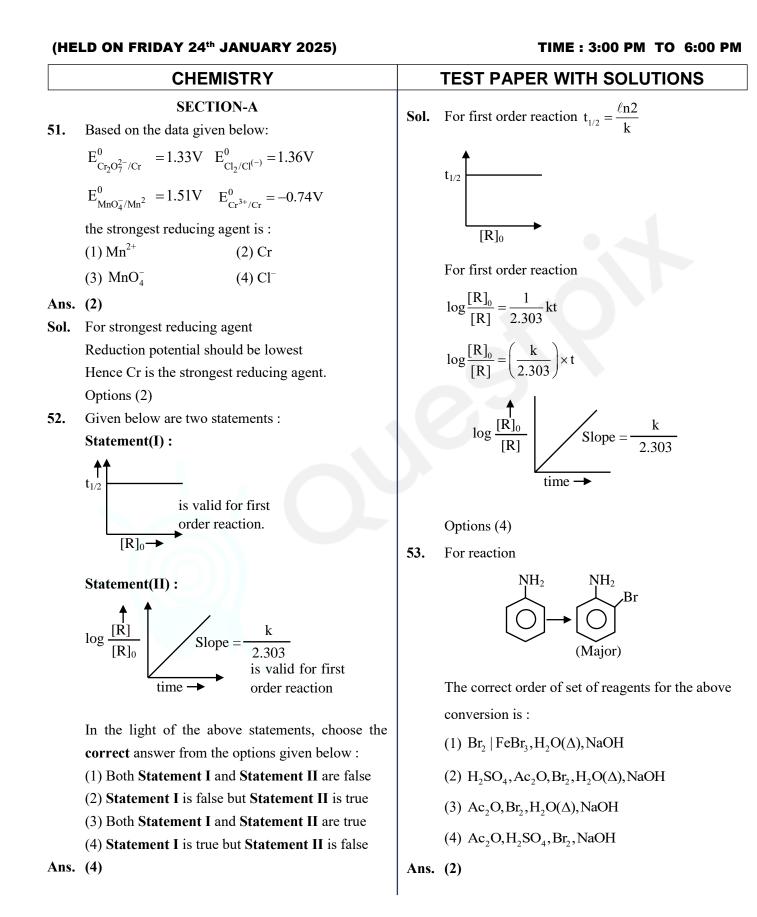
Sol. ∵ acceleration due to gravity on surface is given by

$$g = \frac{GM}{R_e^2}$$

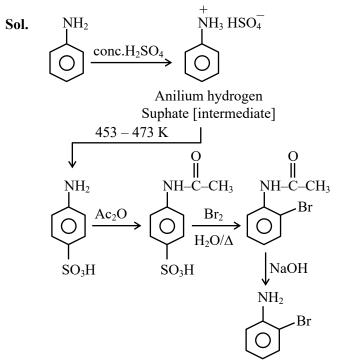
Now since diameter is reduced to $1/3^{rd}$, radius also reduces to $1/3^{rd}$, keeping mass constant New value of acceleration due to gravity on Earth's surface is

$$g' = \frac{GM}{\left(\frac{R_e}{3}\right)^2} = 9\frac{GMe}{R_e^2} = 9g$$









- **54.** For hydrogen atom, the orbital/s with lowest energy is/are :
 - (A) 4s
 - (B) 3p_x
 - (C) $3d_{x v^2}$
 - (D) $3d_{r^2}$
 - (E) 4p_z

Choose the **correct** answer from the options given below :

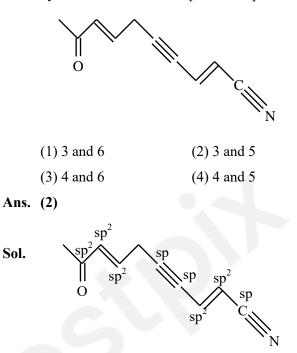
- (1) (A) and (E) only
- (2) (B) only
- (3)(A) only
- (4) (B), (C) and (D) only

Ans. (4)

Sol. In hydrogen atom the orbitals in a shell are degenerate means energy depends only on 'n'

 $\therefore E_{3p_x} = E_{3d_{x^2-y^2}} E_{3d_{z^2}}$

55. In the given structure, number of sp and sp² hybridized carbon atoms present respectively are :



Number of sp and sp^2 hybridised carbon atom are 3 and 5.

- **56.** Which of the following mixing of 1M base and 1M acid leads to the largest increase in temperature?
 - (1) 30 mL HCl and 30 mL NaOH
 - (2) 30 mL CH₃COOH and 30 mL NaOH
 - (3) 50 mL HCl and 20 mL NaOH
 - (4) 45 mL CH₃COOH and 25 mL NaOH

Ans. (1)

Sol. Higher the number of milli moles of acid or base reacted higher will be temperature rise.

Option (4) n_{acid} or n_{base} reacted = 30 m mol Option (2) n_{acid} or n_{base} reacted = 30 m mol but less energy will be released by neutralisation reaction of weak acid hence option (2) can not be correct.

Option (3) \Rightarrow 20 m mol Option (4) \Rightarrow 25 m mol

Hence Correct Option (1)

57. Given below are two statements :

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Statement(I) : Experimentally determined oxygen-oxygen bond lengths in the O_3 are found to be same and the bond length is greater than that of a O = O (double bond) but less than that of a single (O - O) bond.

Statement (II) : The strong lone pair-lone pair repulsion between oxygen atoms is solely responsible for the fact that the bond length in ozone is smaller than that of a double bond (O=O) but more than that of a single bond (O - O).

In the light of the above statements, choose the **correct** answer from the options given below:

(1) Statement I is true but Statement II is false

(2) Both Statement I and Statement II are true

(3) Both Statement I and Statement II are false

(4) Statement I is false but Statement II is true

- Ans. (1)
- Sol. Due to resonance bond length is identical in ozone. Therefore statement I is true and statement II is false
- **58.** Find the compound 'A' from the following reaction sequences.

$$A \xrightarrow{aqua-regia} B \xrightarrow{(1)KNO_2|NH_4OH} yellow ppt$$
(1) ZnS
(2) CoS
(3) MnS
(4) Nis
Ans. (2)

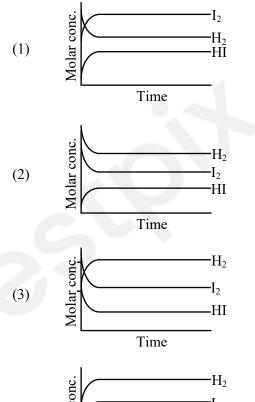
Sol. $\operatorname{CoS} \xrightarrow{\operatorname{Aquaregia}} \operatorname{CoCl}_2 \xrightarrow{1.\mathrm{KNO}_2/\mathrm{NH}_4\mathrm{OH}} \xrightarrow{2.\mathrm{AcOH}}$

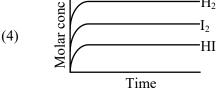
 $K_3[Co(NO_2)_6] \downarrow$ yellow

59. For the reaction,

 $H_2(g) + I_2(g) \Longrightarrow 2HI(g)$

Attainment of equilibrium is predicted correctly by:





Ans. (2)

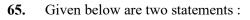
Sol. $H_2 + I \rightleftharpoons 2HI$

Concentration of H_2 and I_2 decreases untill equilibrium condition and concentration of HI increases till equilibrium condition and after equilibrium concentration of all the reactant and products remain constant.

Correct option (2)

Final JEE-Main Exam January, 2025/24-01-2025/Evening Session

60.	Match List-I with List-II.		62. When Ethane-1,2-diamine is added progressively
	List-I	List-II	to an aqueous solution of Nickel (II) chloride, the
	(Transition metal ion)	(Spin only magnetic	sequence of colour change observed will be :
		moment (B.M.))	(1) Pale Blue \rightarrow Blue \rightarrow Green \rightarrow Violet
	(A) Ti ³⁺	(I) 3.87	(2) Pale Blue \rightarrow Blue \rightarrow Violet \rightarrow Green
	(B) V^{2+}	(II) 0.00	(3) Green \rightarrow Pale Blue \rightarrow Blue \rightarrow Violet
	(C) Ni ²⁺	(III) 1.73	(4) Violet \rightarrow Blue \rightarrow Pale Blue \rightarrow Green
	(D) Sc^{3+}	(IV) 2.84	Ans. (3)
	Choose the correct answ	wer from the options given	Sol.
	below :		$[\text{Ni}(\text{H}_{2}\text{O})_{6}]^{+2}_{(aq)} + \text{en}_{(aq)} \rightarrow [\text{Ni}(\text{H}_{2}\text{O})_{4}(\text{en})]^{+2}_{(aq)} + 2\text{H}_{2}\text{O}$
	(1) (A)-(III), (B)-(I), (C)	-(II), (D)-(IV)	Green
	(2) (A)-(III), (B)-(I), (C)		$[Ni(H_2O)_4(en)]^{+2}_{(aq)} + en_{(aq)} \rightarrow [Ni(H_2O)_2(en)_2]^{+2}_{(aq)} + 2H_2O$
	(3) (A)-(IV), (B)-(II), (C		Pale Blue
	(4) (A)-(II), (B)-(IV), (C		$[Ni(H_2O)_2(en)]^{+2}_{(aq)} + en_{(aq)} \rightarrow [Ni(en)_3]^{+2}_{(aq)} + 2H_2O$
Ans.			Blue / purple
	$\mathrm{Sc}^{+3} = 3\mathrm{d}^{\mathrm{o}}$	$\therefore \mu_{\rm spin} = 0$	63. The conditions and consequence that favours the
	$V^{+2} = 3d^3$	$\therefore \mu_{\rm spin} = 3.87 \text{ B.M.}$	t_{2g}^{3} , e_{g}^{1} configuration in a metal complex are :
	$Ni^{+2} = 3d^8$	$\therefore \ \mu_{\rm spin} = 2.84 \text{ B.M.}$	(1) weak field ligand, high spin complex
	$Ti^{+3} = 3d^1 \therefore \mu_{spin} = 1.$		(2) strong field ligand, high spin complex
51.			(3) strong field ligand, low spin complex
1.	-	ition of a compound is 6.6% O. If the malar mass	(4) weak field ligand, low spin complex Ans. (1)
		6.6% O. If the molar mass 2 g mol ^{-1} , the molecular	Sol. For $3d^4$
	formula of the compound	-	If ligand is SFL : $t_{2g}^4 e_g^0$ (Low spin)
	1	omic mass of $C : H : O =$	If ligand is WFL : $t_{2g}^{3} e_{g}^{-1}$ (High spin)
	-	office mass of $C \cdot H \cdot O =$	64. Identify correct statement/s :
	12:1:16]		(A) $-OCH_3$ and $-NHCOCH_3$ are activating
	(1) $C_4H_9O_3$	(2) $C_6H_{12}O_6$ (4) $C_4H_8O_2$	group
\ m a	(3) $C_6H_{12}O_3$	$(4) C_4 \Pi_8 O_2$	(B) — CN and — OH are meta directing group
ns.	• /	0	(C) —CN and —SO ₃ H are meta directing group
Sol.			(D) Activating groups act as ortho - and para
	$\frac{54.2}{12}$: 9.2 :	$\frac{36.6}{16}$	directing groups
			(E) Halides are activating groups
		2.287	Choose the correct answer from the options given
	$\frac{4.516}{2.287}$: $\frac{9.2}{2.287}$:	$\frac{2.287}{2.287}$	below :
			(1) (A), (C) and (D) only (2) (A) $(D) = 1$
	1.97 : 4.02 :		(2) (A), (B) and (E) only
	$C_2H_4O \Rightarrow$ Empirical formula E.F. mass = $24 + 4 + 16 = 44$		(3) (A) only $(4) (A) and (C) and (c)$
			(4) (A) and (C) only
	and molar mass $= 132$		Ans. (1) Sol. (B) –CN is meta directing But –OH is ortho / pera
	Hence molecular formula	$a = (C_2 H_4 O)_3$	
		$= C_6 H_{12} O_3$	directing.



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Statement (I) : The first ionization energy of Pb is greater than that of Sn

Statement(II) : The first ionization energy of Ge is greater than that of Si.

In the light of the above statements, choose the **correct** answer from the options given below :

(1) Statement I is true but Statement II is false

(2) Both Statement I and Statement II are false

(3) Statement I is false but Statement II is true

(4) Both Statement I and Statement II are true

```
Ans. (1)
```

Sol. Order of I.E. (in KJ/mol) :

- C > Si > Ge > Sn < Pb
- $1086 \ 786 \ 761 \ 708 \ 715$

66.
$$S(g) + \frac{3}{2} O_2(g) \rightarrow SO_3(g) + 2x \text{ kcal}$$

$$SO_2(g) + \frac{1}{2} O_2(g) \rightarrow SO_3(g) + y \text{ kcal}$$

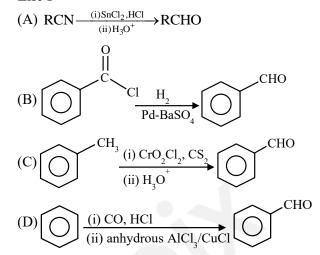
The heat of formation of $SO_2(g)$ is given by :

(1)
$$\frac{2x}{y}$$
 kcal
(2) y - 2x kcal
(3) 2x + y kcal
(4) x + y kcal

Ans. (2)

Sol.
$$SO_{2} + \frac{1}{2}O_{2} \longrightarrow SO_{3} \quad \Delta H = -y$$
$$\Delta H_{r} = (\Delta H_{f})_{SO_{3}} - (\Delta H_{f})_{SO}$$
$$-y = -2x - (\Delta H_{f})_{SO_{2}}$$
$$(\Delta H_{f})_{SO_{2}} = y - 2x$$
Option (2)

67. Match List-I with List-II List-I



List-II

(I) Etard reaction

(II) Gatterman -Koch reaction

(III) Rosenmund reduction

(IV) Stephen reaction

Choose the **correct** answer from the options given below :

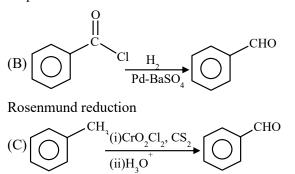
(A)-(IV), (B)-(III), (C)-(I), (D)-(II)
 (A)-(III), (B)-(IV), (C)-(II), (D)-(I)
 (A)-(I), (B)-(III), (C)-(II), (D)-(IV)
 (A)-(III), (B)-(IV), (C)-(I), (D)-(II)

Ans. (1)

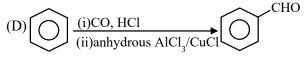
Sol. List-I

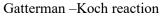
(A) RCN
$$\xrightarrow{(i)SnCl_2,HCl}$$
 RCHO

Stephen reaction



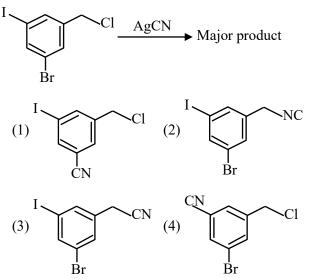
Etard reaction



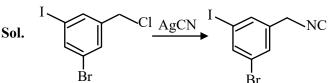




68. The structure of the major product formed in the following reaction is :



Ans. (2)



List-II

H₃C

(III)

١H

١H

Н

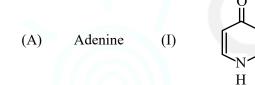
Η

 NH_2

NH₂

Н

69. Match List-I with List-II. List-I



- (B) Cytosine (II)
- (C) Thymine
- (D) Uracil (IV)

Choose the **correct** answer from the options given below :

(1) (A)-(III), (B)-(IV), (C)-(II), (D)-(I) (2) (A)-(III), (B)-(I), (C)-(IV), (D)-(II) (3) (A)-(IV), (B)-(III), (C)-(II), (D)-(I) (4) (A)-(III), (B)-(IV), (C)-(I), (D)-(II)



- (A) Adenine (III)(B) Cytosine (IV)
- H^{1}

١H

Н

 NH_2

Η

Thymine

(II)

- (D) Uracil (I)
- **70.** The successive 5 ionisation energies of an element are 800, 2427, 3658, 25024 and 32824 kJ/mol, respectively. By using the above values predict the group in which the above element is present :
 - (1) Group 2

(C)

- (2) Group 13
- (3) Group 4
- (4) Group 14

Ans. (2)

Sol. The IE_4 is suddenly very high therefore element must have 3 valence $e^{-}(s)$ and it belong to group 13



SECTION-B

- 71. The observed and normal masses of compound MX₂ are 65.6 and 164 respectively. The percent degree of ionisation of MX_2 is _____%. (Nearest integer)
- Ans. (75)
- **Sol.** $MX_2 \rightarrow M^{+2} + 2X^-$

i = <u>normal molar mass</u> observed molar mass

$$i = \frac{164}{65.6}$$

 $1 + (3 - 1)\alpha = \frac{164}{65.6}$

$$2\alpha = \frac{98.4}{65.6}$$

$$\alpha = 0.75$$

percent dissociation = 75%

Ans. 75

- 72. The possible number of stereoisomers for 5-phenylpent-4-en-2-ol is
- Ans. (4)
- Sol. Ph

n (stereogenic unit) = 2, $2^2 = 4$ stereoisomers are possible.

Consider a complex reaction taking place in three 73. steps with rate constants k_1 , k_2 and k_3 respectively. The overall rate constant k is given by the expression $k = \sqrt{\frac{k_1k}{k_2}}$ If the activation energies of the three steps are 60, 30 and 10 kJ mol^{-1} respectively, then the overall energy of activation in kJ mol⁻¹ is _____. (Nearest integer)

Ans. (20)

Sol.
$$K = \sqrt{\frac{K_1K_3}{K_2}}$$

 $A.e^{-Ea/RT} = \sqrt{\frac{A_1e^{-Ea_1/RT} \times A_3e^{-Ea_3/RT}}{A_2e^{-Ea_2/RT}}}$
By comparing exponential term
 $\frac{E_a}{RT} = \frac{1}{2} \times (\frac{RT}{RT} + \frac{E_{a_3}}{RT} - \frac{E_{a_2}}{RT})$
 $E_a = (E_{a_1} + E_{a_3} - E_{a_2})/2$
 $E_a = (60 + 10 - 30)/2 = 20 \text{ kJ mol}^{-1}$
Ans. 20
74. The hydrocarbon (X) with molar mass 80 g mol^{-1}
and 90% carbon has degree of
unsaturation.
Ans. (3)
Sol. Mass of carbon = $\frac{80 \times 90}{100} = 72 \text{ gm}$
Number of C-atoms = $\frac{72}{12} = 6$
Mass of hydrogen = $\frac{80 \times 10}{800} = 8 \text{ gm}$
Number of H-atoms = $\frac{8}{1} = 8$
So molecular formula C₆H₈
D.U. = $6 + 1 - 8/2 = 7 - 4 = 3$
75. In Carius method of estimation of halogen, 0.25 g
of an organic compound gave 0.15 g of silver
bromide (AgBr). The percentage of Bromine in the
organic compound is $\times 10^{-1}$ %

(Nearest integer). (Given : Molar mass of Ag is 108 and Br is 80 g mol^{-1})

Ans. (255)

Sol. % Bromine =
$$\frac{\text{Molar Mass of Bromine}}{\text{Molar Mass of Silver bromide}}$$
$$\times \frac{\text{Weight of AgBr}}{\text{Weight of sample}} \times 100$$
$$= \frac{80}{188} \times \frac{0.165}{0.25} \times 100$$
$$= \frac{4800}{188} = 25.53 = 255 \times 10^{-1}$$

of