

TIME : 3:00 PM TO 6:00 PM

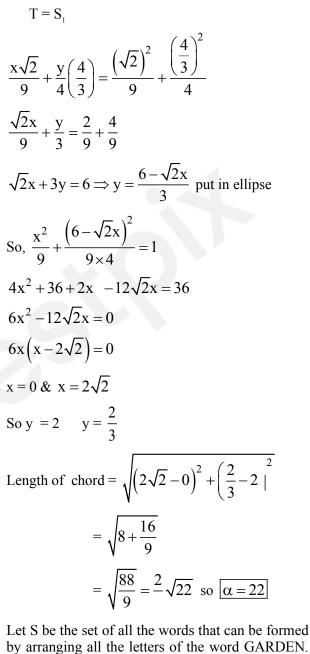
# (HELD ON TUESDAY 28th JANUARY 2025)

(TEED ON TOESDAT 20 SANDART 2023)			TIME : 5.00 FM TO 0.00 FM			
	MATHEMATICS		TEST PAPER WITH SOLUTION			
	SECTION-A	Sol.	Equation of angle bisector : $x - y = 0$			
1.	Bag $B_1$ contains 6 white and 4 blue balls, Bag $B_2$ contains 4 white and 6 blue balls, and Bag $B_3$ contains 5 white and 5 blue balls. One of the bags is selected at random and a ball is drawn from it. If the ball is white, then the probability, that the ball		$\left \frac{a(1-a)}{\sqrt{2}}\right  = \frac{9}{\sqrt{2}} \Longrightarrow a = 5 \text{ or } -4$ Sum = 5 + (-4) = 1			
	is drawn from Bag $B_2$ , is :	3.	If the components of $\vec{a} = \alpha \hat{i} + \beta \hat{j} + \gamma \hat{k}$ along and			
	(1) $\frac{1}{3}$ (2) $\frac{4}{15}$		perpendicular to $\vec{b} = 3\hat{i} + \hat{j} - \hat{k}$ respectively, are			
	(3) $\frac{2}{3}$ (4) $\frac{2}{5}$		$\frac{16}{11}(3\hat{i}+\hat{j}-\hat{k})$ and $\frac{1}{11}(-4\hat{i}-5\hat{j}-17\hat{k})$ , then			
Ans.	(2)		$\alpha^2 + \beta^2 + \gamma^2$ is equal to :			
Sol.	$E_1$ : Bag $B_1$ is selected		(1) 23 (2) 18			
	$\begin{array}{ccc} \mathbf{B}_1 & \mathbf{B}_2 & \mathbf{B}_3 \\ \mathbf{6W} \mathbf{4B} & \mathbf{4W} \mathbf{6B} & \mathbf{5W} \mathbf{5B} \end{array}$		(3) 16 (4) 26			
	E, : bag B, is selected	Ans.				
	$E_3$ : Bag B <sub>3</sub> is selected	Sol.	let			
	A : Drawn ball is white		$\vec{a}_{11}$ = component of $\vec{a}$ along $\vec{b}$			
	We have to find P $\frac{E_2}{A}$		$\vec{a}_1$ = component of $\vec{a}$ perpendicular to $\vec{b}$			
	$P\left(\frac{E_2}{A}\right) = \frac{P(E_2)P\left(\frac{A}{E_2}\right)}{P(E_1)P\left(\frac{A}{E_1}\right) + P(E_2)P\left(\frac{A}{E_2}\right) + P(E_3)P\left(\frac{A}{E_3}\right)}$		$\vec{a}_{11} = \frac{16}{11} \left( 3\hat{i} + \hat{j} - \hat{k} \right)$			
	1		$\vec{a}_1 = \frac{1}{11} \left( -4\hat{i} - 5\hat{j}  17\hat{k} \right)$			
	$=\frac{\frac{1}{3}\times\frac{1}{10}}{\frac{1}{1}\times\frac{6}{10}+\frac{1}{1}\times\frac{4}{10}+\frac{1}{1}\times\frac{5}{10}}=\frac{4}{15}$		$\therefore \vec{a} = \vec{a}_{11} + \vec{a}_1$			
2.	$\frac{1}{3} \times \frac{6}{10} + \frac{1}{3} \times \frac{4}{10} + \frac{1}{3} \times \frac{5}{10}$ Let A, B, C be three points in xy-plane, whose		$\therefore \vec{a} = \frac{16}{11} \left( 3\hat{i} + \hat{j} - \hat{k} \right) + \frac{1}{11} \left( -4\hat{i} - 5\hat{j} - 17\hat{k} \right)$			
2.	position vector are given by $\sqrt{3}\hat{i}+\hat{j}$ , $\hat{i}+\sqrt{3}\hat{j}$ and					
	$a\hat{i} + (1-a)\hat{j}$ respectively with respect to the origin O. If the distance of the point C from the line		$=\frac{44}{11}\hat{i}+\frac{11}{11}\hat{j}-\frac{33}{11}\hat{k}$			
	bisecting the angle between the vectors $\overrightarrow{OA}$ and					
	$\overrightarrow{OB}$ is $\frac{9}{\sqrt{2}}$ , then the sum of all the possible values		$\vec{a} = 4\hat{i} + \hat{j} - 3\hat{k}$			
	$\sqrt{2}$ of a is :		$\alpha = 4$ $\beta = 1$ $\gamma = -3$			
	(1) 1 (2) 9/2					
	(3) 0 (4) 2		$\alpha^2 + \beta^2 + \gamma^2 = 16 + 1 + 9 = 26$			
Ans.	(1)					
		1				



If m $\left(\sqrt{2}, \frac{4}{3}\right)$  than equation of AB is

4.	If $\alpha + i\beta$ and $\gamma + i\delta$ are the roots of		
	$x^{2} - (3-2i)x - (2i-2) = 0, i = 0$	$=\sqrt{-1}$ , then $\alpha\gamma + \beta\delta$ is	
	equal to :		
	(1) 6 (2	2) 2	
	(3) -2 (4	4) – 6	
Ans.	(2)		
Sol.	$x^2 - (3 - 2i)x - (2i - 2) = 0$		
	$(3-2i) \pm \sqrt{(3-2i)^2}$	-4(1)(-(2i-2))	
	$x = \frac{(3-2i) \pm \sqrt{(3-2i)^2}}{2(1)}$		
	$(3-2i)+\sqrt{9-4-1}$	$\frac{1}{2i+8i-8}$	
	$==\frac{(3-2i)\pm\sqrt{9-4-12i}}{2}$		
	$==\frac{3-2i\pm\sqrt{-3-4i}}{2}$		
	3 2i + $\sqrt{(1)^2 + (2i)^2}$	2(1)(2i)	
	$=\frac{3-2i\pm\sqrt{(1)^2+(2i)^2-2}}{2}$	2(1)(21)	
	$3-2i\pm(1-2i)$		
	$=\frac{3-2i\pm(1-2i)}{2}$		
	$\Rightarrow \frac{3-2i+1-2i}{2} \text{ or } \frac{3-2i}{2}$	i-1+2i	
	$\rightarrow \frac{2}{2}$ or $\frac{1}{2}$	2	
	$\Rightarrow 2 - 2i \text{ or } 1 + 0i$		
	So $\alpha\gamma + \beta\delta = 2(1) + (-2)(0)$	) = 2	
5.	If the midpoint of a	chord of the ellipse	
	$\frac{2}{9} + \frac{y}{1}$ is $(\sqrt{2}, 4/3)$ ,	and the length of the	
	chord is $\frac{2\sqrt{\alpha}}{3}$ , then $\alpha$ is :		
	2		
		2) 22	
	(3) 26 (4	4) 20	
Ans.	(2)		
Sol.			



6. Let S be the set of all the words that can be formed by arranging all the letters of the word GARDEN. From the set S, one word is selected at random. The probability that the selected word will NOT have vowels in alphabetical order is :

(1) 
$$\frac{1}{4}$$
 (2)  $\frac{2}{3}$   
(3)  $\frac{1}{3}$  (4)  $\frac{1}{2}$ 



A, E, G R D N Sol.

Probability (P) =  $\frac{\text{favourable case}}{\text{Total case}}$ 

(when A & E are in order) Total case = 6!Favourable case  $= {}^{6}C_{2} \cdot 4!$ 

$$P = \frac{(15)4!}{(30)4!}$$

Probablity when not in order =  $1 - \frac{1}{2} = \frac{1}{2}$ 

7. Let f be a real valued continuous function defined on the positive real axis such that  $g(x) = \int t f(t) dt$ .

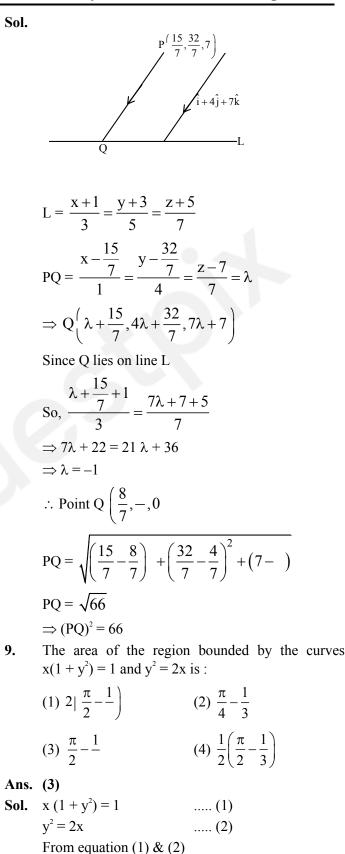
If $g(x^3) = x^6 + x^7$ ,	, then value of $\sum_{r=1}^{15} f(r^3)$ is :
(1) 320	(2) 340
(3) 270	(4) 310
<i></i>	

Ans. (4)

Sol. 
$$g(x) = x2 + x^{\frac{7}{3}}$$
  
 $g'(x) = 2x - \frac{7}{3}x^{\frac{4}{3}}$   
 $f(x) = \frac{g'(x)}{x}$   
 $f(x) = 2 + \frac{7}{3}x^{\frac{1}{3}}$   
 $f(r^3) = 2 + \frac{7r}{3}$   
 $\sum_{r=1}^{15} \left(1 + \frac{7}{3}r - 310\right)$   
8. The square of the distance of the filles.

point  $\left(\frac{15}{7}, \frac{32}{7}, 7\right)$ from the line  $\frac{x+1}{3} = \frac{y+3}{5} + \frac{z+5}{7}$  in the direction of the vector  $\hat{i} + 4\hat{j} + 7\hat{k}$  is : (1)54(2) 41(3) 66 (4) 44

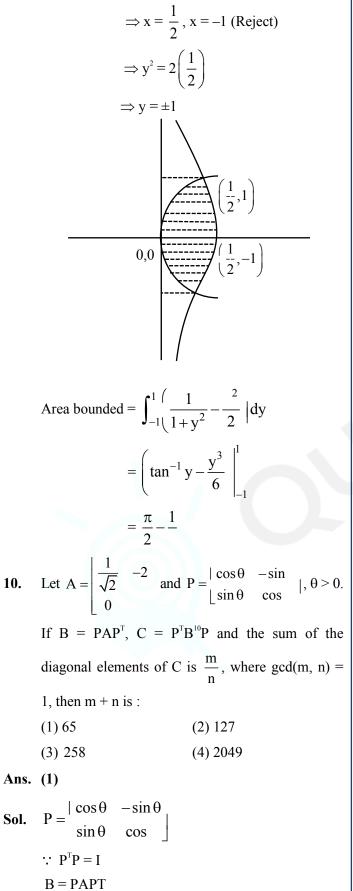
Ans. (3)



 $x (1+2x) = 1 \Longrightarrow 2x^2 + x - 1 = 0$ 

9.





Pre multiply by P<sup>T</sup> ( Given)  
P<sup>T</sup>B = P<sup>T</sup>P AP<sup>T</sup> = AP<sup>T</sup>  
Now post multiply by P  
P<sup>T</sup>BP = AP<sup>T</sup>P = A  
So 
$$A^2 = \underbrace{P^T BP P^T}_{I} BP$$
  
 $A^2 = P^T B^2 P$   
Similarly A<sup>10</sup> = P<sup>T</sup>B<sup>10</sup> P = C  
 $A = \begin{bmatrix} \frac{1}{\sqrt{2}} & -2\\ 0 & 1 \end{bmatrix}$  (Given)  
 $\Rightarrow A^2 = \begin{bmatrix} \frac{1}{2} & -\sqrt{2}\\ 0 & 1 \end{bmatrix}$  (Given)  
 $\Rightarrow A^2 = \begin{bmatrix} \frac{1}{2} & -\sqrt{2}\\ 0 & 1 \end{bmatrix}$  (Given)  
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 $\Rightarrow A^2 = \begin{bmatrix} \frac{1}{2} & -\sqrt{2}\\ 0 & 1 \end{bmatrix}$  (Given)  
 $\Rightarrow M^2 = \begin{bmatrix} \frac{1}{2} & -\sqrt{2}\\ 0 & 1 \end{bmatrix}$  (Given)  
 $\Rightarrow Sum of diagonal elements of C is  $\left(\frac{1}{\sqrt{2}}\right)^{10} + 1$   
 $= \frac{1}{32} + 1 = \frac{33}{32} = \frac{m}{n}$   
g cd(m,n) = 1 (Given)  
 $\Rightarrow m + n = 65$   
11. If  $f(x) = \int \frac{1}{x^{1/4}(1 + x^{1/4})} dx$ ,  $f(0) = -6$ , then  $f(1)$  is  
equal to :  
(1)  $\log_e 2 + 2$  (2)  $4(\log_e 2 - 2)$   
(3)  $2 - \log_e 2$  (4)  $4(\log_e 2 - 2)$   
(3)  $2 - \log_e 2$  (4)  $4(\log_e 2 + 2)$   
Ans. (1)  
Sol. let  $x = t^4$   
 $dx = 4t^3 dt$   
then  $\int \frac{1}{x^{\frac{1}{4}}\left(1 + x^{-1}} dx \Rightarrow \frac{4t^3 dt}{t(1 + t)}\right)$   
 $\Rightarrow \int \frac{4t}{1 + t} dt \Rightarrow 4 \frac{(t^2 - 1) + 1}{1 + t} dt$$ 

## Final JEE-Main Exam January, 2025/28-01-2025/Evening Session

Also

Questpix Final JEE-Main  

$$\Rightarrow 4\int (t-1) + \frac{1}{t+1} dt$$

$$\Rightarrow 4\left\{\frac{(t-1)^2}{2} + ln(t+1)\right\} + c$$
hence  $f(x) = 2\left(x^{\frac{1}{2}} - 1\right)^2 + 4ln\left(1 + x^{\frac{1}{4}}\right) + c$   
 $f(0) = -6 \Rightarrow 2 + 4ln + 6 = -6 \rightarrow C = -8$   
now  $f(1) = 4ln 2 - 8$   
 $= 4(ln 2 - 2)$   
12. Let  $f : R \rightarrow R$  be a twice differentiable function  
such that  $f(2) = 1$ . If  $F(x) = xf(x)$  for all  $x \in R$ ,  
 $\int_0^2 xF'(x)dx = 6$  and  $\int_0^2 x^2F''(x)dx = 40$ , then  
 $F'(2) + \int_0^2 F(x)dx$  is equal to :  
(1) 11 (2) 15  
(3) 9 (4) 13  
Ans. (2)  
Sol.  $\int_0^2 xF'(x)dx = 6$   
 $= xF(x)|_0^2 - \int_0^2 f(x)dx = 6$   
 $= 2F(2) - \int_0^2 xF(x)dx = 6 [\therefore f(2) = 2F(2) = 2]$   
 $\int_0^2 xF(x)dx = -2 \dots (1)$   
 $\Rightarrow \int_0^2 F(x)dx = -2 \dots (2)$ 

$$\begin{aligned} \int_{0}^{2} x^{2} F''(x) dx &= x^{2} F'(x) \Big|_{0}^{2} - 2 \int_{0}^{2} x F'(x) dx = 40 \\ &= 4F'(2) - 2 \times 6 = 40 \\ F'(2) &= 13 \\ \therefore F'(2) + \int_{0}^{2} F(x) = 13 - 2 = 11 \end{aligned}$$
13. For positive integers n, if  $4a_{n} = (n^{2} + 5n + 6)$  and  $S_{n} &= \sum_{k=1}^{n} \left(\frac{1}{a_{k}}\right)$ , then the value of 507  $S_{2025}$  is :  
(1) 540 (2) 1350 (3) 675 (4) 135   
Ans. (3)   
Sol.  $a_{n} = \frac{n^{2} + 5n + 6}{4} \\ S_{n} &= S_{n} = \sum_{k=1}^{n} \frac{1}{a_{k}} \sum_{l} \frac{4}{k^{2} + 5k} = 6 \\ &= 4 \sum_{k=1}^{n} \frac{1}{(k+2)(k+3)} \\ &= 4 \sum_{k=1}^{n} \frac{1}{k+2} - \frac{1}{k+3} \\ &= 4 |\frac{1}{3} - -| + 4| |\frac{1}{4} - -| + ...... \end{aligned}$ 

$$4\left(\frac{1}{n+2} - \frac{1}{n-3}\right)$$
$$= 4\left(\frac{1}{3} - \frac{1}{n+3}\right)$$
$$= \frac{4n}{3(n+3)}$$
$$^{507}S_{2025} = \frac{(507)(4)(2025)}{3(2028)}$$

= 2]

= 675

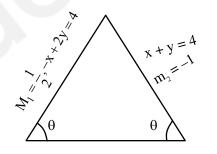


- Let  $f: [0, 3] \rightarrow A$  be defined by 14.  $f(x) = 2x^3 - 15x^2 + 36x + 7$  and  $g : [0, \infty) \to B$  be defined by  $g(x) = \frac{x^{2025}}{x^{2025} + 1}$ . If both the functions are onto and  $S = \{x \in \mathbb{Z} : x \in A \text{ or } x \in B\}$ , then n (S) is equal to : (1) 30(2) 36(3) 29(4) 31Ans. (1) as f(x) is onto hence A is range of f(x)Sol. now  $f'(x) = 6x^2 - 30x + 36$ = 6 (x-2) (x-3)f(2) = 16 - 60 + 72 + 7 = 35f(3) = 54 - 135 + 108 + 7 = 34f(0) = 7hence range  $\in [7,35] = A$ also for range of g(x) $g(x) = 1 - \frac{1}{x^{2025} + 1} \in [0, 1] = B$  $s = \{0, 7, 8, \dots, 35\}$  hence n(s) = 30Let [x] denote the greatest integer less than or 15. equal to x. Then domain of  $f(x) = \sec^{-1}(2[x]+1)$  is :  $(1) (-\infty, -1] \cup [0, \infty)$  $(2)(-\infty, -\infty)$  $(3) (-\infty, -1] \cup [1, \infty)$  $(4) (-\infty, \infty] - \{0\}$ Ans. (2) **Sol.**  $2[x] + 1 \le -1$  or  $2[x] + 1 \ge 1$  $\Rightarrow [x] \leq -1 \cup [x] \geq 0$  $\Rightarrow x \in (-\infty, 0) \cup x \in [0, \infty)$  $\Rightarrow x \in (-\infty, \infty)$ If  $\sum_{r=1}^{13} \frac{1}{\sin\left(\frac{\pi}{4} + (r-1)\frac{\pi}{6}\right)\sin\left(\frac{\pi}{4} + \frac{r\pi}{6}\right)} \left\{ a\sqrt{3} + b, \right\}$ 16.  $a, b \in \mathbb{Z}$ , then  $a^2 + b^2$  is equal to : (1) 10(2) 2(3) 8(4) 4Ans. (3)
- Sol.  $\frac{1}{\sin\frac{\pi}{6}} \sum_{r=1}^{13} \frac{\sin\left(\frac{\pi}{4} + \frac{r\pi}{6}\right) \left(\frac{\pi}{4}\right) (r-1)\frac{\pi}{6}}{\sin\left(\frac{\pi}{4} + \frac{r\pi}{6}\right)}$  $\frac{1}{\sin\frac{\pi}{6}} \sum_{r=1}^{13} \left(\cot\left(\frac{\pi}{4} + (r-1)\frac{\pi}{6}\right) \cot\left(\frac{\pi}{4} + \frac{r\pi}{6}\right)\right)$  $= 2\sqrt{3} 2 = \alpha\sqrt{3} + b$ So  $a^2 + b^2 = 8$ 
  - 17. Two equal sides of an isosceles triangle are along -x + 2y = 4 and x + y = 4. If m is the slope of its third side, then the sum, of all possible distinct values of m, is :

 $(4) - 2\sqrt{10}$ 

Ans. (3)

Sol.



$$\tan \theta \quad \frac{m - \frac{1}{2}}{1 + \frac{1}{2} \cdot m} = \frac{-1 - m}{1 - m} = \frac{m + 1}{m - 1}$$

$$\frac{2m-1}{2+m} = \frac{m+1}{m-1}$$
$$2m^2 - 3m + 1 = m^2 + 3m + 2$$

$$m^2 - 6m - 1 = 0$$

sum of root = 6

sum is 6

- Let the coefficients of three consecutive terms T<sub>r</sub>, 18.  $T_{r+1}$  and  $T_{r+2}$  in the binomial expansion of  $(a + b)^{12}$ be in a G.P. and let p be the number of all possible values of r. Let q be the sum of all rational terms in the binomial expansion of  $\left(\sqrt[4]{3} + \sqrt[3]{4}\right)^{12}$ . Then p + q is equal to : (1) 283(2) 295(3) 287 (4) 299Ans. (1) **Sol.**  $(a+b)^{\frac{1}{2}}$  $T_r, T_{r+1}, T_{r+2} \rightarrow GP$ So,  $\frac{T_{r+1}}{T_r} = \frac{T_{r+2}}{T_{r+1}}$  $\frac{{}^{12}C_{r}}{{}^{12}C_{r}} = \frac{{}^{12}C_{r+1}}{{}^{12}C_{r+1}}$  $\frac{12-r+1}{r} = \frac{12-(r+1)+1}{r+1}$ (13 - r)(r + 1) = (12 - r)(r) $-r + 12r + 13 = 12r - r^{2}$ 13 = 0No value of r possible So P = 0 $\left(3^{\frac{1}{4}} + 4^{\frac{1}{3}}\right)^{12} = \sum{}^{12}C_{r}\left(3^{-1}\right)^{12-r}\left(4^{-1}\right)^{r}$ Exponent of  $\begin{pmatrix} \frac{1}{4} \\ 3^{\frac{1}{4}} \end{pmatrix}$  exponent of  $\begin{pmatrix} \frac{1}{3} \\ 4^{\frac{1}{3}} \end{pmatrix}$  term 12 0 27 0 12 256 q = 27 + 256 = 283p + q = 0 + 283 = 283
- 19. If A and B are the points of intersection of the circle  $x^2 + y^2 - 8x = 0$  and the hyperbola  $\frac{x^2}{2} - \frac{y^2}{4} = 1$  and a point P moves on the line 2x - 3y + 4 = 0, then the centroid of  $\triangle PAB$  lies on the line : (1) 4x - 9y = 12(2) x + 9y = 36(3) 9x - 9y = 32(4) 6x - 9y = 20Ans. (4) **Sol.**  $x^2 + y^2 - 8x = 0, \ \frac{x^2}{9} - \frac{y^2}{4} = 1$ .... (1)  $4x^2 - 9y^2 = 36$ ... (2) Solve (1) & (2)  $4x^2 - 9(8x - x^2) = 36$  $13x^2 - 72x - 36 = 0$ (13x+6)(x=6)=0 $x = \frac{-6}{12}, x = 6$  $x = \frac{-6}{12}$  (rejected)  $y \rightarrow$  Imaginary  $n = 6, \frac{36}{9}, \frac{y^2}{4} = 1$  $v^2 = 12, v = I\sqrt{12}$  $A(6,\sqrt{12}), B(6,-\sqrt{12})$  $p_{1}\alpha, \frac{2\alpha+3}{3}$  P lies on centroid (h,k) 2x - 3y + y = 0 $h = \frac{12 + \alpha}{3}, \ \alpha = 3h - 12$  $k = \frac{\frac{2\alpha + 1}{3}}{3} \Longrightarrow 2\alpha + 4 = 9k$  $\alpha = \frac{9k-4}{2}$ 6h - 2y = 9k - 46x - 9y = 20



20.	Let $f : \mathbf{R} - \{0\} \rightarrow (-\infty, 1)$ be a polynomial of			
	degree 2, satisfying $f(x)f\left(\frac{1}{x}\right) = f(x) + f\left(\frac{1}{x}\right)$ . If			
	f(K) = -2K, then the sum of squares of all possible			
	values of K is :			
	(1) 1 (2) 6			
	(3) 7 (4) 9			
Ans.	(2)			
Sol.	as $f(x)$ is a polynomial of degree two let it be			
	$f(x) = ax^2 + bx + c  (a \neq 0)$			
	on satisfying given conditions we get			
	$C = 1 \& a = \pm 1$			
	hence $f(x) = 1 \pm x^2$			
	also range $\in (-\infty, 1]$ hence			
	$f(x) = 1 - x^2$			
	now $f(k) = -2k$			
	$1 - k^2 = -2k \rightarrow k^2 - 2k - 1 = 0$			
	let roots of this equation be $\alpha \& \beta$			
	then $\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta$			
	=4-2(-1)=6			

#### **SECTION-B**

**21.** The number of natural numbers, between 212 and 999, such that the sum of their digits is 15, is

#### Ans. (64)

Sol. X V Z

Let 
$$x = 2 \Rightarrow y + z = 13$$
  
(4,9), (5,8), (6,7), (7,6), (8,5), (9,4),  $\rightarrow 6$   
Let  $x = 3 \rightarrow y + z = 12$   
(3,9), (4,8), ....., (9,3)  $\rightarrow 7$   
Let  $x = 4 \rightarrow y + z = 11$   
(2,9), (3,8), ...., (9,1)  $\rightarrow 9$   
Let  $x = 5 \rightarrow y + z = 10$   
(1,9), (2,8), ...., (9,1)  $\rightarrow 10$   
Let  $x = 6 \rightarrow y + z = 9$   
(0,9), (1,8), ...., (9,0)  $\rightarrow 9$   
Let  $x = 7 \rightarrow y + z = 8$   
(0,9), (1,7), ...., (8,0)  $\rightarrow 9$   
Let  $x = 8 \rightarrow y + z = 7$ 

$$(0,7), (1,6), \dots, (7,0) \to 8$$
  
Let  $x = 9 \to y + z = 6$   
 $(0,6), (1,5), \dots, (6,0) \to 7$   
Total = 6 = 7 + 8 + 9 + 10 + 9 + 8 + 7 = 64  
**22.** Let  $f(x) = \lim_{n \to \infty} \sum_{r=0}^{n} \left( \frac{\tan(x/2^{r+1}) + \tan^{3}(x/2^{r+1})}{1 - \tan^{2}(x/2^{r+1})} \right).$ 

Then 
$$\lim_{x\to 0} \frac{e^x - e^{f(x)}}{(x - f(x))}$$
 is equal to \_\_\_\_\_

Ans. (1)

Sol. 
$$f(x) = \lim_{n \to \infty} \sum_{r=0}^{n} \left( \tan \frac{x}{2^r} - \tan \frac{x}{2^{r+1}} \right) = \tan x$$
$$\lim_{x \to 0} \left( \frac{e^x - e^{\tan x}}{x - \tan x} \right) = \lim_{x \to 0} e^{\tan x} \frac{\left( e^{x - \tan x} - 1 \right)}{\left( x - \tan x \right)}$$
$$= 1$$

23. The interior angles of a polygon with n sides, are in an A.P. with common difference 6°. If the largest interior angle of the polygon is 219°, then n is equal to \_\_\_\_\_.

#### Ans. (20)

Sol. 
$$\frac{n}{2}(2a + (n-1)6) = (n-2).180^{\circ}$$
  
an + 3n<sup>2</sup> - 3n = (n - 2). 180° ...(1)  
Now according to question  
 $a + (n-1)6^{\circ} = 219^{\circ}$ 

$$\Rightarrow a = 225^{\circ} - 6n^{\circ} \qquad \dots (2)$$

Putting value of a from equation (2) in (1)

We get

$$(225n - 6n^{2}) + 3n^{2} - 3n = 180n - 360$$
$$\Rightarrow 2n^{2} - 42n - 360 = 0$$
$$\Rightarrow n^{2} - 14n - 120 = 0$$

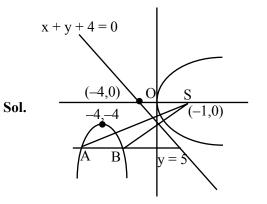
 $\Rightarrow$  n2 -14n -120 = 0

n = 20, -6(rejected)



24. Let A and B be the two points of intersection of the line y + 5 = 0 and the mirror image of the parabola  $y^2 = 4x$  with respect to the line x + y + 4 = 0. If d denotes the distance between A and B, and a denotes the area of  $\Delta$ SAB, where S is the focus of the parabola  $y^2 = 4x$ , then the vlaue of (a + d) is





Area = 
$$\frac{1}{2} \times 4 \times 5 = 10 = a$$
  
6 = 4  
So a + d = 14

25. If y = y(x) is the solution of the differential equation,

$$\sqrt{4 - x^2} \frac{dy}{dx} = \left( \left( \sin^{-1} \left( \frac{x}{2} \right) \right)^2 - y \right) \sin^{-1} \left( \frac{x}{2} \right),$$
$$-2 \le x \le 2, \ y(2) = \left( \frac{\pi^2 - 8}{4} \right), \text{ then } y^2(0) \text{ is equal to}$$

Sol. 
$$\frac{dy}{dx} + \frac{\left(\sin^{-1}\frac{x}{2}\right)}{\sqrt{4 - x^2}}y = \frac{\left(\sin^{-3}\frac{x}{2}\right)^3}{\sqrt{4 - x^2}}$$
  
 $y e^{\frac{\left(\sin^{-\frac{x}{2}}\right)^2}{2}} = \int \frac{\left(\sin^{-3}\frac{x}{2}\right)^3}{4 - x^2} e^{\frac{\left(\sin^{-1}\frac{x}{2}\right)^2}{2}} dx$   
 $y = \left(\sin^{-1}\frac{x}{2}\right)^2 - 2 + c \cdot e^{\frac{-\left(\sin^{-1}\frac{x}{2}\right)^2}{2}}$   
 $y(2) = \frac{\pi^2}{4} \quad 2 \Rightarrow c = 0$   
 $y(0) = -2$ 



TIME : 3:00 PM TO 06:00 PM

	PHYSICS SECTION-A			TEST PAPER WITH SOLUTION			
				Mate	ch List-I with List-I	I	
26.	A uniform magneti	c field of 0.4 T acts			List-I		List-II
	perpendicular to a cire	cular copper disc 20 cm in		(A)	Angular Impulse	(I)	$[M^0 L^2 T^{-2}]$
	radius. The disc is	having a uniform angular		(B)	Latent Heat	(II)	$[M L^2 T^{-3} A^{-1}]$
	velocity of 10 $\pi$ rad s	<sup>-1</sup> about an axis through its		(C)	Electrical	(III)	$[M L^2 T^{-1}]$
	centre and perpendicu	lar to the disc. What is the			resistivity		
	protential difference de	eveloped between the axis of		(D)	Electromotive	(IV)	$[M L^{3} T^{-3} A^{-2}]$
	the disc and the rim ? (	$\pi = 3.14$ )			force		
	(1) 0.0628 V	(2) 0.5024 V		Choo	ose the correct answ	wer fron	n the options giv
	(3) 0.2512 V	(4) 0.1256 V		belov	w :		
ns.	(3)			(1) (2	A)-(III), (B)-(I), (C)	-(IV), (I	D)-(II)
ol.	B = 0.4 T			(2) (2	A)-(I), (B)-(III), (C)	-(IV), (I	D)-(II)
	r = 20 cm			(3) (2	A)-(III), (B)-(I), (C)	-(II), (D	)-(IV)
	$\omega = 10\pi \text{ rad/s}$			(4) (4	A)-(II), (B)-(I), (C)-	(IV), (D	)-(III)
	$E = \frac{1}{2}B R^2$		Ans.	(1)			
	2		Sol.	Ang	ular impulse = [M L	$^{2} \mathrm{T}^{-1}$ ]	
_	= 0.2512 V			Late	nt Heat = $[M^0 L^2 T^{-2}]$	2]	
7.	A parallel plate capacitor of capacitance 1 $\mu$ F is charged to a potential difference of 20 V. The distance between plates is 1 $\mu$ m. The energy			Elect	trical resistivity = [N	$M L^3 T^{-3}$	$A^{-2}$ ]
				Elect	tromotive force = [N	$\Lambda L^2 T^{-3}$	$A^{-1}$ ]
			29.	The	ratio of vapour der	nsities o	f two gases at
	density between plates (1) $1.8 \times 10^3 \text{ J/m}^3$	of capacitor is : (2) $2 \times 10^{-4} \text{ J/m}^3$		same	e temperature is $\frac{4}{24}$	, then	the ratio of r.m
		(4) $1.8 \times 10^5 \text{ J/m}^3$			2: cities will be :	5	
Ans.	(1)					2	
ol.	$C = 1 \ \mu F$			(1) $\frac{2}{2}$ (3) $\frac{2}{2}$	4	(2) $\frac{2}{5}$ (4) $\frac{4}{25}$	
	V = 20 V			(2)	5	(4) 4	
	$d = 1 \ \mu m$			(3) - 2	$\overline{2}$	$(4) \frac{1}{25}$	
	Energy density = $=\frac{1}{2}$	$E_0 E^2$	Ans.				
	2	0	Sol.	$\frac{\rho_1}{2}$ =	$=\frac{4}{1}$		
	$E = \frac{V}{d} = 20 \times 10^6  v /m$			$\rho_2$	25		
	$U = 1.77 \times 10^3 \text{ J/m}^3$			Ratio	$=\frac{4}{25}$	$=\sqrt{\frac{\rho_2}{\rho_2}} =$	$\frac{5}{2}$



30. The kinetic energy of translation of the molecules in 50g of CO<sub>2</sub> gas at 17°C is :
(1) 3986.3 J
(2) 4102.8 J
(3) 4205.5 J
(4) 3582.7 J

Ans. (2)

**Sol.** (KE)<sub>Translational</sub> = 
$$\left[\frac{3}{2}KT\right] \times$$
 no. of molecule  
No. of molecule =  $\left|\frac{50}{44} + 6.023 \times 10^{23}\right|$ 

No. of molecule =  $\begin{bmatrix} \frac{1}{44} & 6.023 \times 10^{23} \end{bmatrix}$ (KE)<sub>Translational</sub> = 4108.644 J

**31.** In a long glass tube, mixture of two liquids A and B with refractive indices 1.3 and 1.4 respectively, forms a convex refractive meniscus towards A. If an object placed at 13 cm from the vertex of the meniscus in A forms an image with a magnification of '-2' then the radius of curvature of meniscus is :

В

 $n_2 = 1.4$ 

(1) 1 cm  
(2) 
$$\frac{1}{3}$$
 cm  
(3)  $\frac{2}{3}$  cm  
(4)  $\frac{4}{3}$  cm

Ans. (3)

Sol.

A  
n<sub>1</sub>=1.3  
O  
13cm  

$$\frac{n_2}{v} - \frac{n_1}{u} \frac{n_2 - n_1}{R}$$

$$\frac{1.4}{v} - \frac{1.3}{-13} \frac{0.1}{R}$$

$$\frac{1.4}{v} = \frac{1 - R}{10R}$$

$$\frac{1.4}{v} = \frac{1 - R}{10R}$$

$$m = \frac{v/n_2}{u/n_1}$$

$$-2 \times \frac{(-13)}{1.3} = \frac{10R}{1 - R}$$

$$R = \frac{2}{3} \text{ cm}$$

**32.** The frequency of revolution of the electron in Bohr's orbit varies with n, the principal quantum number as

(1) 
$$\frac{1}{n}$$
 (2)  $\frac{1}{n^3}$   
(3)  $\frac{1}{4}$  (4)  $\frac{1}{2}$ 

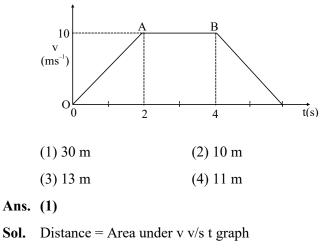
$$\frac{1}{n^4}$$
 (4)  $\frac{1}{n^2}$ 

Ans. (2)

**Sol.** Frequency of revolution  $\propto \frac{1}{n^3}$ 

- **33.** Which of the following phenomena can not be explained by wave theory of light ?
  - (1) Reflection of light
  - (2) Diffraction of light
  - (3) Refraction of light
  - (4) Compton effect

- Sol. Comptan effect is based on particle nature of light.
- 34. The velocity-time graph of an object moving along a straight line is shown in figure. What is the distance covered by the object between t = 0 to t = 4s?



Distance = 
$$\frac{1}{2} \times 2 \times 10 + 2 \times 10 = 30$$
m



d

A bar magnet has total length 2l = 20 units and the field point P is at a distance d = 10 units from the centre of the magnet. If the relative uncertainty of length measurement is 1%, then uncertainty of the magnetic field at point P is :

(1) 10%	(2) 4%
(3) 3%	(4) 5%

## Ans. (2,3)

## Sol. Method-1:

Without considering uncentainity in  $\ell$ .

$$B = \frac{\mu_0}{4\pi} \frac{m}{r^3}$$
$$B \propto \frac{1}{r^3}$$
$$\frac{\Delta B}{B} = 3 \times \left[ -- \right]$$

% uncertainity in B = 3%

## Method-2 :

With considering uncentainity in  $\ell$ .

$$B \propto \frac{1}{\pi^3}$$

$$\frac{\Delta B}{B} = \frac{\Delta \ell}{\ell} + 3 \times \left(\frac{\Delta}{\ell}\right) = 1 + 3 \times 1 = 4\%$$

% uncertainity in B = 4%

Earth has mass 8 times and radius 2 times that of a 36. planet. If the escape velocity from the earth is 11.2 km/s, the escape velocity in km/s from the planet will be :

 $\overline{2}$ 

(1) 11.2	(2) 5.6
(3) 2.8	(4) 8.4
( <b>•</b> )	

Ans. (2)

Sol. 
$$V_{escape} = \sqrt{\frac{2GM}{R}}$$
  
 $\frac{(V_{escape})_{Planet}}{(V_{escape})_{Earth}} = \sqrt{\left(\frac{M_P}{M_E}\right) \times \left(\frac{1}{R_P}\right)} = \frac{1}{2}$   
 $(V_{escape})_{Planet} = \frac{1}{2}(V_{escape})_{Earth}$  5.6km/s

- Given below are two statements. One is labelled as 37. Assertion (A) and the other is labelled as Reason (R). Assertion (A) : Knowing initial position  $x_0$  and initial momentum p0 is enough to determine the position and momentum at any time t for a simple harmonic motion with a given angular frequency  $\omega$ . Reason (R) : The amplitude and phase can be expressed in terms of  $x_0$  an  $p_0$ . In the light of the above statements, choose the correct answer from the options given below :
  - (1) Both (A) and (R) are true but (R) is NOT the correct explanation of (A).
  - (2) (A) is false but (R) is true.
  - (3) (A) is true but (R) is false.

(4) Both (A) and (R) are true and (R) is the correct explanation of (A).

## Ans. (4)

Sol. 
$$x = A \sin(\omega t + \phi)$$
  
 $x_0 = A \sin\phi$  ...(1)  
 $p = mA\omega \cos(\omega t + \phi)$   
 $p_0 = mA\omega \cos\phi$  ....(2)  
 $(2)/(1) \Rightarrow \tan\phi = \left(\frac{x_0}{p_0} \mod \sin\phi\right)$   
 $\sin\phi = \frac{x_0 m\omega}{\sqrt{(m\omega x_0) + p^2}}$ 

From (1), 
$$A = \frac{x_0}{\sin \phi} = \frac{\sqrt{(m\omega x_0)^2 + p^2}}{m}$$

This means we can explain assertion with the given reason.

A concave mirror produces an image of an object 38. such that the distance between the object and image is 20 cm. If the magnification of the image is '-3', then the magnitude of the radius of curvature of the mirror is :



Sol.

$$m = -3 = -\frac{v}{u} \text{ and } v - u = 20 \text{ cm}$$

f = 
$$\frac{vu}{v+u}$$
 =  $\frac{(-30)(-10)}{-30-10}$   
∴ R = +15

39. A body of mass 4 kg is placed on a plane at a point P having coordinate (3, 4) m. Under the action of force  $\vec{F} = (2\hat{i} + 3\hat{j})N$ , it moves to a new point Q having coordinates (6, 10)m in 4 sec. The average power and instantaneous power at the end of 4 sec are in the ratio of :

0

(1) 13 : 6	(2) 6 : 13
(3)1:2	(4) 4 : 3

Ans. (2)

**Sol.** 
$$= \frac{(2\hat{i}+3\hat{j}).(3\hat{i}+6\hat{j})}{4} =$$

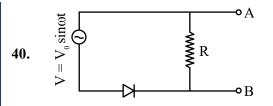
$$\vec{a} = \left(\frac{\vec{F}}{m} = \frac{1}{2}\hat{i} + \frac{3}{4}\hat{j}\right)$$
  
$$\vec{v} \text{ at } t = 4 \text{ sec} = \left(\frac{1}{2}\hat{i} + \frac{3}{4}\hat{j}\right) \times 4 = (2\hat{i} + 3\hat{j})$$
  
$$P_{\text{ins}} = (2\hat{i} + 3)(2\hat{i} + 3\hat{j}) = 13$$
  
$$\leq -2 = 6$$

 $\overline{P_{ins}} = \overline{13}$ 

Note : Given data is not matching.

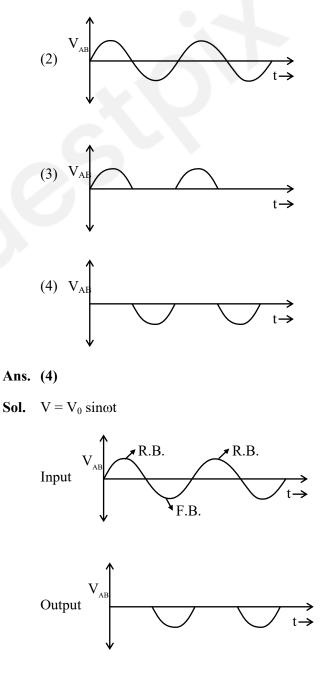
$$S = ut \quad \frac{1}{2}at^{2}$$

$$S = 0 + \frac{1}{2}\frac{(2\hat{i}+3\hat{j})}{4}(4)^{2} = 4\hat{i}+6j$$
If  $\vec{r}_{i} = 3\hat{i}+4\hat{j}$  then  $\vec{r}_{f} = 7\hat{i}+10\hat{j}$ 
But Final position given in the question is (6, 10).

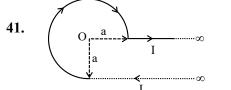


In the circuit shown here, assuming threshold voltage of diode is negligibly small, then voltage V<sub>AB</sub> is correctly represented by :

(1)  $V_{AB}$  would be zero at all times



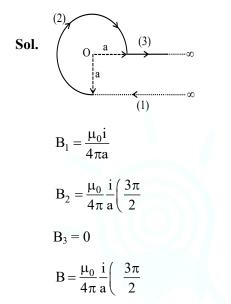




An infinite wire has a circular bend of radius a, and carrying a current I as shown in figure. The magnitude of magnetic field at the origin O of the arc is given by :

(1) 
$$\frac{\mu_0}{4\pi} \frac{I}{a} \left\lfloor \frac{\pi}{2} + 1 \right\rfloor$$
 (2)  $\frac{\mu_0}{4\pi} \frac{I}{a} \left\lfloor \frac{3\pi}{2} + 1 \right\rfloor$   
(3)  $\frac{\mu_0}{2\pi} \frac{I}{a} \left\lfloor \frac{\pi}{2} + 2 \right\rfloor$  (4)  $\frac{\mu_0}{4\pi} \frac{1}{a} \left\lfloor \frac{3\pi}{2} + 2 \right\rfloor$ 

Ans. (2)



42. A uniform rod of mass 250 g having length 100 cm is balanced on a sharp edge at 40 cm mark. A mass of 400 g is suspended at 10 cm mark. To maintain the balance of the rod, the mass to be suspended at 90 cm mark, is

(1) 300 g	(2) 190 g

(3) 200 g (4) 290 g

Ans. (2)

40cm 50cm 10cm 90cm Sol. 250g 400g mg  $\tau_{\text{Net}} = 0 \Longrightarrow (400 \text{g} \times 30) = (250 \text{g} \times 10) \text{ (mg} \times 50)$  $\frac{12000 - 2500}{9500} = \frac{9500}{9500}$ m = 50 50 M = 190 ga 400 g solid cube having an edge of length 10 cm 43. floats in water. How much volume of the cube is outside the water? (Given : density of water =  $1000 \text{ kg m}^{-3}$ ) (2)  $4000 \text{ cm}^3$ (1)  $1400 \text{ cm}^3$  $(4) 600 \text{ cm}^3$  $(3) 400 \text{ cm}^3$ Ans. (4)  $Mg = F_B \Longrightarrow (400 \times 10^{-3}) = 10^3 \times V_d$ Sol.  $V_d = 400 \times 10^{-6} \text{ m}^3$  $(Vol.)_{outside} = (10 \times 10^{-2})^3 - 400 \times 10^{-6}$  $= 600 \times 10^{-6} \text{ m}^2 = 600 \text{ cm}^3$ **44**. The magnetic field of an E.M. wave is given by  $\vec{B} = \left(\frac{\sqrt{3}}{2}\hat{i} + \frac{1}{2}j \quad 30\sin|\omega| t - \frac{z}{c}\right) | (S.I. \text{ Units})$ The corresponding electric field in S.I. units is : (1)  $\vec{E} = \left(\frac{1}{2}\hat{i} - \frac{\sqrt{3}}{2}j \quad 30c\sin|\omega| t - \frac{z}{c}\right)$ (2)  $\vec{E} = \left(\frac{3}{4}i + \frac{1}{4}\hat{j}\right) 30 \cos \left|\omega\left(t - \frac{z}{c}\right)\right]$  $\rightarrow (1, \sqrt{3})$ z

(3) 
$$\vec{E} = \left[\frac{1}{2}\vec{i} + \frac{\sqrt{3}}{2}\vec{j} \quad 30\,\text{csin}\right]\omega\left[t + \frac{z}{c}\right]$$
  
(4)  $\vec{E} = \left(\frac{\sqrt{3}}{2}\hat{i} - \frac{1}{2}\vec{j} \quad 30\,\text{csin}\right]\omega\left[t + \frac{z}{c}\right]$ 

Ans. (1)

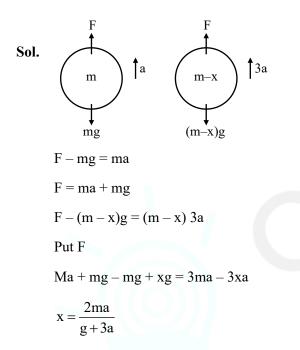
Sol. 
$$\vec{B} = \left(\frac{\sqrt{3}}{2}\hat{i} + \frac{1}{2}j \quad 30\sin|\omega|(t - \frac{z}{c})\right]$$
$$\vec{E} = \vec{B} \times \vec{c} \text{ and } \vec{E} = B_0 c$$
$$\text{Here } \vec{E}\left(\frac{\sqrt{3}}{2}(-\hat{j}) + \frac{1}{-i}\right)$$
$$E_0 = 30c$$
$$\vec{E} = \left(\frac{1}{2}\hat{i} - \frac{\sqrt{3}}{2}j \quad 30c\sin|\omega|(t - \frac{z}{c})\right]$$



**45.** A balloon and its content having mass M is moving up with an acceleration 'a'. The mass that must be released from the content so that the balloon starts moving up with an acceleration '3a' will be : (Take 'g' as acceleration due to gravity)

(1) 
$$\frac{3Ma}{2a-g}$$
 (2)  $\frac{3Ma}{2a+g}$   
(3)  $\frac{2Ma}{3a+g}$  (4)  $\frac{2Ma}{3a-g}$ 

Ans. (3)



#### **SECTION-B**

В

$$\begin{array}{c} \times \times \times \times \times \\ \times \times \times \times \times \\ \times \times \times \times \times \end{array}$$

A conducting bar moves on two conducting rails as shown in the figure. A constant magnetic field B exists into the page. The bar starts to move from the vertex at time t = 0 with a constant velocity. If the induced EMF is  $E \propto t^n$ , then value of n is \_\_\_\_. Ans. (1)

Sol. 
$$ext{Sol} E = \ell v B$$

$$E = \frac{2x}{\sqrt{3}} \times vB \text{ and } x = vt$$
$$E = \frac{2}{\sqrt{3}}v^{2}Bt \qquad E \propto t$$

47. An electric dipole of dipole moment  $6 \times 10^{-6}$  Cm is placed in uniform electric field of magnitude  $10^{6}$  V/m. Initially, the dipole moment is parallel to electric field. The work that needs to be done on the dipole to make its dipole moment opposite to the field, will be J.

### Ans. (12)

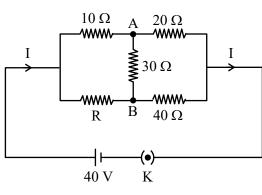
Sol. 
$$p = 6 \times 10^{-6} \text{ Cm}$$
  
 $E = 10^{6} \text{ v/m}$   
 $W = \Delta U = -pE(\cos\theta_{f} - \cos\theta_{i})$   
 $W = 2pE = 12 \text{ J}$ 

**48.** The volume contraction of a solid copper cube of edge length 10 cm, when subjected to a hydraulic pressure of  $7 \times 10^6$  Pa, would be \_\_\_\_\_ mm<sup>3</sup>. (Given bulk modulus of copper =  $1.4 \times 10^{11}$  Nm<sup>-2</sup>)

Sol. 
$$B = \frac{\Delta P}{\frac{\Delta V}{V}}$$
$$\Delta V = \frac{7 \times 10^6}{1.4 \times 10^{11}} \times (10 \times 10^{-2})$$
$$\Delta V = 50 \text{ mm}^3$$

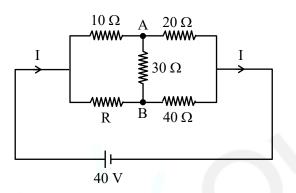


49. The value of current I in the electrical circuit as given below, when potential at A is equal to the potential at B, will be \_\_\_\_\_\_ A.





Sol.



$$V_A = V_B \Longrightarrow$$
 the bridge is balanced

$$\Rightarrow \frac{10}{R} = \frac{20}{40}$$

$$R = 20\Omega$$

$$I = \frac{40}{20} \quad 2A$$

## Ans. (54)

Sol. Maxima condition

$$2\mu t = n\lambda \Rightarrow t = \frac{n\lambda}{2\mu} \Rightarrow t = \frac{2\mu}{2\mu}, \frac{2\lambda}{\mu}, \dots$$

Minima condition  $2\mu t = (2n - 1)\lambda/2$ 

$$\Rightarrow t = \frac{(2n-1)}{4\mu} \Rightarrow t = \frac{\lambda}{\mu}, \frac{3\lambda}{4\mu}, \dots$$
$$\Delta t = \frac{2\lambda}{4\mu}$$

Rate of evaporation =  $\frac{A(\Delta t)}{time}$  = 54 × 10<sup>-13</sup> m<sup>3</sup>/s



# (HELD ON TUESDAY 28th JANUARY 2025)

## TIME: 3:00 PM TO 6:00 PM

CHEMISTRY			TEST PAPER WITH SOLUTION			
		ION-A	53.	Match List-I with L		
51.	consider the elementa	ry reaction		List-I	List_II (Chaosidia linkages	
	$A(g) + B(g) \rightarrow C(g) +$	D(g)		(Saccharides)	(Glycosidic-linkages found)	
	If the volume of re-	eaction mixture is suddenly		(A) Sucrose	(I) α 1 - 4	
	reduced to $\frac{1}{3}$ of its in	itial volume, the reaction rate		<ul><li>(B) Maltose</li><li>(C) Lactose</li></ul>	(II) $\alpha 1 - 4$ and $\alpha 1 - 6$ (III) $\alpha 1 - \beta 2$	
	will become 'x' times	s of the original reaction rate.		(D) Amylopectin	$(IV) \beta 1 - 4$	
	The value of x is :			Choose the correct below :	answer from the options give	
	(1) $\frac{1}{9}$			(1) (A)-(III), (B)-(I),		
				(2) (A)-(IV), (B)-(II)		
	(2) 9			(3) (A)-(II), (B)-(IV) (4) (A)-(I), (B)-(II),		
	(3) $\frac{1}{3}$		Ans.		$(C)^{-(III)}, (D)^{-(IV)}$	
	5		Sol.		32 Glycosidic linkage	
	(4) 3			(B) Maltose $\rightarrow \alpha$ 1–	4 Glycosidic linkage	
Ans.	λ, ´			(C) Lactose $\rightarrow \beta 1 - \beta$	4 Glycosidic linkage	
Sol.	$\mathbf{R}_1 = \mathbf{K}[\mathbf{A}]^{T}[\mathbf{B}]^{T}$			(D) Amylopectin $\rightarrow$		
	$R_{1} = K \left[ \frac{n_{A}}{V} \right] \left[ \frac{1}{V} \right]^{1}$ $R_{2} = K \left[ \frac{3n_{A}}{V} \right] \left[ \frac{3n_{A}}{V} \right]^{1}$				Glycosidic linkage	
			54.	A–III, B–I, C–IV, D–II Identify product [A], [B] and [C] in the following		
			54.	reaction sequence :		
				$CH_3 - C \equiv CH \xrightarrow{Pd/C} [A] \xrightarrow{(i) O_3} [B] + [C]$		
	$R_2 = 9R$			(1) [A] : CH <sub>3</sub> CH=C [C] : HCHO		
52.	The amphoteric oxid	de among $V_2O_3$ , $V_2O_4$ and			0	
	$V_2O_5$ upon reaction v	vith alkali leads to formation		(2) [A] : CH <sub>2</sub> =CH <sub>2</sub> ,	$[B]: \underset{H.C-C-CH}{  }$	
	of an oxide anion. The oxidation state of V in the			[C] : HCHO	3 3	
	oxide anion is :			(3) [A] : CH <sub>3</sub> CH=0	CH <sub>2</sub> , [B] : CH <sub>3</sub> CHO,	
	(1) +3	(2) +7		$[C]: CH_3CH_2OH$	I	
	(3) +5	(4) +4		. , = =	$H_3$ , [B] : CH <sub>3</sub> CHO, [C] : HCHO	
Ans.	(3)		Ans.		· ····	
Sol.	$V_2O_5 + alkali \rightarrow VO_4^3$	-	Sol.	$CH_3 - C \equiv CH - \frac{Pd/C}{H_2}$	$C \rightarrow CH_3 - CH = CH_2[A]$	
				(i) C (ii)Zn,	$_{H_2O}^{O_3} \rightarrow CH_3 - CH = O + HCHO$	
	In $VO_4^{3-}$ ion, vanadium is in +5 oxidation state				[B] [C]	



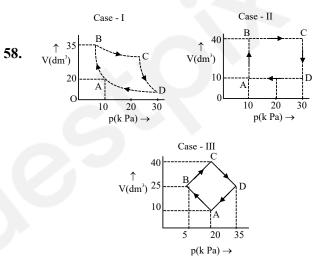
- 55. Arrange the following in increasing order of solubility product : Ca(OH)<sub>2</sub>, AgBr, PbS, HgS (1)  $PbS < HgS < Ca(OH)_2 < AgBr$ (2)  $HgS < PbS < AgBr < Ca(OH)_2$ (3)  $Ca(OH)_2 < AgBr < HgS < PbS$ (4)  $HgS < AgBr < PbS < Ca(OH)_2$ Ans. (2) Sol. Based on the Ksp values and salt analysis cation identification, we can say that order of Ksp value is:  $HgS < PbS < AgBr < Ca(OH)_2$ Ksp values  $\mathrm{HgS} \rightarrow 4 \times 10^{-53}$  $PbS \rightarrow 8 \times 10^{-28}$ AgBr  $\rightarrow 5 \times 10^{-13}$  $Ca(OH)_2 \rightarrow 5.5 \times 10^{-6}$ The purification method based on the following 56.
  - physical transformation is :

 $\begin{array}{ll} \text{Solid} & \xrightarrow{\text{Heat}} & \text{Vapour} & \xrightarrow{\text{Cool}} & \text{Solid} \\ (1) \text{ Sublimation} & (2) \text{ Distillation} \end{array}$ 

- (3) Crystallization (4) Extraction
- Ans. (1)
- Sol. Theory base
- **57.** Identify correct conversion during acidic hydrolysis from the following :
  - (A) starch gives galactose.
  - (B) cane sugar gives equal amount of glucose and fructose.
  - (C) milk sugar gives glucose and galactose.
  - (D) amylopectin gives glucose and fructose.
  - (E) amylose gives only glucose.
  - Choose the **correct** answer from the options given below :
  - (1) (C), (D) and (E) only
  - (2) (A), (B) and (C) only
  - (3) (B), (C) and (E) only
  - (4) (B), (C) and (D) only

Ans. (3)

- **Sol.** (A) Starch  $\xrightarrow{H^+/H_2O}$  Glucose
  - (B) Cane sugar  $\xrightarrow{H^+/H_2O}$  glucose + fructose (Sucrose) 50% 50%
  - (C) Milk sugar  $\xrightarrow{H^+/H_2O}$  glucose + galactose (Lactose)
  - (D) Amylopectin  $\xrightarrow{H^+/H_2O}$  Glucose
  - (E) Amylose  $\xrightarrow{H^+/H_2O}$  Glucose
  - So, correct options are B, C and E only



An ideal gas undergoes a cyclic transformation starting from the point A and coming back to the same point by tracing the path  $A \rightarrow B \rightarrow C \rightarrow D \rightarrow A$ as shown in the three cases above.

Choose the *correct* option regarding  $\Delta U$ .

(1)  $\Delta U$  (Case-III) >  $\Delta U$  (Case-II) >  $\Delta U$  (Case-I)

- (2)  $\Delta U$  (Case-I) >  $\Delta U$  (Case-II) >  $\Delta U$  (Case-III)
- (3)  $\Delta U$  (Case-I) >  $\Delta U$  (Case-III) >  $\Delta U$  (Case-II)
- (4)  $\Delta U$  (Case-I) =  $\Delta U$  (Case-II) =  $\Delta U$  (Case-III)

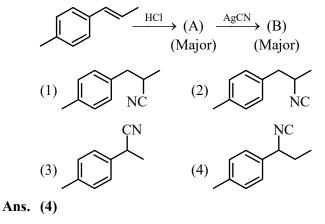
### Ans. (4)

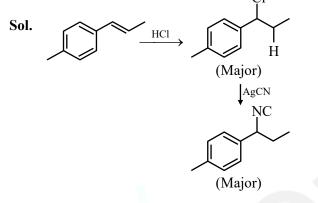
**Sol.** As internal energy 'U' is a state function, its cyclic integral must be zero in a cyclic process

 $\therefore \Delta U \text{ case } (I) = \Delta U \text{ case } (II) = \Delta U \text{ case } (III)$ 



**59.** The product B formed in the following reaction sequence is :





60. Concentrated nitric acid is labelled as 75% by mass. The volume in mL of the solution which contains 30 g of nitric acid is \_\_\_\_\_.

Given : Density of nitric acid solution is 1.25 g/mL

- (1) 45 (2) 55
- (3) 32 (4) 40

## Ans. (3)

**Sol.** % w/w of  $HNO_3 = 75\%$ 

means 100 gm of solution containing 75 g of  $HNO_3$ 

$$\& \left(\frac{\text{gm}}{\text{m}_{1}}\right)_{\text{solution}} = 1.25 \quad \frac{100 \text{gm}}{1.25}$$

$$V_{\text{ml}} \text{ of } 100 \text{ gm solution} = \frac{100}{1.25} \text{ml}$$

$$\therefore 75 \text{ gm of HNO}_{3} \text{ present in } \frac{100}{1.25} \text{ ml solution}$$

$$\therefore 30 \text{ gm of HNO}_{3} \text{ present in}$$

$$\frac{100}{1.25 \times 75} \times 30 \quad 32 \text{ ml solution}$$

61. Match List-I with List-II.

List-I			List-II	
(Complex)		(Hybridisation of		
		central metal ion)		
(A)	$[CoF_6]^{3-}$	(I)	d <sup>2</sup> sp <sup>3</sup>	
(B)	[NiCl <sub>4</sub> ] <sup>2-</sup>	(II)	sp <sup>3</sup>	
(C)	$\left[\text{Co(NH_3)}_6\right]^{3+}$	(III)	$sp^{3}d^{2}$	
(D)	$[Ni(CN)_{4}]^{2-}$	(IV)	dsp <sup>2</sup>	
Choose the <i>correct</i> answer from the options given				

below :

(1) (A)-(I), (B)-(IV), (C)-(III), (D)-(II)

(2) (A)-(III), (B)-(II), (C)-(I), (D)-(IV)

- (3) (A)-(I), (B)-(II), (C)-(III), (D)-(IV)
- (4) (A)-(III), (B)-(IV), (C)-(I), (D)-(II)

Ans. (2)

**Sol.** (A) 
$$[CoF_6]^{-3}$$

$$\mathrm{Co}^{3+} \rightarrow 3\mathrm{d}^6$$

(B) 
$$[NiCl_4]^{2-}$$
  
 $Ni^{2+} \rightarrow 3d^8$ 

(C) 
$$[Co(NH_3)_6]^{3+}$$
  
 $Co^{3+} \rightarrow 3d^6$ 

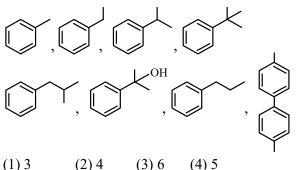
11 11 11		
3d	4s	4p
	$d^2sp^3$	

(D) 
$$[Ni (CN)_4]^{2-}$$

$$\mathrm{Ni}^{2+} \rightarrow 3\mathrm{d}^{8}$$

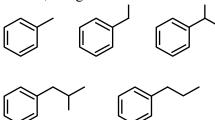


**62.** The total number of compounds from below when treated with hot KMnO<sub>4</sub> giving benzoic acid is :



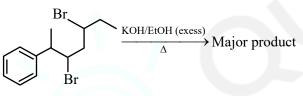
Ans. (4)

**Sol.** Compounds having at least 1  $\alpha$ -H will react with KMnO<sub>4</sub> and give benzoic acid.



Total 5 compounds

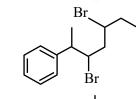
**63.** The major product of the following reaction is :



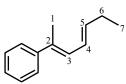
- (1) 6-Phenylhepta-2,4-diene
- (2) 2-Phenylhepta-2,5-diene
- (3) 6-Phenylhepta-3,5-diene
- (4) 2-Phenylhepta-2,4-diene

Ans. (4)

Sol.



KOH/EtOH (excess) Δ



2-Phenylhepta-2,4-diene

**64.** Given below are two statements :

**Statement (I) :** According to the Law of Octaves, the elements were arranged in the increasing order of their atomic number.

**Statement (II) :** Meyer observed a periodically repeated pattern upon plotting physical properties of certain elements against their respective atomic numbers.

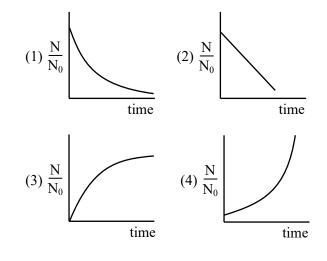
In the light of the above statements, choose the **correct** answer from the options given below :

- (1) Statement I is false but Statement II is true
- (2) Both Statement I and Statement II are true
- (3) Statement I is true but Statement II is false
- (4) Both Statement I and Statement II are false
- Ans. (4)

**Sol.** Law of octaves was arranged in the increasing order of their atomic weight.

Lothar Meyer plotted the physical properties such as atomic volume, melting point and boiling point against atomic weight.

65. For bacterial growth in a cell culture, growth law is very similar to the law of radioactive decay. Which of the following graphs is most suitable to represent bacterial colony growth ?

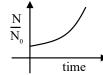




Ans. (4)

Sol. Because no. of bacteria initial =  $N_0$ and No. of bacteria at any time t = N Since bacterial growth is given as  $N = N_0 e^{Kt}$ 

Where K = growth constant for bacterial growth



- **66.** Which of the following is/are not correct with respect to energy of atomic orbitals of hydrogen atom?
  - (A) 1s < 2p < 3d < 4s
  - (B) 1s < 2s = 2p < 3s = 3p
  - (C) 1s < 2s < 2p < 3s < 3p
  - (D) 1s < 2s < 4s < 3d

Choose the **correct** answer from the options given below :

(1) (B) and (D) only
(2) (A) and (C) only
(3) (C) and (D) only
(4) (A) and (B) only

## Ans. (3)

Sol. For single electron species energy only depends on 'n' (principal quantum number)

So energy of 2s = 2p

and energy of 3d < 4s

67. Assume a living cell with 0.9% ( $\omega/\omega$ ) of glucose solution (aqueous). This cell is immersed in another solution having equal mole fraction of glucose and water.

(Consider the data upto first decimal place only) The cell will :

(1) shrink since soluton is 0.5 % ( $\omega/\omega$ )

(2) shrink since solution is 0.45% ( $\omega/\omega$ ) as a result of association of glucose molecules (due to hydrogen bonding)

- (3) swell up since solution is 1% ( $\omega/\omega$ )
- (4) Show no change in volume since solution is  $0.9\% (\omega/\omega)$

# Ans. (BONUS)

## NTA (4)

Sol. Living cell = 0.9 gm in 100 gm of solution % w/w = 0.9 Solution is have equal moles of glucose and water = 0.5

Weight of solution =  $0.5 \times 180 + 0.5 \times 18 = 99$  gm % w/w  $\approx 90\%$ 

- Concentrated solution
- = Cell will shrink.

**68.** Identify correct statements :

(A) Primary amines do not give diazonium salts when treated with  $NaNO_2$  in acide condition.

(B) Aliphatic and aromatic primary amines on heating wth CHCl<sub>3</sub> and ethanolic KOH form carbylamines.

(C) Secondary and tertiary amines also give carbylamine test.

(D) Benzenesulfonyl chloride is known as Hinsberg's reagent.

(E) Tertiary amines reacts with benzenesulfonyl chloride very easily.

Choose the correct answer from the options given below :

(1) (B) and (D) only
(2) (A) and (B) only
(3) (D) and (E) only
(4) (B) and (C) only

Ans. (1)

**Sol.** (A) 
$$R-NH_2 \xrightarrow{NaNO_2} R-N_2^{\oplus}Cl^{\oplus}$$

(B) 
$$\xrightarrow{\text{NH}_2} \xrightarrow{\text{CHCl}_3} \xrightarrow{\text{NC}}$$
  
R-NH<sub>2</sub>  $\xrightarrow{\text{CHCl}_3}$  R-NC

(C) Only primary amine gives carbyl amine test

- (D) Ph–SO<sub>2</sub>Cl  $\longrightarrow$  Hinsberg reagent Benzene sulphonyl chloride
- (E) Tertiary amine do not react with Ph-SO<sub>2</sub>Cl

So correct options are (B) and (D) only

Questpix Final JEE-Main Exam January, 2025/28-01-2025/Evening Session Given below are two statements : 69. **SECTION-B** 71. The spin only magnetic moment ( $\mu$ ) value (B.M.) are are Statement (I) : and of the compound with strongest oxidising power isomeric compounds. among  $Mn_2O_3$ , TiO and VO is B.M. Statement **(II)** /NH and : (Nearest integer). NH are functional group isomers. Ans. (5) In the light of the above statements, choose the Strongest oxidising power among the option is Sol. correct answer from the options given below :  $Mn_2O_3$  because of E° value (1) Both Statement I and Statement II are false  $E^{\circ}_{Mn^{+3}/Mn^{+2}} = +1.57V$ (2) Both Statement I and Statement II are true  $Mn^{+3} \rightarrow d^4$  configuration (3) Statement I is true but Statement II is false (4) Statement I is false but Statement II is true  $\mu = \sqrt{24} BM$ Ans. (2) = 4.89 BMSol. Statement-I  $\rightarrow$  True  $\Rightarrow 5$ Consider the following data : 72. Heat of formation of  $CO_2(g) = -393.5 \text{ kJ mol}^{-1}$ Both are ring chain isomers Heat of formation of  $H_2O(1) = -286.0 \text{ kJ mol}^{-1}$ **Statement-II** → True Heat of combustion of benzene = -3267.0 kJ mol<sup>-1</sup>  $\sim$  NH<sub>2</sub> -NH-The heat of formation of benzene is  $\_\_\_ kJ mol^{-1}$ . 1° Amine 2° Amine (Nearest integer) 1° Amine and 2° Amine are different functional Ans. (48) groups, hence both are functional group isomers. **Sol.**  $\Delta H_{f}[CO_{2}(g)] = -393.5 \text{ kJ} / \text{mole}$ Identify the inorganic sulphides that are yellow in 70.  $\Delta H_{\rm f}[H_2O(\ell)] = -286.0 \text{ kJ} / \text{mole}$ colour :  $(A) (NH_4)_2 S$ (B) PbS  $\Delta H_{c}[C_{6}H_{6}] = -3267.0 \text{ kJ} / \text{mole}$ (C) CuS (D)  $As_2S_3$  $\Delta H_{f} C_{6} H_{6} = (?)$ (E)  $As_2S_5$  $C_6H_6 + \frac{15}{2}O_2(g) \longrightarrow 6CO_2(g) + 3H_2O(\ell)$ Choose the *correct* answer from the options given below :  $\Delta H_{R} = \Delta H_{C} = \Sigma \Delta H_{f}(P) - \Sigma \Delta H_{f}(R)$ (A) (A) and (C) only(2) (A), (D) and (E) only  $-3267 = 6 \times (-393.5) + 3(-286) - \Delta H_{f}(C_{6}H_{6})$ (3) (A) and (B) only (4) (D) and (E) only Ans. (4)  $\Delta H_f (C_6 H_6) = 48 \text{ kJ/mole}$ NTA (2) Electrolysis of 600 mL aqueous solution of NaCl 73. Sol.  $As_2S_3$  and  $As_2S_5$  are yellow colour sulphides, for 5 min changes the pH of the solution to 12. (NH<sub>4</sub>)<sub>2</sub>S is colourless, PbS is black, CuS is black in The current in Amperes used for the given colour electrolysis is . (Nearest integer).



Ans. (2)

**Sol.** Electrolysis of NaCl is

NaCl + H<sub>2</sub>O (aq) 
$$\rightarrow$$
 NaOH (aq) +  $\frac{1}{2}$ Cl<sub>2</sub>(g) +  $\frac{1}{2}$ H<sub>2</sub>(g)

Since during electrolysis pH changes to 12

So  $[OH^{\odot}] = 10^{-2}$  and  $[H^{+}] = 10^{-12}$ 

So by Faraday law

Gram amount of substance deposited =

Amount of electricity passed

$$10^{-2} \times \frac{600}{1000} \times 96500 = I \times t$$
$$\frac{10^{-2} \times 600}{1000} \times 96500 = I \times 5 \times 60$$
$$I = \frac{10^{-2} \times 600 \times 96500}{1000 \times 5 \times 60}$$

I = 1.93 ampere

So, I = 2 ampere (nearest integer)

74. A group 15 element forms  $d\pi - d\pi$  bond with transition metals. It also forms hydride, which is a strongest base among the hydrides of other group members that form  $d\pi - d\pi$  bond. The atomic number of the element is \_\_\_\_\_.

### Ans. (15)

Sol. Phosphorus belongs to  $15^{\text{th}}$  group and forms  $d\pi - d\pi$  bond with transition metal and PH<sub>3</sub> is strongest base among the other group members except NH<sub>3</sub>.

75. Total number of molecules/species from following which will be paramagnetic is \_\_\_\_\_.
O<sub>2</sub>, O<sup>+</sup><sub>2</sub>, O<sup>-</sup><sub>2</sub>, NO, NO<sub>2</sub>, CO, K<sub>2</sub>[NiCl<sub>4</sub>],

[Co(NH<sub>3</sub>)<sub>6</sub>]Cl<sub>3</sub>, K<sub>2</sub>[Ni(CN)<sub>4</sub>]

Ans. (6)

**Sol.**  $O_2 \rightarrow 2$  unpaired electrons according to MOT

 $O_2^+ \rightarrow 1$  unpaired electrons according to MOT

 $O_2^- \rightarrow 1$  unpaired electrons according to MOT

NO  $\rightarrow$  odd electron species

 $NO_2 \rightarrow odd \ electron \ species$ 

 $K_2[NiCl_4] \rightarrow Ni^{2+} \Rightarrow 3d^8$  weak Ligand, C.N. = 4

 $\Rightarrow$  Tetrahedral, Paramagnetic with 2 unpaired electrons