

Multiple Choice Questions I

- 14.1. The displacement of a particle is represented by the equation $y = 3 \cos(\pi/4 2\omega t)$. The motion of the particle is
- a) simple harmonic with period 2p/w
- b) simple harmonic with period π/ω
- c) periodic but not simple harmonic
- d) non-periodic

Answer:

The correct answer is b) simple harmonic with period π/ω

- 14.2. The displacement of a particle is represented by the equation $y = \sin^3 \omega t$. The motion is
- a) non-periodic
- b) periodic but not simple harmonic
- c) simple harmonic with period $2\pi/\omega$
- d) simple harmonic with period π/ω

Answer:

The correct answer is c) simple harmonic with period $2\pi/\omega$

- 14.3. The relation between acceleration and displacement of four particles are given below:
- a) $a_x = +2x$
- b) $a_x = +2x^2$
- c) $a_x = -2x^2$
- d) $a_x = -2x$

Which one of the particles is executing simple harmonic motion?

Answer:

The correct answer is d) $a_x = -2x$

- 14.4. Motion of an oscillating liquid column in a U-tube is
- a) periodic but not simple harmonic
- b) non-periodic
- c) simple harmonic and time period is independent of the density of the liquid
- d) simple harmonic and time period is directly proportional to the density of the liquid Answer:

The correct answer is c) simple harmonic and time period is independent of the density of the liquid

- 14.5. A particle is acted simultaneously by mutually perpendicular simple harmonic motions $x = a \cos \omega t$ and $y = a \sin \omega t$. The trajectory of motion of the particle will be
- a) an ellipse
- b) a parabola
- c) a circle
- d) a straight line

Answer:

The correct answer is c) a circle

- 14.6. The displacement of a particle varies with time according to the relation $y = a \sin \omega t + b \cos \omega t$
- a) the motion is oscillatory but not SHM
- b) the motion is SHM with amplitude a + b
- c) the motion is SHM with amplitude $a^2 + b^2$
- d) the motion is SHM with amplitude $\sqrt{a^2 + b^2}$

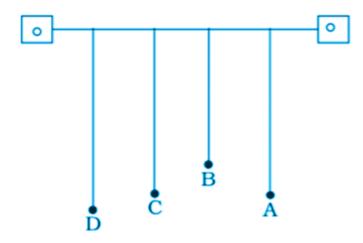
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The correct answer is d) the motion is SHM with amplitude $\sqrt{a^2 + b^2}$

14.7. Four pendulums A, B, C, and D are suspended from the same elastic support as shown in the figure. A and C are of the same length, while B is smaller than A and D is larger than A. If A is given a transverse displacement,



- a) D will vibrate with maximum amplitude
- b) C will vibrate with maximum amplitude
- c) B will vibrate with maximum amplitude
- d) all the four will oscillate with equal amplitude

Answer:

The correct answer b) C will vibrate with maximum amplitude

14.8. Figure shows the circular motion of a particle. The radius of the circle, the period, sense of revolution, and the initial position are indicated on the figure. The simple harmonic motion of the x-projection of the radius vector of the rotating particle P is

a) $x(t) = B \sin(2\pi t/30)$

b) $x(t) = B \cos (\pi t/15)$

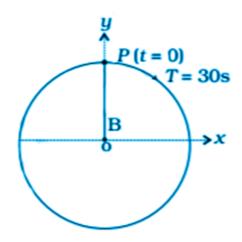
c) $x(t) = B \sin (\pi t/15 + \pi/2)$

d) $x(t) = B \cos (\pi t/15 + \pi/2)$

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The correct answer a) $x(t) = B \sin(2\pi t/30)$

14.9. The equation of motion of a particle is $x = a \cos(\alpha t)^2$. The motion is

- a) periodic but not oscillatory
- b) periodic and oscillatory
- c) oscillatory but not periodic
- d) neither periodic nor oscillatory

Answer:

The correct answer c) oscillator but not periodic

14.10. A particle executing SHM has a maximum speed of 30 cm/s and a maximum acceleration of 60 cm/s². The period of oscillation is

- a) πs
- b) $\pi/2$ s
- c) 2 πs
- d) π/t s

Answer:

The correct answer a) π s

14.11. When a mass m is connected individually to two springs S1 and S2, the oscillation frequencies are v1 and v2. If the same mass is attached to the two springs are shown in the figure, the oscillation frequency would be

a) v1 + v2

b)

$$\sqrt{v_1^2 + v_2^2}$$

c)

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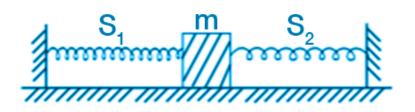
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$$\left(\frac{1}{v_1} + \frac{1}{v_2}\right)^{-1}$$

d)

$$\sqrt{v_1^2 - v_2^2}$$



Answer:

$$\sqrt{v_1^2 + v_2^2}$$

The correct answer b)

Multiple Choice Questions II

14.12. The rotation of earth about its axis is

- a) periodic motion
- b) simple harmonic motion
- c) periodic but not simple harmonic motion
- d) non-periodic motion

Answer:

The correct answer

- a) periodic motion
- c) periodic but not simple harmonic motion

14.13. Motion of a ball bearing inside a smooth curved bowl, when released from a point slightly above the

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lower point is

- a) simple harmonic motion
- b) non-periodic motion
- c) periodic motion
- d) periodic but not SHM

Answer:

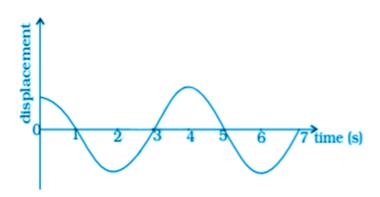
The correct answer

- a) simple harmonic motion
- b) non-periodic motion

14.14. Displacement versus time curve for a particle executing SHM is shown in figure. Choose the correct statements.

- a) phase of the oscillator is same at t = 0 s and t = 2 s
- b) phase of the oscillator is same at t = 2 s and t = 6 s
- c) phase of the oscillator is same at t = 1 s and t = 7 s
- d) phase of the oscillator is same at t = 1 s and t = 5 s





Answer:

The correct answer

- b) phase of the oscillator is same at t = 2 s and t = 6 s
- d) phase of the oscillator is same at t = 1 s and t = 5 s

14.15. Which of the following statements is/are true for a simple harmonic oscillator?

- a) force acting is directly proportional to displacement from the mean position and opposite to it
- b) motion is periodic
- c) acceleration of the oscillator is constant
- d) the velocity is periodic

Answer:

The correct answer

a) force acting is directly proportional to displacement from the mean position and opposite to it

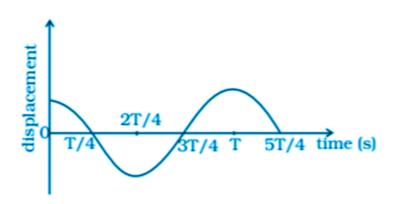
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- b) motion is periodic
- d) the velocity is periodic

14.16. The displacement time graph of a particle executing SHM is shown in the figure. Which of the following statement is/are true?



- a) the force is zero at t = 3T/4
- b) the acceleration is maximum at t = 4T/4
- c) the velocity is maximum at t = T/4
- d) the PE is equal to KE of oscillation t = T/2 Answer:

The correct answer

- a) the force is zero at t = 3T/4
- b) the acceleration is maximum at t = 4T/4
- c) the velocity is maximum at t = T/4

14.17. A body is performing SHM. Then its

- a) average total energy per cycle is equal to its maximum kinetic energy
- b) average kinetic energy per cycle is equal to half of its maximum kinetic energy
- c) mean velocity over a complete cycle is equal to $2/\pi$ times of its maximum velocity
- d) root mean square velocity is $1/\sqrt{2}$ times of its maximum velocity

Answer:

The correct answer

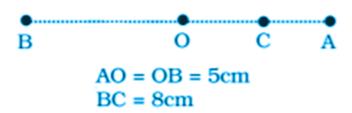
- a) average total energy per cycle is equal to its maximum kinetic energy
- b) average kinetic energy per cycle is equal to half of its maximum kinetic energy
- d) root mean square velocity is $1/\sqrt{2}$ times of its maximum velocity

14.18. A particle is in linear simple harmonic motion between two points A and B, 10 cm apart. Taken the direction from A to B as the +ve direction and choose the correct statements.

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- a) the sign of velocity, acceleration, and force on the particle when it is 3 cm away from A going towards B are positive
- b) the sign of velocity of the particle at C going towards O is negative
- c) the sign of velocity, acceleration, and force on the particle when it is 4 cm away from B going towards A are negative
- d) the sign of acceleration and force on the particle when it is at point B is negative Answer:

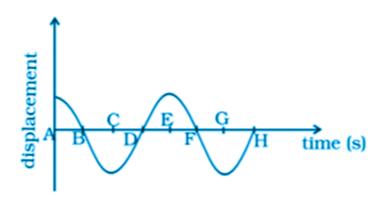
The correct answer

- a) the sign of velocity, acceleration, and force on the particle when it is 3 cm away from A going towards B are positive
- c) the sign of velocity, acceleration, and force on the particle when it is 4 cm away from B going towards A are negative
- d) the sign of acceleration and force on the particle when it is at point B is negative

Very Short Answers

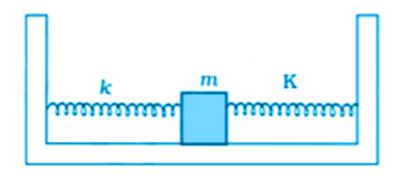
- 14.19. Displacement versus time curve for a particle executing SHM is shown. Identify the points marked at which
- i) velocity of the oscillator is zero
- ii) speed of the oscillator is maximum





- i) When the points A, C, E, and G lie at their extreme positions, the velocity of the oscillator is zero.
- ii) When the points B, D, F, and H lie at their mean positions, the speed of the oscillator is maximum.

14.20. Two identical springs of spring constant K are attached to a block of mass m and to fixed supports as shown in the figure. When the mass is displaced from equilibrium position by a distance x towards right, find the restoring force.

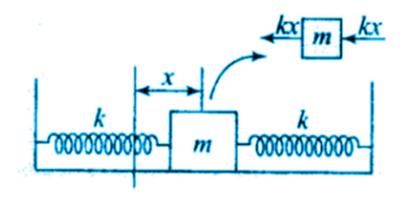


Answer:

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Given,

F1 = -kx for the left spring

F2 = -kx for the right spring

Restoring force, F = F1 + F2 = -2kx

Therefore, when the spring is towards left, F = 2kx

14.21. What are the two basic characteristics of a simple harmonic motion?

Answer:

Following are the two basic characteristics of a SHM:

- a) acceleration and displacement are directly proportional to each other
- b) the direction of acceleration is towards the mean position while the direction of displacement is towards the opposite side of the mean position

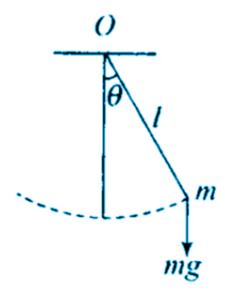
14.22. When will the motion of a simple pendulum be simple harmonic?

Answer:

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Consider a simple pendulum with O as the fixed point that has a restoring torque.

The restoring force is given as $F = -mg \sin \theta$

 θ is so small that $\theta = arc/radius = x/1$

Therefore, F = - mg x/l

Therefore, it can be said that the motion of the simple pendulum will be simple harmonic when θ is small.

14.23. What is the ratio of maximum acceleration to the maximum velocity of a simple harmonic oscillator? Answer:

The displacement equation of SHM is $x = a \sin{(\omega t + \phi)}$ The velocity of the particle, v = dx/dt = d a $\sin{(\omega t + \phi)}/dt$ Maximum velocity, $|v|max = a\omega$ Acceleration, $A = dv/dt = a\omega^2 \sin{(\omega t + \phi)}$

Maximum acceleration, $|A|max = \omega 2a$

 $|v| \max / |A| \max = \omega$

14.24. What is the ratio between the distance travelled by the oscillator in one time period and amplitude? Answer:

Distance travelled by the oscillator in one time period = 4A

Where A is the amplitude of the oscillation

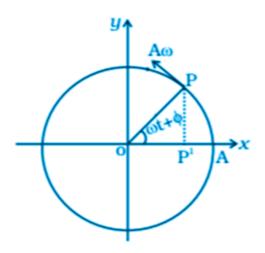
Therefore, required ration = 4A/A = 4/1 = 4:1

14.25. In figure, what will be the sign of the velocity of the point P', which is the projection of the velocity of the reference particle P. P is moving in a circle of radius R in anticlockwise direction.

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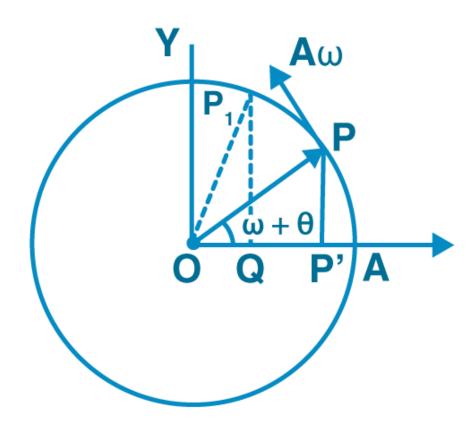






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P' is the perpendicular of the velocity vector for the particle Pat time t.

When the particle moves from P to P1, the foot of the particle moves from P' to Q and that is towards the negative axis.

Therefore, the sign is negative.

14.26. Show that for a particle executing SHM, velocity, and displacement have a phase difference of $\pi/2$. Answer:

The displacement equation of SHM, $x = a \cos \omega t$

Velocity, $v = dx/dt = -a\omega \sin \omega t$

The phase displacement, $\phi 1 = \omega t$

Phase velocity, $\phi 2 = \pi/2 + \omega t$

Therefore, difference in phase of displacement = $\phi 2 - \phi 1 = \pi/2$

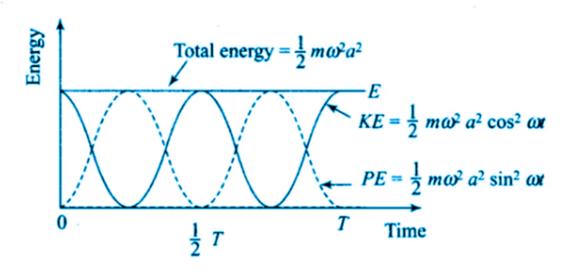
14.27. Draw a graph to show the variation of PE, KE, and total energy of a simple harmonic oscillator with displacement.

Answer:

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14.28. The length of a second's pendulum on the surface of earth is 1 m. What will be the length of a second's pendulum on the moon?

Time period of a simple pendulum, $T = 2\pi\sqrt{l/g}$

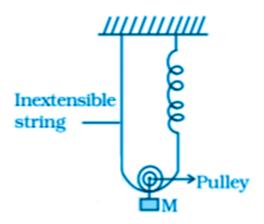
Where, l is the length of the pendulum and g is the acceleration due to gravity

Therefore, lmoon/gmoon = learth/gearth = 1/6 m

Short Answers

14.29. Find the time period of mass M when displaced from its equilibrium position and then released for the system shown in the figure.





The distance through which the mass is pulled is y.

The total extension of the spring is y + y = 2y.

The initial equilibrium mean position = x_0

The net extension in the spring = $x_0 + 2y$

When the equation, F = 2T is solved where $T = kx_0$,

We get, a as proportional to -x.

When the acceleration obtained above is compared to the standard SHM equation, we get

 $\omega^2 = 4k/m$

 $\omega = \sqrt{4k/M}$

14.30. Show that the motion of a particle represented by $y = \sin \omega t - \cos \omega t$ is simple harmonic with a period of $2\pi/\omega$.

Answer:

A function will represents SHM and is written as $\sin (2\pi/T t + \phi)$

 $y = \sin \omega t - \cos \omega t$

 $y = \sqrt{2} \sin (\omega t - \pi/4)$

The standard SHM has $y = a s \sin (2\pi/T t + \phi)$

 $T = 2\pi/\omega$

14.31. Find the displacement of a simple harmonic oscillator at which its PE is half of the maximum energy of the oscillator.

Answer:

The mean position of the oscillator at x with PE = $1/2 \text{ kx}^2$

 $PE = -m^2x^2$

When PE is maximum, KE = 0 at x = A

 $E = 1/2 \text{ m}\omega^2 A^2$

PE = 1/2 total energy

 $x^2 = 1/2 A^2$

 $x = \pm A/\sqrt{2}$

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14.32. A body of mass m is situated in a potential field $U(x) = U0 (1 - \cos \alpha x)$ when U0 and α are constants. Find the time period of small oscillations.

Answer:

The time period of the small oscillation is $T = 2\pi/\alpha \sqrt{m/U_0}$

14.33. A mass of 2 kg is attached to the spring of spring constant 50 N/m. The block is pulled to a distance of 5 cm from its equilibrium position at x = 0 on a horizontal frictionless surface from rest at t = 0. Write the expression for its displacement at anytime t.

Answer:

 $x = 5 \sin 5t$

14.34. Consider a pair of identical pendulums, which oscillate with equal amplitude independently such that when one pendulum is at its extreme position making an angle of 2° to the right with the vertical, the other pendulum makes an angle of 1° to the left of the vertical. What is the phase difference between the pendulums?

Answer:

$$\theta_1 = \theta_0 \sin (wt + \delta_1)$$

$$\theta_2 = \theta_0 \sin (wt + \delta_2)$$

for first, $\theta = 2^\circ$
for second, $\theta = -1^\circ$

$$\delta_1 - \delta_2 = 120^\circ$$

Long Answers

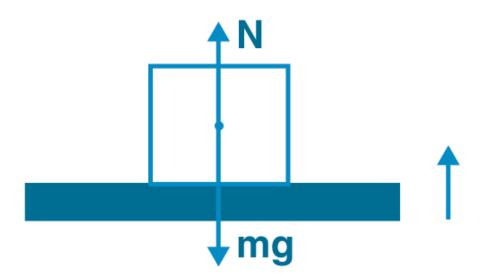
- 14.35. A person normally weighing 50 kg stands on a massless platform which oscillates up and down harmonically at a frequency of 2 s^{-1} and an amplitude 5 cm. A weighing machine on the platform gives the persons weight against time.
- a) will there be any change in weight of the body, during the oscillation?
- b) if answer to part a) is yes, what will be the maximum and minimum reading in the machine and at which position?

Answer:

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- a) The change in the weight of the body during the oscillation is 885 N
- b) The maximum weight is 885 N while the minimum weight is 95.5 N.

14.36. A body of mass m is attached to one end of a massless spring which is suspended vertically from a fixed point. The mass is held in hand so that the spring is neither stretched nor compressed. Suddenly the support of the hand is removed. The lowest position attained by the mass during oscillation is 4 cm below the point, where it was held in hand.

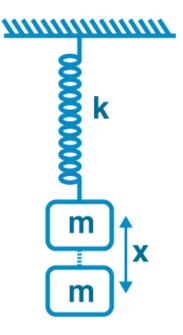
- a) what is the amplitude of oscillation?
- b) find the frequency of oscillation?

Answer:

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The PE of spring = gravitational PE lost by the man

PE = mgx

1/2 kx2 is the PE due to spring

x = 2mg/k

- a) the amplitude of the spring is 2cm
- b) frequency of oscillation is v = 3.52 Hz

14.37. A cylindrical log of wood of height h and area of cross section A floats in water. It is pressed and

$$T = 2\pi \sqrt{\frac{m}{A\rho g}}$$

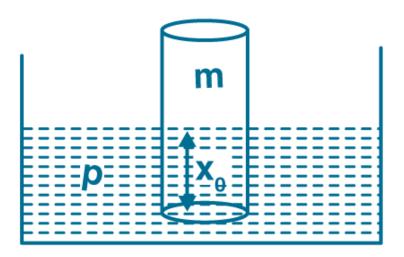
then released. Show that the log would execute SHM with a time period is mass of the body and ρ is density of the liquid. Answer:

where m

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The SHM executed by the cylindrical wood log is given as $T = 2\pi \sqrt{m/A\rho g}$

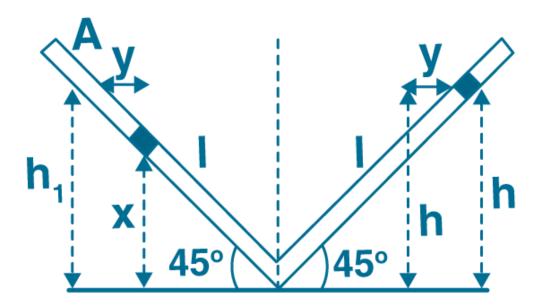
14.38. One end of a V-tube containing mercury is connected to a suction pump and the other end to atmosphere. The two arms of the tube are inclined to horizontal at an angle of 45° each. A small pressure difference is created between two columns when the suction pump is removed. Will the column of mercury in V-tube execute simple harmonic motion? Neglect capillary and viscous forces. Find the time period of oscillation.

Answer:

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The initial height of the columns is h_0 Let dx be the element that needs to be considered The mass is dm = A.dx. ρ PE on the left of dm = (dm)gh Total PE = A ρ g h1²/2

When the above equation is differentiated along with KE where KE is A ρlv^2

We get the equation of SHM oscillator along with the standard equation of SHM when the total energy is obtained by adding PE and KE

 $T = 2\pi\sqrt{1/g}$

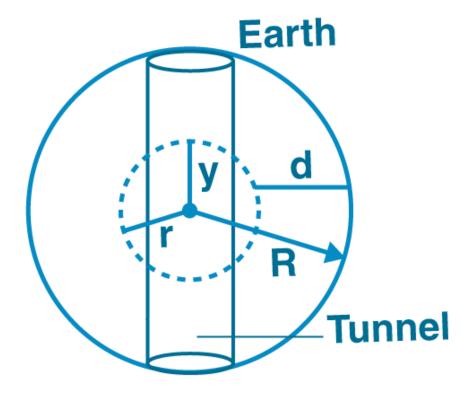
14.39. A tunnel is dug through the centre of the earth. Show that a body of mass 'm' when dropped from rest from one end of the tunnel will execute simple harmonic motion.

Answer:

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Acceleration due to gravity of the earth inside the earth is g'

g' = g(1-d/R)

R-d = y

g' = g y/R

F = -mg y/R

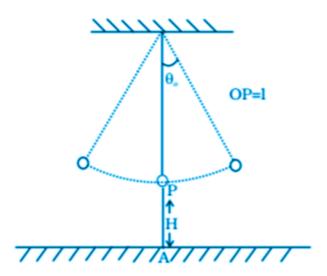
F is proportional to (-y)

When the body is in a tunnel the motion is SHM. ma = -mg'

 $T = 2\pi \sqrt{R/g}$

14.40. A simple pendulum of time period 1s and length l is hung from a fixed support at O, such that the bob is at a distance H vertically above A on the ground. The amplitude is θ_0 . The string snaps at $\theta = \theta_0/2$. Find the time taken by the bob to hit the ground. Also, find distance from A where bob hits the ground. Assume θ_0 to be small so that $\sin \theta_0$, θ_0 and $\cos \theta_0$ 1.



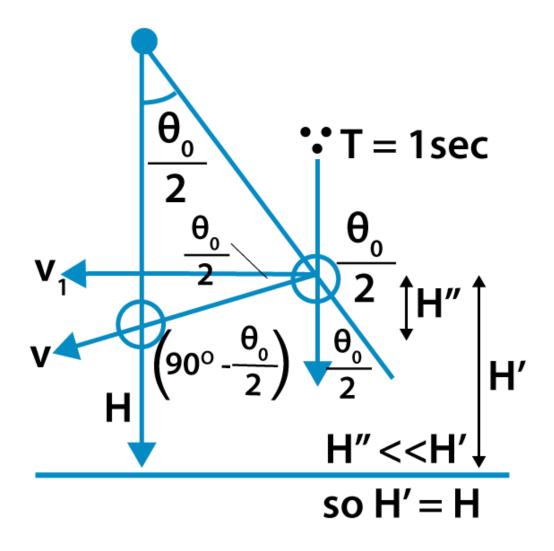


At t = t1 and $\theta = \theta_0/a$ T = 1 sec $\theta_0/2 = \theta_0 \cos 2\pi/T t1$ d $\theta/dt = -\theta_0 2\pi \sin 2\pi t$



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At t = 1/6, that is when $\theta = \theta_0/2$ d $\theta/dt = -\theta_0\pi\sqrt{3}$ $v/l = -\theta_0\pi\sqrt{3}$

 $v = -\theta_0 \pi \sqrt{31}$

The distance between the bob from A is $\theta_0 l [1/2 - \pi \sqrt{6H/g}]$